

CRYSTALLOGRAPHY OF LANARKITE

W. E. RICHMOND AND C. W. WOLFE,
Harvard University, Cambridge, Mass.

Lanarkite, Pb_2SO_5 , has been found in measurable monoclinic crystals only from the Susanna Mine, Leadhills, Lanarkshire, Scotland (Hedde, 1901). The only complete description of these crystals was given by Schrauf (1877), who chose pseudorectangular axes ($\beta = 91^\circ 49'$). Goldschmidt chose a setting with the axes considerably inclined ($\beta = 119^\circ 23'$). Specimens in the Harvard collection from the type locality were examined by Richmond in connection with other work; these proved to be a rich source of new data. X-ray investigation revealed that neither the Schrauf nor the Goldschmidt settings were in agreement with that of the simplest structural cell.

X-Ray Determinations. A carefully selected crystal, approximately 0.5 millimeter long, was employed for rotation and Weissenberg photographs. The results of measurements and calculations of the photographs gave the following cell edge lengths for the base-centered lattice which was chosen: $a_0 = 13.73\text{\AA}$, $b_0 = 5.68\text{\AA}$, $c_0 = 7.07\text{\AA}$; $a_0 : b_0 : c_0 = 2.417 : 1 : 1.245$, $\beta = 116^\circ 13'$.

The choice of the correct axial directions in this case, except for the b -axis, which is fixed by symmetry considerations, is not without ambiguity. If, in the reciprocal lattice, the three shortest translations, with c^* greater than a^* , are chosen, giving the cell with the least axial obliquity, the following reflections are observed on the Weissenberg pictures:

- (hkl)—with $h+k+l$, even
- ($h0l$)—with $h+k$, even
- ($0k0$)—with k , even

The criterion, (hkl) with $h+k+l$, even, indicates a body-centered or "I" lattice. As there are, conventionally, only two types of monoclinic lattices, the primitive and the face-centered, it is advisable to choose a cell which may be referred to one of these lattice types.

A face-centered lattice may be obtained if the next shortest translation is taken for c^* , with a^* and b^* remaining identical with the a^* and b^* of the body-centered cell. The reflections appearing from this lattice are:

- (hkl)—with $h+k$, even
- ($h0l$)—with h , even
- ($0k0$)—with k , even

The criterion (hkl) with $h+k$, even, is that for the base-centered or "C" lattice, which is adopted for the mineral. The space group, fixed by the above criteria plus the fact that a morphological investigation showed

to the base-centered setting, with those obtained by x -ray analysis is given below.

	$a:b:c$	β
Richmond and Wolfe	2.4137:1:1.2363	116°06'
Schrauf	2.4149:1:1.2424	115 48
X -ray	2.417 :1:1.245	116 13

There is essential agreement between the various elements, although Schrauf's value for β departs from the x -ray value by 0°25'. Because of this agreement, Schrauf's values are retained.

Schrauf's elements may be transformed to the base-centered setting by the method of Wolfe (1937), using the transformation formula, $\frac{1}{2}0\frac{1}{2}/0\frac{1}{3}0/\frac{1}{4}0\frac{1}{4}$. Similarly, Goldschmidt's elements, derived from Schrauf's work, may be transformed to the base-centered setting by the formula, $\frac{1}{3}0\frac{2}{3}/0\frac{1}{3}0/\frac{1}{6}0\frac{1}{6}$. The reverse transformations are, respectively: $\bar{1}0\bar{2}/0\bar{3}0/\bar{1}0\bar{2}$ and $\bar{1}0\bar{4}/0\bar{3}0/\bar{1}0\bar{2}$. The meaning of these transformations in the space-lattice is readily observed in Fig. 1.

Five new, well-authenticated forms were observed. In the discussion which follows, the indices refer to the "C" lattice. The new forms are: $c\{001\}$, $d\{103\}$, $E\{403\}$, $R\{\bar{8}01\}$, and $P\{\bar{1}11\}$. All were seen at least twice in good position and, except for $d\{103\}$, were sufficiently prominent to be figured (Fig. 2). In addition, the forms $m\{110\}$, $f\{201\}$ (with indistinct cleavage), $F\{201\}$ (with perfect cleavage), and $U\{401\}$ (with indistinct cleavage), first observed by Schrauf, were each observed several times in this study.

Five other forms— $\{100\}$, $\{101\}$, $\{\bar{1}01\}$, $\{401\}$, and $\{601\}$ —were each observed twice, but the reflections were of poor quality. These forms, therefore, require confirmation. $\sigma\{205\}$ and $s\{9.10.3\}$, observed by Schrauf, were not seen by the authors.

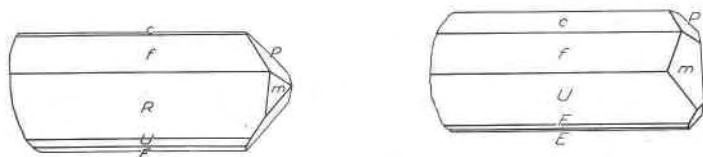


FIG. 2. Lanarkite—Typical crystals from Leadhills, Scotland.

A tabulated comparison of the measured and calculated values for the new, certain forms is given in Table 1. As the crystals are always elongated parallel to the b -axis, measurement of the crystals was made with this axis vertical. The ϕ and ρ angles obtained in this orientation correspond to ϕ_2 and ρ_2 of the angle table, and direct comparison may thus be made.

TABLE 1. LANARKITE: MEASURED AND CALCULATED ANGLES

Form	No. xls.	No. times	Measured Range			Weighted Mean		Calculated	
			ϕ_2		ρ_2	ϕ_2	ρ_2	ϕ_2	ρ_2
001	3	3	63°47'–	64°23'	90°00'–	64°07'	90°00'	64°12'	90°00'
103	2	2	55 50	55 55	90 00	55 53	90 00	56 01½	90 00
403	2	2	105 13	105 20	90 00	105 18	90 00	105 34	90 00
801	7	11	164 38	166 05	90 00	165 15	90 00	166 15	90 00
111	5	9	94 03	95 19	38 58–39°07'	95 04	39 03	95 03	38 56½

The indices for all of the forms noted in the literature in the base-centered, Schrauf, and Goldschmidt settings are given below. The new forms are marked with an asterisk.

Base-centered		Schrauf	Goldschmidt
<i>c</i>	001*	101	201
<i>m</i>	110	<i>z</i> 131	<i>z</i> 131
<i>d</i>	103*	705	13.0.5
σ	205	σ 302	σ 11.0.4
<i>E</i>	403*	105	405
<i>f</i>	201	<i>a</i> 100	<i>a</i> 100
<i>F</i>	201	<i>c</i> 001	<i>c</i> 102
<i>U</i>	401	<i>u</i> 103	<i>u</i> 001
<i>R</i>	801*	305	205
<i>P</i>	111*	133	111
Unconfirmed			
	100*	101	101
	101*	301	501
	101*	103	101
	401*	301	401
	601*	201	502
	9.10.3	<i>s</i> 1.10.5	<i>s</i> 1.10.5
Discarded			
	234.4.57	<i>v</i> 10.1.29	1.2.58
	75.4.18	<i>w</i> 13.4.37	1.4.37
	24.2.57	τ 23.1.15	42.1.15

Vicinal forms similar to the last three listed above were observed on the larger crystals. In all cases they were too dull for accurate measurement, and are apparently solution forms. The faces on the smaller crystals, however, gave clear, bright reflections with rational indices. It seems advisable to discard the vicinal forms from the form list.

An angle table, summarizing the crystallographic elements and angles, is given below.

TABLE 2. LANARKITE: ANGLE TABLE

Lanarkite—Pb ₂ SO ₅							
Monoclinic; prismatic—2/m							
$a:b:c=2.4149:1:1.2424$; $\beta=115^{\circ}48'$; $p_0:q_0:r_0=0.5145:1.1186:1$							
$r_2:p_2:q_2=0.8940:0.4600:1$; $\mu=64^{\circ}12'$; $p_0'=0.5714$, $q_0'=1.2424$, $x_0'=0.4834$							
Forms	ϕ	ρ	ϕ_1	$\rho_1=A$	ϕ_2	$\rho_2=B$	Dana '92
<i>c</i> 001	90°00'	25°48'	64°12'	90°00'	0°00'	64°12'	
<i>m</i> 110	24 42	90 00	0 00	24 42	79 33	65 18	<i>z</i>
<i>d</i> 103	90 00	33 58½	56 01½	90 00	8 10½	56 01½	
<i>o</i> 205	90 00	35 27	54 33	90 00	9 39	54 33	<i>σ</i>
<i>E</i> 403	-90 00	15 34	105 34	90 00	41 22	105 34	
<i>f</i> 201	90 00	58 24½	31 35½	90 00	32 36½	31 35½	<i>ā</i>
<i>F</i> 201	-90 00	33 24	123 24	90 00	59 12	123 24	<i>c</i>
<i>U</i> 401	-90 00	60 58½	150 58½	90 00	86 46½	150 58½	<i>u</i>
<i>R</i> 801	-90 00	76 15	166 15	90 00	102 03	166 15	
<i>P</i> 111	- 4 03	51 14½	95 03	38 56½	57 20	93 09½	

Unconfirmed:—{100}, {101}, {101}, {401}, {601}, {9.10.3}

Discarded:—{8.2.57}, {234.4.57}, {75.4.18}

OPTICS

The refractive indices and optical orientation were determined by the immersion method, giving the following results:

	$n(\text{Na})$	
X	1.928	} ±0.003 negative 2V=60°±2°
Y=b	2.007	
Z∧c=30°	2.036	

CHEMISTRY

Using an existing analysis by E. Pisani (1873) and a density 6.92, determined here by the float method, together with the cell volume, $V_0=494.4$, the contents of the unit cell were determined and are given in the following table:

TABLE 3. LANARKITE: ATOMIC CONTENT OF UNIT CELL

	1		2	3	4
PbO	84.63	Pb	0.379	7.86	8
SO ₃	15.37	S	.191	3.96	4
		O	.952	19.74	20

1. Lanarkite, Leadhills, Scotland. Analysis reduced to 100%. Analyst, E. Pisani (1873).
2. Atomic proportions.
3. Number of atoms in unit cell yielding the formula Pb₈S₄O₂₀.
4. Theoretical number of atoms in unit cell for $M_0=2073.8$.

ACKNOWLEDGMENTS

The authors wish to acknowledge the help they have received during the preparation of this paper from Professor Palache and Dr. Berman and from Professor Peacock of Toronto.

REFERENCES

- Goldschmidt, Victor (1890): *Index der Krystallformen der Mineralien*, vol. 2, p. 281.
 Heddle, M. F. (1901): *The Mineralogy of Scotland*, vol. 2, pp. 174-175.
 Pisani, E. (1873): *Compte Rendus*, vol. 76, p. 114.
 Schrauf, A. (1877): *Zeits. Krist.*, vol. 1, pp. 31-38.
 Wolfe, C. W. (1937): *Am. Mineral.*, vol. 22, pp. 736-741.