

## CRYSTALLOGRAPHIC TABLES FOR THE RHOMBOHEDRAL CARBONATES

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### ABSTRACT

Cell constants are given for  $\text{CaCO}_3$ ,  $\text{MgCO}_3$ ,  $\text{CaMg}(\text{CO}_3)_2$ ,  $\text{MnCO}_3$ ,  $\text{FeCO}_3$ ,  $\text{ZnCO}_3$ ,  $\text{CoCO}_3$ ,  $\text{NiCO}_3$ , and  $\text{CdCO}_3$ , together with listings of all possible  $d$ -values for powder diagrams taken with  $\text{CuK}\alpha_1$  radiation. Less complete information is presented for  $\text{CuCO}_3$ ,  $\text{Mg}_5\text{Ca}(\text{CO}_3)_4$ ,  $\text{CaMn}(\text{CO}_3)_2$ ,  $\text{CdMg}(\text{CO}_3)_2$ , and the hypothetical end member,  $\text{CaFe}(\text{CO}_3)_2$ . Samples of some of these materials prepared at or near room temperature have unit cells distinctly larger than those of equivalent samples prepared at higher temperature.

Amplitude contributions to the structure factors of calcite and dolomite powder reflections are given, based upon recently refined parameters cited in the literature. Front reflection intensities, based upon a simplified model essentially involving spherical neutral atoms at rest, are computed for a number of carbonates.

### INTRODUCTION

The rhombohedral carbonate solid solutions, because of their widespread occurrence in a variety of geochemical environments, are important in evaluating the conditions under which various rocks formed. They are also of theoretical interest in a variety of solid-state studies. X-ray diffraction probably is the single most valuable technique for characterizing these materials. The change of unit-cell size among rhombohedral  $\text{CaMg}$  and  $\text{CaMn}$  carbonate solid solutions has been shown to be sufficient to allow the positions of suitably located individual back reflections on films taken with standard 114.59 mm. diameter powder cameras to be used as accurate measures of composition (Goldsmith, Graf and Joensuu, 1955; Goldsmith and Graf, 1957; Goldsmith and Graf, 1958b; Goldsmith, Graf, and Heard, 1961). The Debye-Scherrer method is particularly suitable for samples too small to utilize the maximum potential accuracy of the diffractometer.

Such back reflection measurements will yield useful information regardless of the indices of the particular reflection. Major advantages, however, are derived from considering the indices of the various back reflections:

- 1) More accurate values of the cell constants,  $a_0$  and  $c_0$ , may be obtained by making extrapolations using reflections having, respectively, very large  $a$ -axis and  $c$ -axis components. Because reflections of this nature are limited in number, the procedure is most effective when various characteristic X-radiations may be utilized in order to bring the desired reflections as close as possible to  $2\theta = 180^\circ$ ;

- 2) The change in  $c:a$  ratio between some pairs of carbonates is great enough to cause appreciable differential shifts in the positions of nearby reflections. The change of separation of such reflections becomes in itself an accurate measure of the extent of solid solution; film shrinkage can be

ignored over such a small portion of the film and errors varying with  $\theta$  can be assumed to affect the two reflections equally and thus to cancel. The differential shift will be a maximum if one of the reflections has a strong  $c$ -axis component and the other, a strong  $a$ -axis component;

3) The spacings of reflections with strong  $c$ -axis components from carbonates with mixed-layer progressions along the  $c$ -axis (Graf, Blyth, and Stemmler, 1957; Goldsmith and Graf, 1958*b*; Graf, Blyth, and Stemmler, 1958) are altered because of this arrangement, and compositional measurements of such materials are best carried out using reflections with little or no  $c$ -axis component.

The back reflections of the rhombohedral carbonates are numerous enough so that interference or superposition of two or more reflections is not uncommon. Reliable unit-cell and  $d$ -spacing values for pure, well crystallized end members and ordered 1:1 compounds are, therefore, a prerequisite if diffraction diagrams of intermediate solid solutions and poorly crystallized materials are to yield maximum information. Tables 1 and 2 are a somewhat expanded version of a compilation of these quantities which has proved its usefulness. The accurate values given in Table 3 of the angles between  $[c]$  and the various plane normals of  $\text{CaMg}(\text{CO}_3)_2$  may be used to estimate the orientation of planes in the other carbonates.

Intensities are important in evaluating cation and anion disorder and in estimating compositions of solid solutions between carbonates whose cations are very similar in size, such as  $\text{ZnCO}_3$  and  $\text{CoCO}_3$ , and the ferroan dolomites,  $\text{Ca}(\text{Mg}, \text{Fe})(\text{CO}_3)_2$ . The amplitude contributions of the several kinds of atoms to the structure factor are presented in Table 3 for the various reflections of  $\text{CaCO}_3$  and  $\text{CaMg}(\text{CO}_3)_2$ , the only two rhombohedral carbonates for which variable parameters have been determined. These values were used in calculating the relative intensities of calcite and dolomite reflections out to  $\{00 \cdot 12\}$  which are given in Table 4. The parameter approximations made in calculating analogous intensities for the other carbonates of Table 4 are discussed in a later section of the paper.

Measurements of reflection profiles and of the amounts of carbonates present in mixtures typically utilize low-angle reflections. Table 5 gives the  $2\theta$  values for such reflections from the more common rhombohedral carbonates for  $\text{CuK}\alpha_1$  radiation.

#### UNIT-CELL DIMENSIONS

Table 6 summarizes the methods used in preparing the various materials for which unit-cell dimensions were determined. It also gives spectro-

TABLE 1. PREFERRED CELL CONSTANTS FOR THE RHOMBOHEDRAL CARBONATES\*

Material	$a_0$	$c_0$	$c_0/a_0$	$a_{rh}$	$\alpha$
CaCO <sub>3</sub>					
20° C.	4.9900	17.061 <sub>5</sub>	3.4191	6.3753	46° 4.6'
26° C.	4.9899	17.064	3.4197	6.3760	46° 4.3'
CaMg(CO <sub>3</sub> ) <sub>2</sub>					
(ordered)	4.8079	16.010	3.3299	6.0154	47° 6.6'
Ca <sub>50</sub> Mg <sub>50</sub> †	4.8114 <sub>5</sub>	16.039 <sub>5</sub>	3.3336	6.0251	47 4.0'
MgCO <sub>3</sub>	4.6330	15.016	3.2411	5.6752	48° 10.9'
MnCO <sub>3</sub>	4.7771	15.664	3.2790	5.9050	47° 43.1 <sub>5</sub> '
CaMn(CO <sub>3</sub> ) <sub>2</sub>					
(disordered)	4.8797	16.367	3.3541		
Ca <sub>50</sub> Mn <sub>50</sub> †	4.8835	16.364	3.3509	6.1402 <sub>5</sub>	46° 51.8 <sub>5</sub> '
FeCO <sub>3</sub>	4.6887	15.373	3.2787	5.7954	47° 43.3'
Ca <sub>50</sub> Fe <sub>50</sub> †	4.8393	16.218 <sub>5</sub>	3.3514	6.0855	46° 51.5'
ZnCO <sub>3</sub>	4.6528	15.025	3.2292	5.6833	48° 19.6'
CdCO <sub>3</sub>	4.9204	16.298	3.3123	6.1306	47° 19.1 <sub>5</sub> '
CoCO <sub>3</sub>	4.6581	14.958	3.2112	5.6650 <sub>5</sub>	48° 33.1'
Cd <sub>50</sub> Mg <sub>50</sub> †	4.7767	15.657	3.2778	5.9028 <sub>5</sub>	47° 44.0'
CdMg(CO <sub>3</sub> ) <sub>2</sub>					
(ordered)	4.7770	15.641	3.2742		
	±0.0009‡	±0.003‡			
CdMg(CO <sub>3</sub> ) <sub>2</sub>					
(disordered)	4.7746	15.678	3.2836		
	±0.0009‡	±0.03‡			
NiCO <sub>3</sub>	4.5975	14.723	3.2024	5.5795	48° 39.7'

\* Pistorius (1960) has synthesized what appear to be mixtures of malachite and the anhydrous rhombohedral cupric carbonate, CuCO<sub>3</sub>. Seven powder diffraction lines of the latter material give, from least square analysis,  $a_0=4.796\pm 0.005$  Å,  $c_0=15.48\pm 0.01$  Å,  $c_0/a_0=3.227$ ,  $\alpha=48^\circ 11'$ ,  $a_{rh}=5.856$  Å.

† Hypothetical solid solutions with  $a_0$  and  $c_0$  midway between those of the two end members.

‡ The ranges given for  $a_0$  and  $c_0$  of ordered and disordered CdMg(CO<sub>3</sub>)<sub>2</sub> indicate only the uncertainty that would result from a misreading of line position on the films (taken with a Guinier-type focusing camera) by the smallest unit measured, 0.05 mm. The procedure used in obtaining these CdMg(CO<sub>3</sub>)<sub>2</sub> values is summarized in Table 7.

graphic analyses of those cations considered most likely to enter into solid solution in the carbonates. The analyses are computed with all cations as carbonates in solid solution, the most severe assumption possible inasmuch as some of the impurities may be present as traces of other compounds. Of the impurities detected, the 0.38 mol percent CaCO<sub>3</sub> in the MgCO<sub>3</sub> is the most significant, both because of the absolute amount and because the large size difference between Ca<sup>++</sup> and Mg<sup>++</sup> results in maximum spacing change. Assuming a linear relation between cell size

TABLE 2. POSSIBLE X-RAY REFLECTIONS FOR THE RHOMBOHEDRAL CARBONATES IN DEBYE-SCHERRER DIAGRAMS TAKEN WITH  $\text{CuK}\alpha_1$  RADIATION

$h \cdot k \cdot l$	$h \cdot k \cdot l$	$\text{MgCO}_3$	$\text{CaMg}(\text{CO}_3)_2$	$\text{Ca}_{50}\text{Mg}_{50}^*$	$\text{CaCO}_3$ (26° C.)	$\text{Ca}_{50}\text{Fe}_{50}^*$	$\text{FeCO}_3$	$\text{Ca}_{50}\text{Mn}_{50}^*$	$\text{MnCO}_3$	$\text{ZnCO}_3$	$\text{CdCO}_3$	$\text{CoCO}_3$	$\text{NiCO}_3$
00·3	111		5.3366	5.3645		5.4062		5.4547					
10·1	100		4.0297	4.0330		4.0577		4.0947					
01·2	110	3.5387	3.6939	3.6975	3.8551	3.7233	3.5903	3.7570	3.6581	3.5509	3.7761	3.5505	3.5021
10·4	211	2.7412	2.8855	2.8893	3.0359	2.9141	2.7912	2.9404	2.8440	2.7476	2.9449	2.7424	2.7028
00·6	222	2.5027	2.6683	2.6733	2.8440	2.7031	2.5622	2.7273	2.6107	2.5042	2.7163	2.4930	2.4538
01·5	201		2.5382	2.5419		2.5651		2.5883					
11·0	101	2.3165	2.4039	2.4057	2.4949	2.4197	2.3443	2.4417	2.3886	2.3264	2.4602	2.3291	2.2988
11·3	210	2.1023	2.1918	2.1939	2.2848	2.2085	2.1318	2.2286	2.1721	2.1099	2.2411	2.1102	2.0817
02·1	111		2.0645	2.0661		2.0782		2.0972					
20·2	200	1.9832	2.0149	2.0165	2.0946	2.0288	1.9629	2.0473	2.0000	1.9460	2.0613	1.9474	1.9217
10·7	322		2.0046	2.0078		2.0277		2.0460					
02·4	220	1.7693	1.8470	1.8488	1.9275	1.8616	1.7952	1.8785	1.8290	1.7754	1.8880	1.7752	1.7511
01·8	332	1.7002	1.8037	1.8067	1.9127	1.8250	1.7369	1.8414	1.7698	1.7023	1.8380	1.6964	1.6705
11·6	321	1.7000	1.7860	1.7882	1.8755	1.8029	1.7296	1.8192	1.7623	1.7044	1.8235	1.7019	1.6776
00·9	333		1.7789	1.7822		1.8021		1.8182					
20·5	311		1.7454	1.7473		1.7601		1.7761					
21·1	201	1.5088	1.5662	1.5674	1.6259	1.5765	1.5271	1.5909	1.5559	1.5152	1.6028	1.5169	1.4971
12·2	211	1.4865	1.5442	1.5454	1.6042	1.5547	1.5050	1.5688	1.5334	1.4926	1.5800	1.4940	1.4744
02·7	331		1.5396	1.5415		1.5541		1.5682					
10·10	433	1.4063	1.4943	1.4969	1.5872	1.5125	1.4377	1.5261	1.4649	1.4078	1.5223	1.4025	1.3809
21·4	310	1.4061	1.4646	1.4659	1.5253	1.4754	1.4253	1.4889	1.4522	1.4114	1.4978	1.4119	1.3930
20·8	422	1.3706	1.4428	1.4447	1.5180	1.4570	1.3956	1.4702	1.4220	1.3728	1.4724	1.3712	1.3514
11·9	432	1.3538	1.4300	1.4320	1.5096	1.4453	1.3805	1.4583	1.4066	1.3563	1.4584	1.3529	1.3328
12·5	320	1.3537	1.4124	1.4137	1.4733	1.4234	1.3732	1.4363	1.3991	1.3585	1.4439	1.3585	1.3400
03·0	112	1.3374	1.3879	1.3889	1.4404	1.3970	1.3535	1.4097	1.3790	1.3432	1.4204	1.3447	1.3272

\* Hypothetical solid solutions with  $a_0$  and  $c_0$  midway between those of the two end members.

<i>hk.l</i>	<i>h.k.l</i>	MgCO <sub>3</sub>	CaMg(CO <sub>3</sub> ) <sub>2</sub>	Ca <sub>50</sub> Mg <sub>50</sub> *	CaCO <sub>3</sub> (26° C.)	Ca <sub>50</sub> Fe <sub>50</sub> *	FeCO <sub>3</sub>	Ca <sub>50</sub> Mn <sub>50</sub> *	MnCO <sub>3</sub>	ZnCO <sub>3</sub>	CaCO <sub>3</sub>	CoCO <sub>3</sub>	NiCO <sub>3</sub>
01-11	443		1.3739	1.3763		1.3908		1.4034					
{30-3	300		1.3432	1.3443		1.3526		1.3649					
221	221												
{03-3	444	1.2513	1.3342	1.3366	1.4220	1.3515	1.2811	1.3637	1.3053	1.2521	1.3582	1.2465	1.2269
00-12	444	1.2383	1.2965	1.2979	1.3569	1.3076	1.2580	1.3195	1.2817	1.2421	1.3246	1.2412	1.2239
21-7	421	1.2021	1.2691	1.2709	1.3391	1.2826	1.2256	1.2942	1.2488	1.2044	1.2945	1.2015	1.1837
02-10	442												
12-8	431	1.1796	1.2371	1.2385	1.2968	1.2482	1.1992	1.2595	1.2219	1.1829	1.2634	1.1816	1.1650
{30-6	411	1.1796	1.2313	1.2325	1.2850	1.2410	1.1968	1.2523	1.2194	1.1836	1.2587	1.1835	1.1674
330	330												
{03-6	202	1.1583	1.2020	1.2029	1.2475	1.2098	1.1722	1.2209	1.1943	1.1632	1.2301	1.1645	1.1494
22-0	202												
20-11	533		1.1929	1.1946		1.2058		1.2167					
10-13	544		1.1810	1.1830		1.1937		1.2065					
22-3	311	1.1284	1.1726	1.1735	1.2185	1.1806	1.1427	1.1914	1.1642	1.1330	1.1997	1.1340	1.1191
11-12	543	1.1010	1.1665	1.1684	1.2354	1.1799	1.1242	1.1906	1.1454	1.1025	1.1890	1.0990	1.0824
13-1	212	1.1098	1.1518	1.1527	1.1956	1.1594	1.1232	1.1700	1.1444	1.1145	1.1787	1.1157	1.1012
31-2	301	1.1008	1.1430	1.1439	1.1869	1.1506	1.1143	1.1611	1.1353	1.1054	1.1696	1.1065	1.0921
21-10	532	1.0670	1.1223	1.1238	1.1799	1.1332	1.0861	1.1435	1.1066	1.0696	1.1456	1.0678	1.0524
13-4	321	1.0669	1.1096	1.1105	1.1539	1.1174	1.0807	1.1275	1.1011	1.0712	1.1351	1.0719	1.0577
01-14	554	1.0362	1.1027	1.1047	1.1731	1.1166	1.0600	1.1266	1.0801	1.0371	1.1230	1.0328	1.0168
22-6	420	1.0511	1.0959	1.0969	1.1424	1.1043	1.0659	1.1143	1.0860	1.0549	1.1206	1.0551	1.0409
{03-9	441												
522	522												
31-5	410	1.0435	1.0863	1.0873	1.1308	1.0942	1.0575	1.1042	1.0774	1.0475	1.1111	1.0480	1.0340
12-11	542	1.0146	1.0685	1.0700	1.1248	1.0792	1.0333	1.0890	1.0528	1.0169	1.0904	1.0148	1.0001
00-15	555		1.0673	1.0693		1.0812		1.0909					
02-13	553		1.0600	1.0616		1.0720		1.0816					



<i>hk.l</i>	<i>h<sub>1</sub>k<sub>1</sub>l<sub>1</sub></i>	MgCO <sub>3</sub>	CaMg(CO <sub>3</sub> ) <sub>2</sub>	Ca <sub>30</sub> Mg <sub>50</sub> *	CaCO <sub>3</sub> (26° C.)	Ca <sub>50</sub> Fe <sub>50</sub> *	FeCO <sub>3</sub>	Ca <sub>50</sub> Mn <sub>50</sub> *	MnCO <sub>3</sub>	ZnCO <sub>3</sub>	CaCO <sub>3</sub>	CaCO <sub>3</sub>	NiCO <sub>3</sub>
22-12	642	.85001	.89301	.89411	.93777	.90143	.86479	.90960	.88113	.85219	.91173	.91173	.83881
00-18	666	.83422	.88944	.89109	.94801	.90103	.85405	.90911	.87022	.83472	.90545	.85095	.81794
32-7	520	.84590	.88144	.88224	.91835	.88805	.85759	.89613	.87377	.84902	.90136	.84924	.83783
40-10	622	.83409	.87269	.87363	.91278	.88007	.84711	.88806	.86310	.83671	.89171	.83620	.82461
23-8	530	.82646	.86206	.86288	.89903	.86873	.83824	.87663	.85406	.82939	.88136	.82943	.81820
{41-6	510}	.82644	.86011	.86084	.89508	.86630	.83741	.87420	.85321	.82964	.87975	.83007	.81902
{14-6	431}												
20-17	755		.85805	.85948		.86827		.87609					
04-11	551		.84668	.84762		.85406		.86181					
{03-15	663}					.85505		.86277					
{30-15	744}		.84608	.84729									
21-16	754	.79804	.84439	.84568	.89299	.85380	.81438	.86150	.82978	.79932	.86089	.79698	.78506
13-13	652	.80140	.84239	.84345	.88508	.85045	.81553	.85815	.83093	.80340	.85997	.80213	.79065
11-18	765	.78488	.83417	.83560	.88619	.84438	.80246	.85198	.81764	.78567	.84972	.78267	.77061
05-1	225		.83163	.83224		.83708		.84472					
50-2	114	.79792	.82828	.82890	.85987	.83375	.80761	.84136	.82284	.80129	.84761	.80216	.79169
10-19	766		.82589	.82738		.83643		.84394					
32-10	631	.78477	.82031	.82116	.85722	.82706	.79699	.83458	.81173	.78733	.83834	.78701	.77618
05-4	332	.78473	.81529	.81593	.84706	.82084	.79456	.82833	.80954	.78796	.83419	.78866	.77830
31-14	743	.77226	.81257	.81363	.85459	.82053	.78620	.82795	.80106	.77408	.82936	.77270	
{14-9	540}	.77529	.80916	.80995	.84433	.81553	.78655	.82295	.80139	.77798	.82719	.77792	
{41-9	621}												
12-17	764		.80812	.80937	.85519	.81725	.77910	.82462	.79384				
50-5	500		.80594	.80659	.83164	.81154	.78145	.81893	.79618	.77546	.82007	.77635	
33-0	303		.80131	.80191		.80655		.81392					





TABLE 3. AMPLITUDE CONTRIBUTIONS TO STRUCTURE FACTORS, AND ANGLES BETWEEN [c] AND PLANE NORMALS, FOR CALCITE AND DOLOMITE

<i>hk.l</i>	<i>h<sub>r</sub>k<sub>r</sub>l<sub>r</sub></i>	Amplitude contributions* to structure factors, F, for calcite			Amplitude contributions* to structure factors, F, for dolomite				Angle between plane normal and [c], for dolomite, in degrees
		<i>f<sub>Ca</sub></i>	<i>f<sub>C</sub></i>	<i>f<sub>O</sub></i>	<i>f<sub>Ca</sub></i>	<i>f<sub>Mg</sub></i>	<i>f<sub>C</sub></i>	<i>f<sub>O</sub></i>	
00·3	111				+1	-1	-0.2444	-0.6771	0
10·1	100				+1	-1	+0.0817	-0.3761	75.422
01·2	110	+2	-2	-1.8040	+1	+1	-1.9933	-1.7952	62.519
10·4	211	+2	+2	+1.8040	+1	+1	+1.9734	+1.8801	43.869
00·6	222	+2	-2	-6.0000	+1	+1	-1.9402	-5.8472	0
01·5	221				+1	-1	+0.4056	+0.7814	37.562
11·0	10 $\bar{1}$	+2	+2	-2.1864	+1	+1	+2.0000	-2.1095	90
11·3	210			+4.1910	+1	-1	-0.2444	{+4.1187 -3.6426	65.751
02·1	11 $\bar{1}$				+1	-1	+0.0817	+1.6286	82.591
20·2	200	+2	-2	+1.9808	+1	+1	-1.9933	+1.9509	75.422
10·7	322				+1	-1	-0.5640	-0.0482	28.782
02·4	220	+2	+2	-1.9808	+1	+1	+1.9734	-2.3185	62.518
01·8	332	+2	+2	+1.8040	+1	+1	+1.8942	+1.6189	25.672
11·6	321	+2	-2	+2.1864	+1	+1	-1.9402	{+1.1798 +2.9316	47.985
00·9	333				+1	-1	+0.7187	+1.9969	0
20·5	311				+1	-1	+0.4056	-2.0689	56.969
21·1	20 $\bar{1}$			+3.7802	+1	+1	+0.0817	{-4.4674 +2.7560 +0.6004 +2.8753	84.386
12·2	21 $\bar{1}$	+2	-2	+1.7954	+1	+1	-1.9933		78.878
02·7	331				+1	-1	-0.5640	-1.1053	47.689
10·10	433	+2	-2	-1.8040	+1	+1	-1.8355	-1.8692	21.036
21·4	310	+2	+2	-1.7954	+1	+1	+1.9734	{-1.8669 -1.2224	68.535
20·8	422	+2	+2	-1.9808	+1	+1	+1.8942	-1.4839	43.867
11·9	432			+4.1910	+1	-1	+0.7187	{-4.3850 +3.0204 -2.8915 +3.8184	36.499
12·5	320			+3.7802	+1	-1	+0.4056		63.826
03·0	11 $\bar{2}$	+2	+2	+2.5860	+1	+1	+2.0000	+1.9259	90
01·11	443				+1	-1	-0.8686	-1.1467	19.271
30·3	300				+1	-1	-0.2444	{+0.8776 -1.3123	75.422
03·3	22 $\bar{1}$								
00·12	444	+2	+2	+6.0000	+1	+1	+1.7646	+5.3964	0
21·7	421			+3.7802	+1	-1	-0.5640	{+4.8888 -2.4801	55.468

\* The amplitude contributions have been divided by 6 in order to obtain expressions corresponding to the contents of the rhombohedral unit cell.

TABLE 3—(continued)

$hk \cdot l$	$h_r k_r l_r$	Amplitude contributions* to structure factors, F, for calcite			Amplitude contributions* to structure factors, F, for dolomite				Angle between normal and normal and [c], for dolomite, in degrees
		$f_{Ca}$	$f_C$	$f_O$	$f_{Ca}$	$f_{Mg}$	$f_C$	$f_O$	
02·10	442	+2	-2	+1.9808	+1	+1	-1.8355	+2.5679	37.562
12·8	431	+2	+2	-1.7954	+1	+1	+1.8942	+0.0523	51.818
30·6	411	+2	-2	-2.5860	+1	+1	-1.9402	-3.7372	62.519
03·6	330							-2.1240	
22·0	20 $\bar{2}$	+2	+2	-2.0192	+1	+1	+2.0000	-1.1830	90
20·11	533				+1	-1	-0.8686	+2.4039	34.955
10·13	544				+1	-1	+1.0127	+0.4701	16.470
22·3	31 $\bar{1}$			-0.7811	+1	-1	-0.2444	-0.2913	77.307
								+0.5583	
11·12	543	+2	+2	-2.1864	+1	+1	+1.7646	-0.1901	29.035
								-3.6045	
13·1	21 $\bar{2}$			-0.3704	+1	-1	+0.0817	+0.0978	85.875
								-1.0696	
31·2	30 $\bar{1}$	+2	-2	-2.1566	+1	+1	-1.9933	+0.4957	81.791
								-4.4963	
21·10	532	+2	-2	+1.7954	+1	+1	-1.8355	+0.7635	45.493
								+1.7822	
13·4	32 $\bar{1}$	+2	+2	+2.1566	+1	+1	+1.9734	+4.4742	73.905
								-0.2543	
01·14	554	+2	-2	-1.8040	+1	+1	-1.6819	-1.3600	15.365
22·6	420	+2	-2	+2.0192	+1	+1	-1.9402	+1.2488	65.751
								+1.0570	
03·9	441	+2	-2		+1	-1	+0.7187	+1.6801	52.036
30·9	522							-0.3982	
31·5	410			-0.3704	+1	-1	+0.4056	+0.9577	70.169
								+0.9170	
12·11	542			+3.7802	+1	-1	-0.8686	+2.8797	42.766
								-2.9749	
00·15	555				+1	-1	-1.1500	-3.2150	0
02·13	553				+1	-1	+1.0127	+0.5257	30.603
04· $\bar{1}$	11 $\bar{3}$				+1	-1	+0.0817	+0.3301	86.280
04·2	222	+2	-2	-5.9232	+1	+1	-1.9933	-4.8835	82.591
13·7	430			-0.3704	+1	-1	-0.5640	-1.1077	63.209
								+1.1270	
40·4	400	+2	+2	+5.9232	+1	+1	+1.9734	+4.8089	75.422
20·14	644	+2	-2	+1.9808	+1	+1	-1.6819	+0.9413	28.782
31·8	521	+2	+2	+2.1566	+1	+1	+1.8942	-0.7119	60.014
								+4.2893	
22·8	531			-0.7811	+1	-1	+0.7187	+0.0095	60.155
								-0.7969	
04·5	33 $\bar{1}$				+1	-1	+0.4056	+0.7721	71.991

TABLE 3—(continued)

$hk \cdot l$	$h_r k_r l_r$	Amplitude contributions* to structure factors, F, for calcite			Amplitude contributions* to structure factors, F, for dolomite				Angle between plane normal and [c], for dolomite, in degrees
		$f_{Ca}$	$f_C$	$f_O$	$f_{Ca}$	$f_{Mg}$	$f_C$	$f_O$	
11·15	654			+4.1910	+1	-1	-1.1500	+4.4279 -2.1673	23.942
10·16	655	+2	+2	+1.8040	+1	+1	+1.5880	+1.7631	13.514
21·13	643			+3.7802	+1	-1	+1.0127	-5.0611 +2.0778	38.045
30·12 03·12	633 552	+2	+2	+2.5860	+1	+1	+1.7646	+2.2139 +1.2505	43.868
32·1	302			-4.1145	+1	-1	+0.0817	+4.9874 -1.8593	86.586
23·2 40·7	312 511	+2	-2	+2.1826	+1	+1	-1.9933	+0.0903 +2.5584	83.195
					+1	-1	-0.5640	-1.4156	65.528
13·10	541	+2	-2	-2.1566	+1	+1	-1.8355	-4.2242 -0.0001	54.197
32·4	41 $\bar{1}$	+2	+2	-2.1826	+1	+1	+1.9734	-3.6841 +0.3294	76.577
12·14	653	+2	-2	+1.7954	+1	+1	-1.6819	-0.7023 +4.4086	36.005
04·8 01·17	440 665	+2	+2	+5.9232	+1	+1	+1.8942	+4.7092	62.519
					+1	-1	+1.2797	+1.4537	12.745
23·5	42 $\bar{1}$			-4.1145	+1	-1	+0.4056	+1.8389 -5.5649	73.389
14·0	21 $\bar{3}$	+2	+2	+1.3784	+1	+1	+2.0000	+3.4131 -0.8908	90
31·11	632			-0.3704	+1	-1	-0.8686	-0.7970 -1.8852	51.570
02·16	664	+2	+2	-1.9808	+1	+1	+1.5880	-2.6866	25.671
								+0.2011	
14·3 41·3	32 $\bar{2}$ 40 $\bar{1}$			+0.4469	+1	-1	-0.2444	+1.8240 -1.6229 -0.9715	80.338
22·12	642	+2	+2	-2.0192	+1	+1	+1.7646	-1.2509 -0.8771	47.984
00·18	666	+2	-2	-6.0000	+1	+1	-1.4835	-4.6708	0
32·7	520			-4.1145	+1	-1	-0.5640	-4.1559 +1.7849	67.332
40·10	622	+2	-2	-5.9232	+1	+1	-1.8355	-4.4894	56.969
23·8	530	+2	+2	-2.1826	+1	+1	+1.8942	-0.5054 -1.3023	64.484
								+1.2571	
41·6 14·6	510 43 $\bar{1}$	+2	-2	-1.3784	+1	+1	-1.9402	-3.1938 -3.4585 +0.4791	71.196

TABLE 3—(continued)

$hk \cdot l$	$h_r k_r l_r$	Amplitude contributions* to structure factors, F, for calcite			Amplitude contributions* to structure factors, F, for dolomite				Angle between plane normal and [c], for dolomite, in degrees
		$f_{Ca}$	$f_C$	$f_o$	$f_{Ca}$	$f_{Mg}$	$f_C$	$f_o$	
20·17	755				+1	-1	+1.2797	-2.6163	24.341
04·11	551				+1	-1	-0.8686	-1.8350	54.428
03·15	663				+1	-1	-1.1500	-1.9624	37.561
30·15	744						-0.1016	+0.3789	
21·16	754	+2	+2	-1.7954	+1	+1	+1.5880	-2.2512	32.450
13·13	652			-0.3704	+1	-1	+1.0127	+2.0612	46.842
							-1.1270	-0.8094	
11·18	765	+2	-2	+2.1864	+1	+1	-1.4835	+4.0937	20.306
05·1	223				+1	-1	+0.0817	+2.0959	87.023
05·2	114	+2	-2	-1.0296	+1	+1	-1.9933	-0.5718	84.061
10·19	766				+1	-1	-1.4008	-0.8681	11.441
32·10	631	+2	-2	+2.1826	+1	+1	-1.8355	+4.6221	59.178
							-0.7322	+0.0988	
05·4	332	+2	+2	+1.0296	+1	+1	+1.9734	+0.8918	78.247
							-3.8638	+0.5795	
31·14	743	+2	-2	-2.1566	+1	+1	-1.6819	-1.9321	44.720
							+1.3391	+1.6923	
14·9	540			+0.4469	+1	-1	+0.7187	-2.7212	62.944
41·9	621						+1.9798	+1.9798	
12·17	764			+3.7802	+1	-1	+1.2797	-1.9669	30.897
							+0.4056	-1.9669	
50·5	500				+1	-1	+0.4056	-1.7691	75.422
33·0	303	+2	+2	-1.3282	+1	+1	+2.0000	-1.7248	
23·11	641			-4.1145	+1	-1	-0.8686	+5.8588	56.723
							+0.2729	+0.9949	
22·15	753			-0.7811	+1	-1	-1.1500	+2.4289	41.605
							+1.0127	+2.4289	
40·13	733				+1	-1	+1.0127	-1.6477	49.794
							-0.2444	+2.0470	
33·3	412			-3.3772	+1	-1	-0.2444	+1.0319	81.460
							+1.3691	+1.0319	
01·20	776	+2	+2	+1.8040	+1	+1	+1.3691	-3.3813	10.883
							+0.0817	-2.4627	
24·1	313			+0.7735	+1	-1	+0.0817	+1.3808	87.186
							-1.9933	+2.1764	
42·2	402	+2	-2	+1.9430	+1	+1	-1.9933	+1.7233	84.386
							+0.0817	+1.7233	
05·7	441				+1	-1	-0.5640	+0.0808	69.993
02·19	775				+1	-1	-1.4008	+0.0808	

TABLE 3—(continued)

$hk \cdot l$	$h_r k_r l_r$	Amplitude contributions* to structure factors, F, for calcite			Amplitude contributions* to structure factors, F, for dolomite				Angle between plane normal and $[c]$ , for dolomite, in degrees
		$f_{Ca}$	$f_C$	$f_o$	$f_{Ca}$	$f_{Mg}$	$f_C$	$f_o$	
24·4	42 $\bar{2}$	+2	+2	-1.9430	+1	+1	+1.9734	$\begin{cases} -1.4132 \\ -0.8250 \end{cases}$	78.878
04·14	662	+2	-2	-5.9232					48.448†
50·8	611	+2	+2	+1.0296					67.943†
33·6	52 $\bar{1}$	+2	-2	+1.3282					73.700†
42·5	51 $\bar{1}$			+0.7735					76.543†
13·16	763	+2	+2	+2.1566					41.664†
20·20	866	+2	+2	-1.9808					21.546†
30·18	855	+2	-2	-2.5860					33.350†
03·18	774								
32·13	742			-4.1145					52.937†
21·19	865			+3.7802					28.805†
41·12	732	+2	-2	-1.3784					56.449†
14·12	651								
15· $\bar{1}$	21 $\bar{4}$			+4.5175					87.396†
24·7	53 $\bar{1}$			+0.7735					71.479†
15·2	32 $\bar{3}$	+2	-2	+2.4974					84.802†
11·21	876			+4.1910					18.040†
05·10	550	+2	-2	-1.0296					63.138†

† These angles are for calcite (26° C.).

and composition, 0.38 mol percent substituted  $\text{CaCO}_3$  in  $\text{MgCO}_3$  would produce a change of 0.0005 Å in a 1 Å basal reflection and 0.0003 Å in a 1 Å reflection with no  $c$ -axis component. These differences would be readily measurable in the back reflection region of films taken with a 114.59 mm. diameter powder camera such as that used in this work.\*

The other impurities in Table 6, where they are greater than the limit of detection, would probably not produce detectable spacing changes. The  $\text{Li}_2\text{CO}_3$  used to facilitate recrystallization of some of these samples in runs made with a squeezer-type apparatus (Griggs and Kennedy, 1956) has never been observed to lead to changed spacings in cases where carbonates were initially well crystallized and careful comparisons of back-reflection spacings before and after the run could be made.

\* The slight equilibrium substitution of  $\text{CaCO}_3$  in  $\text{MgCO}_3$  at higher temperatures (Harker and Tuttle, 1955) suggests that the 0.38 mol percent  $\text{CaCO}_3$  here computed is probably not all present in solid solution.

TABLE 4. COMPUTED RELATIVE INTENSITIES OF FRONT REFLECTIONS IN POWDER DIAGRAMS OF THE RHOMBOHEDRAL CARBONATES AND THE HYPOTHETICAL END MEMBER,  $\text{CaFe}(\text{CO}_3)_2$ , FOR COPPER RADIATION

$h_1k_1l_1$	$\text{MgCO}_3$	$\text{Mg}_2\text{Ca}(\text{CO}_3)_4$	$\text{CaMg}(\text{CO}_3)_2$	$\text{CaCO}_3$	$\text{CaMn}(\text{CO}_3)_2$	$\text{CaFe}(\text{CO}_3)_2$	$\text{MnCO}_3$	$\text{FeCO}_3$	$\text{CoCO}_3$	$\text{NiCO}_3$	$\text{CuCO}_3$	$\text{ZnCO}_3$	$\text{CdMg}(\text{CO}_3)_2$	$\text{CdCO}_3$
111			.021		(14.2)†	(16.4)†								67.6
100			2.46		(9.17)	(12.7)								141
110			3.38	17.3	42.1	48.1	75.4	90.1	105	122	136	154		565
211	6.89	4.05 111*	196 200	213	231	246	246	243	231	249	323	296		779
222	9.73	17.9 111	6.65 4.96	7.20	1.59 1.15	1.85	.145	.0020	.0864	.346	.712	1.27		28.0
221			7.20		(.039)	(.0052)								68.0
101	5.17	22.7 202	17.0	30.2	40.2	41.3	50.7	52.7	58.1	61.8	82.3	80.3		267
210	39.4		34.9	44.6	43.4	42.5	41.6	40.4	39.4	38.6	41.2	39.5		97.7
111			6.07		(.465)	(.229)								45.2
200	10.3	18.3 311	20.2	33.2	40.8	41.6	48.0	48.9	52.5	54.3	71.8	69.2		20.5
220			.260		(1.64)	(2.02)								73.2
220	4.29	6.88 222	6.48	14.6	1.97	20.9	25.1	26.9	29.5	32.0	40.0	41.2		37.3
332	14.7	36.3 220	26.8	45.9	48.2	48.0	49.3	48.5	48.3	48.7	66.7	62.7		70.3
321	18.9	35.8 311	28.6	48.4	59.6	61.5	69.5	72.8	76.7	80.5	101	102		181
333			1.86		(.360)	(.247)								275
311			.273		(3.64)	(4.09)								10.4
201	4.09		6.95	8.98	7.78	6.72	5.88	5.06	4.38	3.71	6.11	4.33		23.7
211	6.24	6.94 313	14.9	21.4	28.6	28.9	33.0	33.2	35.9	37.3	52.6	49.9		57.9
331			0.16		(1.65)	(1.92)								6.21
433			.324		3.93	4.40	5.69	6.64	7.29	8.29	10.7	11.7		11.7
310	5.17	8.46 311	7.82	2.15	3.93	4.40	21.9	25.9	28.6	31.1	38.6	40.3		41.4
422	1.76	7.34 402	8.46	13.6	18.7	19.8	8.50	10.6	11.4	12.4	16.1	16.6		121
422	3.62	400	4.00	6.20	8.14	8.50	9.89	10.6	11.4	12.4	16.1	16.6		56.1
432	5.85		5.05	7.92	6.71	7.05	6.42	6.17	5.73	5.52	6.18	5.81		19.1
320	2.50		4.78	5.74	4.61	4.23	3.63	2.91	2.65	2.24	3.70	2.63		4.90
112	11.2	7.81 422	10.4	17.7	21.5	22.2	25.1	26.4	28.4	30.0	34.6	35.7		30.6
443			.0534		(1.26)	(1.42)								4.02
300			.455		(.970)	(1.14)								12.3
221														12.4
444	4.18	10.7 222	5.77	10.1	9.95	9.93	9.62	9.53	9.17	9.22	12.0	11.5		30.1

\* The calcite rhombohedral cell, on the basis of which the intensities in this table are computed, contains only  $\frac{1}{2}\text{MgCa}(\text{CO}_3)_2$  and is thus a pseudo-cell for huntite. The huntite reflections listed here may be indexed on this pseudo-cell; the corresponding index in the true huntite rhombohedral cell is given immediately after each huntite relative intensity value (see Graf and Bradley, in press).

† The intensities in parentheses were computed for a dolomite-type structure, the other  $\text{CaMn}(\text{CO}_3)_2$  and  $\text{CaFe}(\text{CO}_3)_2$  intensities, for a calcite-type structure (see text).

TABLE 5. VALUES OF  $2\theta$  FOR LOW-ANGLE X-RAY REFLECTIONS OF THE COMMON RHOMBOHEDRAL CARBONATES, COMPUTED FOR  $\text{CuK}\alpha_1$  RADIATION

$hk \cdot l$	$h_r k_r l_r$	$\text{MgCO}_3$	$\text{CaMg}(\text{CO}_3)_2$	$\text{CaCO}_3$ (26° C.)	$\text{FeCO}_3$	$\text{MnCO}_3$	$\text{ZnCO}_3$
00.3	111		16.597				
10.1	100		22.039				
01.2	110	25.143	24.071	23.051	24.777	24.310	25.056
10.4	211	32.637	30.964	29.394	32.038	31.428	32.561
00.6	222	35.850	33.557	31.427	34.989	34.319	35.827
01.5	221		35.331				
11.0	10 $\bar{1}$	38.841	37.376	35.965	38.363	37.625	38.670
11.3	210	42.985	41.148	39.402	42.362	41.539	42.822
02.1	11 $\bar{1}$		43.812				
20.2	200	46.832	44.950	43.152	46.208	45.302	46.633
10.7	322		45.193				
02.4	220	51.614	49.295	47.107	50.815	49.812	51.424
01.8	332	53.877	50.560	47.494	52.650	51.597	53.806
11.6	321	53.884	51.096	48.496	52.889	51.835	53.733
00.9	333		51.315				
20.5	311		52.374				
21.1	20 $\bar{1}$	61.395	58.918	56.555	60.581	59.346	61.108
12.2	21 $\bar{1}$	62.417	59.841	57.391	61.567	60.309	62.135
02.7	331		60.039				
10.10	433	66.420	62.056	58.063	64.789	63.448	66.340
21.4	310	66.431	63.459	60.660	65.423	64.065	66.149
20.8	422	68.386	64.533	60.983	66.996	65.595	68.204
11.9	432	69.354	65.182	61.359	67.828	66.405	69.210
12.5	320	69.360	66.097	63.042	68.239	66.806	69.081
03.0	11 $\bar{2}$	70.329	67.419	64.654	69.372	67.911	69.981
01.11	443		68.199				
{30.3	300}		69.981				
{03.3	22 $\bar{1}$ }		69.981				
00.12	444	75.986	70.523	65.595	73.917	72.327	75.928

Table 6 also gives the  $a_0$  and  $c_0$  values obtained from  $\cos^2 \theta$  and

$$\left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right)$$

extrapolations for various samples of  $\text{MgCO}_3$ ,  $\text{FeCO}_3$ ,  $\text{MnCO}_3$ ,  $\text{CoCO}_3$ ,  $\text{CdCO}_3$ ,  $\text{NiCO}_3$ ,  $\text{ZnCO}_3$ , and  $\text{CaMn}(\text{CO}_3)_2$ , together with measurements of  $\text{CdMg}(\text{CO}_3)_2$  samples made on films taken with a Guinier-type focusing camera. The comparable information for  $\text{CaCO}_3$  and  $\text{CaMg}(\text{CO}_3)_2$  has been given in Goldsmith and Graf (1958*b*), together with a discussion of the extrapolation procedure, which involves successive approximations.

In making spacing measurements, film shrinkage and camera radius

TABLE 6. METHOD OF PREPARATION, PURITY, AND CELL CONSTANTS OF VARIOUS RHOMBOHEDRAL CARBONATE SAMPLES

MgCO<sub>3</sub>, No. G-1219; basic Mg carbonate+CO<sub>2</sub>+H<sub>2</sub>O, 15 hours in Morey bomb at 300° C.; 0.38±0.06% CaCO<sub>3</sub>, 0.01±0.003% FeCO<sub>3</sub>, <0.003% MnCO<sub>3</sub>, <0.04% CdCO<sub>3</sub>, <0.007% CoCO<sub>3</sub>, <0.25% ZnCO<sub>3</sub>.

$$a_0 = 4.6330 \text{ \AA}, \text{ Cu radiation}$$

$$c_0 = 15.016 \text{ \AA} \text{ (Goldsmith and Graf, 1958b)}$$

$$c_0/a_0 = 3.2411$$

MnCO<sub>3</sub>, reagent grade chemical; 0.1±0.03% CaCO<sub>3</sub>, 0.02±0.01% CdCO<sub>3</sub>, <0.02% CoCO<sub>3</sub>, <0.01% FeCO<sub>3</sub>, 0.1±0.05% MgCO<sub>3</sub>, <0.2% ZnCO<sub>3</sub>. H<sub>2</sub>O (-110° C.), 0.85%\*; H<sub>2</sub>O (+110° C.), 3.32%\*.

$$a_0 = 4.792 \text{ \AA}, \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right) \text{ extrapolation, Fe radiation}$$

$$c_0 = 15.71 \text{ \AA}, \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right) \text{ extrapolation, Fe radiation}$$

$$c_0/a_0 = 3.278$$

MnCO<sub>3</sub>, No. G-738; reagent grade MnCO<sub>3</sub>+CO<sub>2</sub>, 3 hours at 722° C. in cold-seal bomb; 0.09±0.02% CaCO<sub>3</sub>, 0.1±0.05% MgCO<sub>3</sub>, 0.01±0.008% FeCO<sub>3</sub>, <0.02% CdCO<sub>3</sub>, <0.02% CoCO<sub>3</sub>, <0.2% ZnCO<sub>3</sub>.

$$a_0 = 4.7771 \text{ \AA}, \text{ Fe radiation}$$

$$a_0 = 4.7772 \text{ \AA}, \text{ Cu radiation}$$

$$c_0 = 15.664 \text{ \AA}, \text{ Fe radiation}$$

$$c_0/a_0 = 3.2790$$

FeCO<sub>3</sub>, No. G-613; FeSO<sub>4</sub>+Na<sub>2</sub>CO<sub>3</sub>+CO<sub>2</sub>+H<sub>2</sub>O, 20 hours at 143° C. in Morey bomb;

$$a_0 = 4.690_2 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 15.369 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.276_8$$

FeCO<sub>3</sub>, No. G-1219; FeSO<sub>4</sub>+Na<sub>2</sub>CO<sub>3</sub>+CO<sub>2</sub>+H<sub>2</sub>O, 15 hours at 300° C. in Morey bomb; 0.038±0.020% CaCO<sub>3</sub>, 0.072±0.014% MgCO<sub>3</sub>, 0.13±0.013% MnCO<sub>3</sub>, <0.08% CdCO<sub>3</sub>, 0.008±0.002% CoCO<sub>3</sub>, 0.18±0.04% ZnCO<sub>3</sub>.

$$a_0 = 4.6887 \text{ \AA}, \text{ Co radiation}$$

$$a_0 = 4.6888 \text{ \AA}, \text{ Fe radiation}$$

$$c_0 = 15.373 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.2787$$

FeCO<sub>3</sub>, material from No. G-1219+NaHCO<sub>3</sub>, 3 hours in squeezer-type apparatus (Griggs and Kennedy, 1956), 14 kb, 659° C.

$$a_0 = 4.6889 \text{ \AA}, \text{ Fe radiation}$$

$$c_0 = 15.373 \text{ \AA}, \text{ Fe radiation}$$

$$c_0/a_0 = 3.2786$$

CdCO<sub>3</sub>, reagent grade chemical; <0.09% CaCO<sub>3</sub>, <0.06% CoCO<sub>3</sub>, 0.01<sub>2</sub>±0.009% FeCO<sub>3</sub>,

Unless otherwise noted, impurities reported in spectrographic analyses by Juanita Witters as weight per cent metal have been recalculated to mol per cent carbonate. Cell constants were obtained by cos<sup>2</sup>θ extrapolations unless otherwise noted. The ranges given for a<sub>0</sub> and c<sub>0</sub> of ordered and disordered CdMg(CO<sub>3</sub>)<sub>2</sub> indicate only the uncertainty that would result from a misreading of line position on the films by the smallest unit measured, 0.05 mm.

\* Analyst, L. D. McVicker.



TABLE 6—(continued)

0.03<sub>8</sub>±0.02<sub>5</sub>% MgCO<sub>3</sub>, 0.06±0.03% MnCO<sub>3</sub>, <0.08% ZnCO<sub>3</sub>, H<sub>2</sub>O (−110° C.), 0.23%\*; H<sub>2</sub>O (+110° C.), 2.87%\*.

$$a_0 = 4.936 \text{ \AA}, \quad \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right) \text{ extrapolation, Fe radiation}$$

$$c_0 = 16.29 \text{ \AA}, \quad \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right) \text{ extrapolation, Fe radiation}$$

$$c_0/a_0 = 3.300$$

CdCO<sub>3</sub>, No. G-1321; CdSO<sub>4</sub>+Na<sub>2</sub>CO<sub>3</sub>+CO<sub>2</sub>+H<sub>2</sub>O, 15 hours at 255° C. in Morey bomb; 0.09±0.07% CaCO<sub>3</sub>, <0.01<sub>8</sub>% MgCO<sub>3</sub>, 0.009±0.007% FeCO<sub>3</sub>, 0.003±0.002<sub>8</sub>% MnCO<sub>3</sub>, <0.06% CoCO<sub>3</sub>, <0.08% ZnCO<sub>3</sub>.

$$a_0 = 4.9207 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 16.295 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.3115$$

CdCO<sub>3</sub>, material from No. G-1321 plus Li<sub>2</sub>CO<sub>3</sub> in squeezer-type apparatus for 3 hours at 10 kb, 500° C.

$$a_0 = 4.9204 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 16.298 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.3123$$

ZnCO<sub>3</sub>, No. G-1316; reagent grade chemical +H<sub>2</sub>O+CO<sub>2</sub>, 15 hours at 250° C. in Morey bomb; 0.19±0.04% CaCO<sub>3</sub>, 0.01±0.008% MgCO<sub>3</sub>, 0.040±0.020% FeCO<sub>3</sub>, 0.002±0.001<sub>5</sub>% MnCO<sub>3</sub>, <0.02% CdCO<sub>3</sub>, <0.02% CoCO<sub>3</sub>; H<sub>2</sub>O (−110° C.), 0.54%†; H<sub>2</sub>O (+110° C.), 3.73%†.

$$a_0 = 4.6528 \text{ \AA}, \text{ Cu radiation}$$

$$a_0 = 4.6525 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 15.025 \text{ \AA}, \text{ Cu radiation}$$

$$c_0 = 15.024 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.2292$$

ZnCO<sub>3</sub>, transparent crystal from Broken Hill, Rhodesia; 0.03±0.01<sub>5</sub>% CaCO<sub>3</sub>, 0.92±0.09% FeCO<sub>3</sub>, 0.30±0.03% MgCO<sub>3</sub>, 0.041±0.004% MnCO<sub>3</sub>, <0.02% CdCO<sub>3</sub>, <0.04% CoCO<sub>3</sub>, <0.004% NiCO<sub>3</sub>.

$$a_0 = 4.6534 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 15.027 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.2293$$

NiCO<sub>3</sub> (prepared by Thelma Isaacs), NiCl<sub>2</sub>·6H<sub>2</sub>O+NaHCO<sub>3</sub>+H<sub>2</sub>O+CO<sub>2</sub>, 2.5 months at 250° C. in Morey bomb; 0.06±0.03% CaCO<sub>3</sub>, 0.04±0.02% FeCO<sub>3</sub>, 0.01<sub>5</sub>±0.008% MgCO<sub>3</sub>, 0.04±0.02% MnCO<sub>3</sub>, 0.09±0.05% ZnCO<sub>3</sub>, 0.02 wt % Cu, 0.2 wt % Na, 0.02 wt % Si. Infrared absorption curve shows no water in excess of that for the KBr blank.

$$a_0 = 4.5975 \text{ \AA}, \text{ Co radiation}$$

$$c_0 = 14.723 \text{ \AA}, \text{ Co radiation}$$

$$c_0/a_0 = 3.2024$$

25° C.

CoCO<sub>3</sub>, No. G-1319; "Specpure" Co<sub>3</sub>O<sub>4</sub>+KHSO<sub>4</sub>→Co sulfate; Co sulfate+"Spec-

25° C.

pure" Na<sub>2</sub>CO<sub>3</sub>→basic Co carbonate; basic Co carbonate+H<sub>2</sub>O+CO<sub>2</sub> for 15 hours at 255° C. in Morey bomb; <0.1<sub>5</sub>% CaCO<sub>3</sub>, 0.04±0.03<sub>5</sub>% MgCO<sub>3</sub>, 0.01

† Microanalyst, D. R. Dickerson.

TABLE 6—(continued)

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$\pm 0.008\%$ FeCO <sub>3</sub> , $< 0.004\%$ MnCO <sub>3</sub> , $< 0.1\%$ CdCO <sub>3</sub> , $< 0.002\%$ NiCO <sub>3</sub> , $< 0.09\%$ ZnCO <sub>3</sub> . H <sub>2</sub> O ( $-110^\circ$ C.), none†; H <sub>2</sub> O ( $+110^\circ$ C.), 8.10%†.	
$a_0 = 4.6620 \text{ \AA}$ , Co radiation	
$c_0 = 14.975 \text{ \AA}$ , Co radiation	
$c_0/a_0 = 3.2121$	
CoCO <sub>3</sub> , material from No. G-1319+Li <sub>2</sub> CO <sub>3</sub> , 2 hours in squeezer-type apparatus at 10 kb., 60° C.	
$a_0 = 4.6581 \text{ \AA}$ , Co radiation	
$c_0 = 14.958 \text{ \AA}$ , Co radiation	
$c_0/a_0 = 3.2112$	
CdMg(CO <sub>3</sub> ) <sub>2</sub> , ordered; Li <sub>2</sub> CO <sub>3</sub> added to equimolar mixture of CdCO <sub>3</sub> and MgCO <sub>3</sub> , treated in cold-seal bomb for 23 hours under 27,000 psi CO <sub>2</sub> at 600° C.	
$d_{\{444\}}$ and $d_{\{11\bar{2}\}}$ measured on film taken with FeK $\alpha_1$ radiation, using a Guinier-type focusing camera, and calibrated against the closely similar $d_{\{444\}}$ and $d_{\{11\bar{2}\}}$ values of synthetic MnCO <sub>3</sub> run on the adjoining strip of the same film.	
$a_0 = 4.7770 \pm 0.0009 \text{ \AA}$	
$c_0 = 15.641 \pm 0.003 \text{ \AA}$	
$c_0/a_0 = 3.2742$	
CdMg(CO <sub>3</sub> ) <sub>2</sub> , disordered; equimolar mixture of CdCO <sub>3</sub> and MgCO <sub>3</sub> treated at 10 kb. and 900° C. for 1.5 hours in sealed-tube gas system; spacing measurements made as for the ordered material.	
$a_0 = 4.7746 \pm 0.0009 \text{ \AA}$	
$c_0 = 15.678 \pm 0.003 \text{ \AA}$	
$c_0/a_0 = 3.2836$	
CaMn(CO <sub>3</sub> ) <sub>2</sub> , disordered; equimolar mixture of CaCO <sub>3</sub> and MnCO <sub>3</sub> reacted in cold-seal bomb at 706–710° C. under 14,000 psi CO <sub>2</sub> pressure for 22 hours.	
Line coincidence of $\{400\}$ and $\{644\}$ used to obtain accurate $c_0/a_0$ ratio, followed by $a_0$ and $c_0$ extrapolations of back reflections on film taken with Fe radiation. $I_{\{400\}}:I_{\{644\}}$ is computed to be about 3, and observed as such on films of CaMn carbonate solid solutions containing 40 and 60 mol per cent MnCO <sub>3</sub> , for which the two reflections are resolved. Departure from coincidence in the CaMn(CO <sub>3</sub> ) <sub>2</sub> sample would thus readily be observable as line broadening relative to the line breadths of neighboring reflections.	
$a_0 = 4.8797 \text{ \AA}$	
$c_0 = 16.367 \text{ \AA}$	
$c_0/a_0 = 3.3541$	

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errors were taken into account by using the Straumanis film mount and correction procedure. Reflections in the range  $\theta = 60^\circ - 90^\circ$  were used for the  $\cos^2 \theta$  extrapolations, in accordance with the finding of Taylor and Sinclair (1945) that almost linear extrapolation curves which simultaneously eliminate eccentricity and absorption errors are obtained within this angular range.

#### COMPARISON OF CELL CONSTANTS WITH PUBLISHED VALUES

Cell constants cited in this paper are compared in Table 7 with values obtained from the literature. For most of the carbonates, the agreement

is excellent. The newly determined values for coarsely crystalline synthetic  $\text{NiCO}_3$  are preferred over those of Pistorius (1959), and there is a small discrepancy for  $\text{CdCO}_3$ .

The range of  $a_0$  values reported in Table 7 for several  $\text{CdCO}_3$  samples, 4.9204 to 4.936 Å, includes the values published by Swanson *et al.* (1957) and Ramdohr and Strunz (1941), but the range of  $c_0$  values, 16.298 to 16.29 Å, is clearly distinct from their 16.27 Å. Mr. Swanson (personal communication) finds  $a_0 = 4.9279$  Å and  $c_0 = 16.284$  Å on repeating the least squares calculation for his  $\text{CdCO}_3$  sample.

The several sets of  $\text{CdCO}_3$  values in Tables 6 and 7 suggest that  $a_0$  increases and  $c_0$  decreases with decreasing temperature of formation, although some of these differences are near the limit of error, and that Swanson's sample was made at fairly low temperature.

#### ENLARGED UNIT CELLS OF LOWER TEMPERATURE PREPARATIONS

Effects analogous to the change in cell size of  $\text{CdCO}_3$  prepared at lower temperatures are noted for other carbonates (Table 6). There is a considerable increase in both  $a_0$  and  $c_0$  of  $\text{CoCO}_3$  prepared at 255° C., compared with that made at 600° C. Reagent-grade chemical  $\text{MnCO}_3$  as received has a markedly enlarged cell compared with that of material crystallized at 722° C. Saint Léon Langlès (1952) reported values for two  $\text{NiCO}_3$  preparations that indicate the higher temperature product has a smaller cell. Graf *et al.* (1961) have described a magnesite from the Lake Bonneville sediments of Quaternary age in the Great Salt Lake Desert, Utah, which has  $a_0 = 4.669$  Å,  $c_0 = 15.21$  Å, compared with  $a_0 = 4.6330$  Å and  $c_0 = 15.016$  Å given in Table 7 for material prepared at 250° C. The impurity content which could conceivably be in solid solution in the magnesite of the Utah sample, 0.7 wt% Fe, 0.01 wt% Mn, and about 0.2 wt% Ca (spectrographic analysis by Juanita Witters), fails by an order of magnitude to explain the change in cell size.

Calculations by Verwey (1946) for several alkali halides, which should be similar enough to the rhombohedral carbonates for order-of-magnitude comparison, indicated that near-surface shifts of position of positive and negative ions and their electron clouds should occur, but only for one or two atomic layers below the surface. The effect would thus be insignificant for particles of the order of 1 micron diameter such as those making up the lowest-temperature carbonate preparations. Rymer's recent (1957) review indicates extensive disagreement as to the size and magnitude of the effect of small particle-size *per se* on cell constants.

Lehovec (1953) computed that the space-charge zone in NaCl particles, which causes an electrostatic potential between the bulk and the surface of the crystal and affects the concentration of point defects, should extend inward from the surface about 0.013 micron at 627° C.,

TABLE 7. COMPARISON WITH PUBLISHED VALUES OF CELL CONSTANTS

Material	$c_0$ in Å	$a_0$ in Å	Reference	Remarks
CaCO <sub>3</sub>	17.064	4.9900, 4.9896	Goldsmith and Graf (1958 <i>b</i> ) See discussion in Graf and Lamar (1955) Andrews (1950)	Extrapolated values; spectrographic standard CaCO <sub>3</sub> Calculated from spectrometer measurements of $\alpha$ and $d_{\{211\}}$ of single crystals Spectrographic standard CaCO <sub>3</sub>  Andrews' values recalculated to 26° C. using thermal expansion data of Austin <i>et al.</i> (1940) 0.01–0.1% Sr is major residual impurity after purification  Sample heated four days at 120,000 psi and 280° C.; 0.01–0.1% Ca  Ppt. from solutions of MnSO <sub>4</sub> and NaHCO <sub>3</sub> , heated in CO <sub>2</sub> atmosphere 3 days at 400° C. Recrystallized at 722° C. (see Table 6)  NaHCO <sub>3</sub> and FeSO <sub>4</sub> ·7H <sub>2</sub> O reacted at 200° C. under 500 bars (CO <sub>2</sub> +H <sub>2</sub> O) pressure, then held at 600° C. under 15 lb. pressure in squeezer apparatus of Griggs and Kennedy (1956); least squares treatment of diffractometer data Prepared at 300° C. (see Table 6)
	17.064 (26° C.)	4.9899 (26° C.)		
	17.060 ± 0.005 (18° C.)	4.9898 ± 0.0003 (18° C.)		
	17.063 <sub>b</sub> (26° C.)	4.9896 (26° C.)		
	17.062 (26° C.)	4.989 (26° C.)		
MgCO <sub>3</sub>	15.016	4.6330	Swanson and Fuyat (1953)	
	15.015	4.6332	Goldsmith and Graf (1958 <i>b</i> ) Swanson <i>et al.</i> (1957)	
MnCO <sub>3</sub>	15.664	4.7768	Goldsmith and Graf (1957)	
	15.67	4.777	Swanson <i>et al.</i> (1957)	
	15.664	4.7771	This paper	
FeCO <sub>3</sub>	15.370 ± 0.003	4.690 ± 0.002	Sharp (1960)	
	15.373	4.6887	This paper	

Material	$c_0$ in Å	$a_2$ in Å	Reference	Remarks
ZnCO <sub>3</sub>	15.028 (25° C.)	4.6533 (25° C.)	Swanson <i>et al.</i> (1959)	U.S.N.M.#96155, Broken Hill, Rhodesia; 0.01–0.1% of Cd, Fe, Mg, and Pb; 0.001–0.01% of Ca, Mn, and Si; 0.0001–0.001% Cu. Small transparent smithsonite crystals from Broken Hill, Rhodesia, supplied by C. S. Hurlbut, Jr. (see Hurlbut, 1954); spectrographic analysis calculates to 0.92 mol per cent FeCO <sub>3</sub> , 0.30 mol per cent MgCO <sub>3</sub> content
	15.027	4.6534	This paper	
	15.024	4.6531	This paper	
NiCO <sub>3</sub>	15.025	4.6528	This paper	Previous entry corrected for FeCO <sub>3</sub> and MgCO <sub>3</sub> , assuming straight-line relation between cell constants and composition in systems ZnCO <sub>3</sub> -FeCO <sub>3</sub> and ZnCO <sub>3</sub> -MgCO <sub>3</sub> . Recrystallized at 250° C. (see Table 6)
	14.744 ± 0.003 (25° C.)	4.602 ± 0.001 (25° C.)	Pistorius (1959)	
	14.723	4.5975	This paper	
CdCO <sub>3</sub>	16.27	4.92	Ramdohr and Strunz (1941)	Schering's (chemical) CdCO <sub>3</sub> ; kX values here converted to Å. Fine-grained material; 0.001–0.01% of Cr, Ni, and Pb; 0.0001–0.001% of Ca, Cu, Fe, Mg, and Si. Recrystallized at 500° C. (see Table 6)
	16.27	4.930	Swanson <i>et al.</i> (1957)	
	16.298	4.9204	This paper	
CoCO <sub>3</sub>	14.957	4.659	Swanson <i>et al.</i> (1960)	CoCl <sub>2</sub> ·6H <sub>2</sub> O, NaHCO <sub>3</sub> , and H <sub>2</sub> CO <sub>3</sub> reacted in Morey bomb; 0.01–0.1% of Mo, Ni; 0.001–0.01% of Ba, Cu, Mg, Si, and Ag. Recrystallized at 600° C. (see Table 6)
	14.958	4.6581	This paper	

0.22 micron at 327° C. However, the vacancy concentrations observed in the alkali halides even at high temperature hardly seem adequate to explain the larger of the cell-size anomalies described in this paper.

Some of the samples prepared at lower temperatures include several percent of H<sub>2</sub>O or OH<sup>-</sup> that is not released in 12 to 15 hours at 110° C. (Table 6). The remarkably high value reported for CoCO<sub>3</sub> is from a microanalysis that totals poorly and may be in error, but there is no reason to doubt the results given for ZnCO<sub>3</sub>, CdCO<sub>3</sub>, and MnCO<sub>3</sub>. The structural location of this H<sub>2</sub>O or OH<sup>-</sup> (it may, of course, only be tightly adsorbed) and its possible effect upon cell constants will be discussed in a subsequent communication.

It is possible that some of the cell enlargement of dolomite in fine-grained precipitates formed at room temperature, hitherto attributed exclusively to excess calcium (Graf and Goldsmith, 1956; Goldsmith and Graf, 1958*a*), may actually result from structurally incorporated H<sub>2</sub>O or OH<sup>-</sup>. Such a hydration effect is, of course, ruled out for other dolomites with enlarged cells which were formed by high-temperature synthesis in an anhydrous system.

#### THE UNIT CELL OF HUNTITE, Mg<sub>3</sub>Ca(CO<sub>3</sub>)<sub>4</sub>

Graf and Bradley (In press) gave for the unit cell of huntite  $a_0 = 9.505$  Å,  $c_0 = 7.821$  Å, obtained from a powder diffraction film of huntite from Currant Creek, Nevada, by making a least squares analysis involving a drift error term of the form

$$\sin^2 \theta \left( \frac{1}{\sin \theta} - \frac{1}{\theta} \right).$$

Their cell was of principal value in demonstrating the close agreement between observed and calculated d-spacings of front reflections. A more accurate  $a_0$  value can be obtained by combining the  $c/a$  ratio obtained from the least squares analysis with measurements on a film taken with iron radiation of the positions of the {71·3} and {72·2} reflections, at  $2\theta \cong 149^\circ$  and  $168^\circ$ , respectively, to make a two-point  $\cos^2 \theta$  extrapolation. Then  $c_0$  is calculated from  $d_{(100 \cdot 6)}$ , the latter first corrected by the amount that the measured spacing of the adjacent {25·0} reflection differs from the value calculated from  $a_0$ . Varying the  $c/a$  ratio by an amount corresponding to  $a_0$  fixed at 9.4980 Å and  $c_0$  changing from 7.81 to 7.82 Å changes the extrapolated  $a_0$  value by only  $\pm 0.0003$  Å.

Measurements for three huntite samples, all very fine-grained naturally-occurring materials, are given in Table 8. The cell constants of the two samples from Currant Creek, Nevada, are identical within the general limits of error observed in such extrapolations for the other

rhombohedral carbonates. The sample from Tea Tree Gully has a significantly larger cell. Graf and Bradley estimated that the  $a_0$  of the Currant Creek huntite was 0.61% greater than predicted from a straight-line interpolation between the values for magnesite and calcite;  $c_0$ , 0.75% larger. The corresponding values for the more accurately determined unit cells in Table 8 are  $a_0$ , 0.57–0.61%,  $c_0$  0.66–0.70%.

Coarsely crystalline huntite will have to be found in nature or synthesized before it will be possible to attribute a particular cell size to

TABLE 8. UNIT CELL DIMENSIONS OF THE HEXAGONAL STRUCTURE CELL OF HUNTITE

Sample	$a_0$ by extra- polation	$c_0$		
		Using $a_0$ and the $c/a$ ratio of the least squares analysis	From $d_{\{00\cdot6\}}$ corrected against $d_{\{25\cdot0\}}$	
			Diffractometer	Film
Currant Creek, Nevada (Collected by D. L. Graf)	9.4981	7.815 <sub>5</sub>	7.815 <sub>8</sub>	
Currant Creek, Nevada (Collected by G. T. Faust)	9.4979	7.815 <sub>5</sub>		7.815 <sub>0</sub>
Tea Tree Gully, South Australia	9.5020	7.818 <sub>7</sub>		7.818 <sub>5</sub>

material of strictly 3:1 molar  $\text{MgCO}_3$ : $\text{CaCO}_3$  composition, free of hydration effects.

#### EFFECT OF CATION ORDER ON CELL SIZE

Small but measurable changes in cell size take place with cation disordering of the 1:1 compounds. Comparison of  $a_0$  and  $c_0$  values for the ordered and disordered cells with those predicted by taking  $a_0$  and  $c_0$  values midway between those of the two end members is interesting. Thus far, the only composition for which all three sets of values are available is  $\text{CdMg}(\text{CO}_3)_2$  (Goldsmith, 1958). The crystallinity of these preparations is not ideal, and back reflection measurements are therefore not of the highest quality. The most accurate data available are those obtained from films taken with a Guinier-type focusing camera. The change in  $a_0$  on disordering is  $-0.0024 \text{ \AA}$ , that in  $c_0$ ,  $+0.037 \text{ \AA}$  (Table 1). One might suspect that these slight differences resulted from a sampling or mixing error—it need involve only about 0.2 mol percent  $\text{CdCO}_3$ —were it not for the fact that the two axial lengths change in

opposite directions and that comparable effects, discussed below, are observed for dolomite. Actually, Goldsmith's mixing was achieved by prolonged hand mulling of small portions under alcohol, a method that leaves little reason to distrust the stated compositions.

The  $a_0$  and  $c_0$  cited for dolomite in Table 1 and used in computations elsewhere in this paper, 4.8079 and 16.010 Å, respectively, are those derived by Goldsmith and Graf (1958*b*) from study of several analyzed single-crystal dolomite samples. Goldsmith and Graf have discussed the relations between these values and those derived by averages of the  $a_0$  values and of the  $c_0$  values for calcite and magnesite. These averages also are included in Table 1.

The most probable  $\Delta a_0$  and  $\Delta c_0$  values for largely but not completely disordered materials having essentially the composition  $\text{CaMg}(\text{CO}_3)_2$  are respectively,  $-0.003$  Å and  $+0.03_5$  Å (Goldsmith *et al.*, 1961). Most of the measurements were made on films taken with a Guinier-type focusing camera; the uncertainty in  $\Delta a_0$  resulting from a possible Guinier measurement error on each pattern of the smallest unit recorded, 0.05 mm, is  $\pm 0.0018$  Å, and in  $c_0$  is  $\pm 0.006$  Å.

The agreement among  $\Delta a_0$  and  $\Delta c_0$  values for the various  $\text{CaMg}(\text{CO}_3)_2$  and  $\text{CdMg}(\text{CO}_3)_2$  samples is good, in view of the difficulty in making accurate measurements on imperfectly crystallized materials and the fact that neither the compositions of the several dolomite samples nor the amounts of residual order remaining in them after quenching from temperatures near 1125° C. are precisely the same. Any variation that may exist in  $\Delta a_0$  and  $\Delta c_0$  with slight departures from equimolar composition is masked by the experimental uncertainty.

No 1:1 ordered calcium iron carbonate has yet been described, but  $a_0$  and  $c_0$  values predicted from those for  $\text{FeCO}_3$  and  $\text{CaCO}_3$  are presented in Table 1 because of their possible usefulness in studies of ferroan dolomite. The ordered compound  $\text{CaMn}(\text{CO}_3)_2$ , kutnahorite, is present in nature in well crystallized specimens, but none of the single-phase samples yet studied is sufficiently free of Mg and Fe in solid solution to permit precise comparison with predicted values. Order reflections for this composition can be detected with certainty only in single-crystal  $x$ -ray diagrams, so that it has not proved possible to determine whether ordered synthetic powders have been prepared. However, at a sufficiently high temperature, by analogy with single-crystal experiments (Goldsmith and Graf, unpublished data), one can be certain that such a powder is disordered, and values are given in Table 1 for a sample of this kind.

#### RELIABILITY OF CELL CONSTANTS

The extrapolated cell constants presented here and by Goldsmith and Graf (1958*b*) for materials recrystallized at high temperatures appear to



differ from comparable published data, and also among themselves where measurements of the same constant were made with several radiations, by from 0.0001 to 0.0003 Å in  $a_0$  and by 0.001 or 0.001<sub>5</sub> Å in  $c_0$ , or from 2.5 to 10 parts per 100,000. The maximum uncertainty in the temperature for which cell constants are valid is  $26 \pm 3^\circ$  C., the range of temperature encountered in the laboratory where the films were taken, which is air-conditioned in summer. The correction for these materials for a temperature difference of  $5^\circ$  C., based upon available thermal expansion data, would be about 0.0001 Å in  $a_0$  and about 0.002 Å in  $c_0$ , values comparable with the differences mentioned above.

The cell constants presented here should be satisfactory for most geochemical and mineralogical purposes, but they may not be adequate for some studies of defects in these solids. The extent to which they can be further refined appears to be limited by poor crystallinity for materials formed at moderate temperatures. Less than perfect cation ordering in 1:1 compounds such as dolomite appears, in principle, to be present in greater or lesser amount at all temperatures (Goldsmith and Graf, 1958*b*), and places a further limit on the accuracy with which cell constants can be obtained for these materials.

#### INTERPLANAR SPACINGS

The  $a_0$  and  $c_0$  values selected for use in calculating  $d$ -values, typically those for well crystallized high-temperature materials giving the most accurate  $\cos^2 \theta$  extrapolations, are given in Table 1 together with  $a_{rh}$  and  $\alpha$  values for the rhombohedral cells.

Table 2 includes all possible reflections of the carbonates listed there using  $\text{CuK}\alpha_1$  radiation. A list of such reflections was first prepared for a hypothetical dolomite-type structure having the  $a_0$  and  $c_0$  of  $\text{CaCO}_3$ . Deletions from this list were then made of reflections forbidden for calcite-type structures, and of reflections with  $d < 0.77025$  for the carbonates with smaller cells. The spacings listed for  $\text{CaCO}_3$  by Andrews (1950) and Swanson and Fuyat (1953), for  $\text{CaMg}(\text{CO}_3)_2$  by Howie and Broadhurst (1958), for  $\text{MnCO}_3$  by Goldsmith and Graf (1957) and Swanson *et al.* (1957), for  $\text{CdCO}_3$  and  $\text{MgCO}_3$  by Swanson *et al.* (1957), for  $\text{ZnCO}_3$  by Swanson *et al.* (1959) and for  $\text{CoCO}_3$  by Swanson *et al.* (1960) indicate which of the possible reflections for these compounds have sufficient intensity to be readily observed in routine diffraction analyses.

#### STRUCTURE FACTORS

Calcite belongs to space group  $R\bar{3}c$ , dolomite to  $R\bar{3}$ , and the huntite model proposed by Graf and Bradley (In press) to  $R32$ . The unit cells of these materials contain, respectively,  $2\text{CaCO}_3$ ,  $\text{Ca} > \text{Mg}(\text{CO}_3)_2$ , and  $\text{Mg}_3\text{Ca}(\text{CO}_3)_4$ . All  $\{h, k, l_r\}$  are possible reflections for dolomite and for

huntite, but for calcite reflections having  $h_r + k_r + l_r$  odd are forbidden unless  $h_r \neq k_r \neq l_r$ .

Structure factor computations like those which follow are simplified considerably by using the rhombohedral cell. The amplitude contributions to the calcite structure factors, obtained by substituting in the appropriate expression (International Tables for X-ray Crystallography, volume 1, 1952, p. 473) for each atom in the rhombohedral unit cell and summing, fall into three types that may be represented by greatly simplified expressions. The types are defined using sign changes of amplitude contributions from atoms whose coordinates do not involve variable parameters, and the zero or non-zero character of amplitude contributions in general. Further definitions involving variable parameters which are very nearly equal to simple fractions could be made, but would break down for higher order reflections. The letter-designated subdivisions are not distinct types, but will be useful in a comparison of calcite, dolomite, and huntite reflection types which follow.

The calcite types are:

1.  $(h_r + k_r + l_r)$  divisible by 4  
 $2f_{Ca} + 2sf_C + 2f_O [\cos 2\pi x(h-k) + \cos 2\pi x(k-l) + \cos 2\pi x(l-h)]$   
 (1a. Two or three indices alike)  
 (1b.  $h \neq k \neq l$ )
2.  $(h_r + k_r + l_r)$  even, but not divisible by 4  
 $2f_{Ca} - 2f_C - 2f_O [\cos 2\pi x(h-k) + \cos 2\pi x(k-l) + \cos 2\pi x(l-h)]$   
 (2a. Two or three indices alike)  
 (2b.  $h \neq k \neq l$ )
3.  $(h_r + k_r + l_r)$  odd,  $h \neq k \neq l$   
 $2f_O [\sin 2\pi x(h-k) + \sin 2\pi x(k-l) + \sin 2\pi x(l-h)]$ .

These expressions are analogous to those presented by Tahvonen (1947) for the isostructural  $\text{NaNO}_3$ , but with calcium rather than the anion at the origin. Like the amplitude contributions which follow for dolomite and huntite, those for calcite have been divided by an appropriate constant so that they refer to the contents of one unit cell.

From the expression for the dolomite space group, given on page 463 of volume 1 of the International Tables for X-ray Crystallography, with calcium at the origin, three simplified expressions for the various types of dolomite reflections may be obtained:

1.  $(h_r + k_r + l_r)$  even  
 $f_{Ca} + f_{Mg} + 2f_C [\cos 2\pi x(h+k+l)] \quad 2f_O [\cos 2\pi (hx+ky+lz) + \cos 2\pi (kx+ly+hz) + \cos 2\pi (lx+ly+kz)]$   
 (1a.  $(h_r + k_r + l_r)$  divisible by 4; 2 or 3 indices alike)  
 (1b.  $(h_r + k_r + l_r)$  divisible by 4;  $h \neq k \neq l$ )  
 (1c.  $(h_r + k_r + l_r)$  even but not divisible by 4; 2 or 3 indices alike)  
 (1d.  $(h_r + k_r + l_r)$  even but not divisible by 4;  $h \neq k \neq l$ )

2.  $(h_r+k_r+l_r)$  odd, two or three indices alike

$$f_{Ca}-f_{Mg}+2f_c[\cos 2\pi x(h+k+l)]+2f_0[\text{as in 1}]$$

3.  $(h_r+k_r+l_r)$  odd,  $h \neq k \neq l$

$$f_{Ca}-f_{Mg}+2f_c[\cos 2\pi x(h+k+l)]+2f_0[\cos 2\pi(hx+ky+lz)+\cos 2\pi(kx+ly+hz)+\cos 2\pi(lx+hy+kz)];$$

$$f_{Ca}-f_{Mg}+2f_c[\cos 2\pi x(h+k+l)]+2f_0[\cos 2\pi(kx+hy+lz)+\cos 2\pi(hx+ly+kz)+\cos 2\pi(lx+ky+hz)]$$

Dolomite reflections of type 2, a consequence of cation ordering, are forbidden in calcite. Those of dolomite type 3 are in calcite contributed to exclusively by oxygen.

From the expressions for the space group of the Graf-Bradley huntite model, given on page 466 of volume 1 of the International Tables for X-ray Crystallography, with calcium at the origin, the following four simplified expressions for the various types of reflections may be obtained. Lengthy trigonometric expressions which appear within the brackets have been omitted; those indicated by asterisks include both sines and cosines, the others, only cosines:

1.  $(h+k+l)$  even, 2 or 3 indices the same

$$f_{Ca}+f_{C_1}+1/3[ ]f_{C_{II}}+1/3[ ]f_{Mg}+1/3[ ]f_{O_I}+1/3[ ]f_{O_{II}}+2/3[ ]f_{O_{III}}$$

(a.  $h, k, l$  all even numbers)

(b. Only one even index)

2.  $(h+k+l)$  even,  $h \neq k \neq l$

$$\sqrt{A^2+B^2}, \text{ where}$$

$A$  = the expression given under 1

$$B = 1/3[*]f_{C_{II}}+1/3[*]f_{Mg}+1/3[*]f_{O_I}+1/3[*]f_{O_{II}}+2/3[*]f_{O_{III}}$$

(2a.  $h, k, l$  all even numbers)

(2b. Only one even index)

3.  $(h+k+l)$  odd, 2 or 3 indices the same

$$f_{Ca}-f_{C_1}+\dots \text{ remainder as in 1}$$

(3a.  $h, k, l$  all odd numbers)

(3b. Only one odd index)

4.  $(h+k+l)$  odd,  $h \neq k \neq l$

$$\sqrt{A^2+B^2}, \text{ where}$$

$A = f_{Ca}-f_{C_1}+\dots$  remainder as in 1

$B$  as in 2

(4a.  $h, k, l$  all odd numbers)

(4b. Only one odd index)

Table 9 gives correlations among the several groups of reflections which have been described for calcite, dolomite, and huntite.

The number of cooperating planes for the various types of calcite and huntite powder reflections, expressed in hexagonal indices, is (See Internationale Tabellen, 1935, p. 502):  $\{hkil\}$ , 2·12;  $\{hh2\bar{h}l\}$ , 12;  $\{0k\bar{k}l\}$ , 2·6;  $\{hk\bar{i}0\}$ , 12;  $\{hh2\bar{h}0\}$ , 6;  $\{0k\bar{k}0\}$ , 6;  $\{000l\}$ , 2. For dolomite powder reflections the analogous values are:  $\{hkil\}$ , 4·6;  $\{hh2\bar{h}l\}$ , 2·6;  $\{0k\bar{k}l\}$ , 2·6;  $\{hk\bar{i}0\}$ , 2·6;  $\{hh2\bar{h}0\}$ , 6;  $\{0k\bar{k}0\}$ , 6;  $\{000l\}$ , 2. The 4·6 and 2·6

entries for dolomite indicate that atoms in general positions, namely, oxygens, will scatter with a different amplitude for some of the co-operating planes of a given  $\{hkl\}$ ,  $\{hh2\bar{h}l\}$ , or  $\{hki0\}$  reflection than for others.

Zero amplitudes result for particular sets of planes whose hexagonal indices do not transform to whole-number rhombohedral indices. Thus, there are for dolomite only two non-zero oxygen amplitudes for  $\{21\cdot4\}$  and only one for  $\{02\cdot7\}$ . These relations are somewhat more simply stated in terms of rhombohedral indices: two non-zero oxygen amplitudes

TABLE 9. CORRELATION OF POWDER REFLECTION TYPES FOR THREE RHOMBOHEDRAL STRUCTURE CELLS (see text)

Calcite	Dolomite	Huntite
1a	1a	1a
1b	1b	2a
2a	1c	3a
2b	1d	4a
	2	
3	3	
		1b
		2b
		3b
		4b

result for all dolomite  $\{h_r k_r l_r\}$  in which  $h_r \neq k_r \neq l_r$ , except for  $\{h0\bar{h}\}$  reflections, which have a unique oxygen amplitude. The occurrence of zero amplitudes for calcite and huntite is such that there is only one non-zero oxygen amplitude for each  $\{h_r k_r l_r\}$ .

The amplitude contributions for calcite given in Table 3 have been calculated by using the value of  $x=0.2578$  (corresponding to a C—O distance of 1.286 Å) given by Chessin and Post (1958). Sass *et al.* (1957) obtained closely similar values,  $x=0.2593 \pm 0.0008$  and C—O = 1.294  $\pm$  0.004 Å. The amplitude contributions for dolomite derive from Steinfink and Sans' (1959) oxygen parameters,  $x=0.2374 \pm 0.0068$ ,  $y=-0.0347 \pm 0.0068$ , and  $z=0.2440 \pm 0.00017$ , and their value of  $z=0.2435 \pm 0.00031$  for carbon, all in terms of the hexagonal unit cell. The corresponding values for the rhombohedral unit cell upon which the discussion in this paper is based are  $x_0=0.4814$ ,  $y_0=-0.0281$ ,  $z_0=0.2787$ , and  $x_c=0.2435$ . The C—O distance for dolomite corresponding to these parameters is 1.283 Å, in particularly good agreement with Chessin and Post's value. All three of the parameter determinations are based

upon single-crystal measurements. Those for calcite involve oxygen-only reflections, and those for dolomite are based on some 500 reflections of all types.

The variable parameters used for the other calcite structures (Table 10) were calculated by assuming that the C—O bond length remains constant at 1.286 Å; the parameter  $x = C—O/a_0$ . The dolomite  $x$  and  $y$  hexagonal unit-cell parameters were multiplied by the ratio of  $a_0$  for  $\text{CaMg}(\text{CO}_3)_2$  to that of  $a_0$  for  $\text{CdMg}(\text{CO}_3)_2$ , so as to retain in  $\text{CdMg}(\text{CO}_3)_2$  the same C—O value of 1.283 Å found for dolomite. In the absence of evidence for making other assumptions, the dolomite  $z$  parameters for

TABLE 10. ESTIMATED VARIABLE PARAMETERS USED IN INTENSITY CALCULATIONS

$\text{MgCO}_3$	$x = 0.2776$	$\text{CdCO}_3$	$x = 0.2614$
$\text{MnCO}_3$	$x = 0.2692$	$\text{CoCO}_3$	$x = 0.2761$
$\text{FeCO}_3$	$x = 0.2743$	$\text{NiCO}_3$	$x = 0.2797$
$\text{ZnCO}_3$	$x = 0.2764$	$\text{CuCO}_3$	$x = 0.2681^*$
$\text{CaMn}(\text{CO}_3)_2$	$x = 0.2635$	$\text{CaFe}(\text{CO}_3)_2$	$x = 0.2657$
$\text{CaMn}(\text{CO}_3)_2$	$x_0 = 0.4779$ , $y_0 = -0.0241$ , $z_0 = 0.2782$	$x_C = 0.2435$	
$\text{CaFe}(\text{CO}_3)_2$	$x_0 = 0.4799$ , $y_0 = -0.0264$ , $z_0 = 0.2785$	$x_C = 0.2435$	
$\text{CdMg}(\text{CO}_3)_2$	$x_0 = 0.4829$ , $y_0 = -0.0298$ , $z_0 = 0.2789$	$x_C = 0.2435$	

\* Using the  $a_0$  value given by Pistorius (1960).

oxygen and carbon were retained for  $\text{CdMg}(\text{CO}_3)_2$ , as was the slight rotation of the carbonate group relative to the hexagonal  $a$  axes, and the parameters for the hexagonal cell were then converted to values for the rhombohedral cell. Coplanarity of carbon with the oxygens of its carbonate group is not required by symmetry for the dolomite structure as is the case for calcite. The reality of the 0.0005 difference between the Steinfink and Sans  $z$  parameters for oxygen and carbon is indeterminate, because the uncertainty ranges attached to these values are just great enough to allow for coplanarity at  $z = 0.2438$ . The intensity difference for this shift of carbon by about 0.01 Å is, in any event, insignificant compared with other sources of error.

Parameter assumptions of the same type as those for  $\text{CdMg}(\text{CO}_3)_2$  were used in calculating the values given in Table 10 for dolomite structures having the compositions  $\text{CaMn}(\text{CO}_3)_2$  and  $\text{CaFe}(\text{CO}_3)_2$ . These parameters involve a further approximation because, as discussed earlier, the  $a_0$  values available for the calculations were not measured on ordered compounds. The  $a_0$  available for  $\text{CaMn}(\text{CO}_3)_2$  is that for disordered material, that for  $\text{CaFe}(\text{CO}_3)_2$ , merely the mean of the values for calcite and siderite. However, these parameters are the best that can

be derived at present for making intensity estimates for order reflections. Parameter estimates for calcite-type structures having the compositions  $\text{CaMn}(\text{CO}_3)_2$  and  $\text{CaFe}(\text{CO}_3)_2$  are also shown in Table 10.

The variable parameters given by Graf and Bradley (In press) for a huntite structure model derived from powder *x*-ray diffraction data are, for the rhombohedral unit cell,  $x_{\text{Mg}}=0.541$ ,  $x_{\text{CII}}=-0.039$ ,  $x_{\text{OI}}=0.365$ ,  $x_{\text{OII}}=0.096$ ,  $x_{\text{OIII}}=-0.033$ ,  $y_{\text{OIII}}=0.180$ ,  $z_{\text{OIII}}=0.371$ .

#### INTENSITIES

Intensities of front reflections in powder diagrams of the rhombohedral carbonates, computed for copper radiation, are given in Table 4. The change of intensities in the solid solution series between  $\text{CaMg}(\text{CO}_3)_2$  and the hypothetical end member,  $\text{CaFe}(\text{CO}_3)_2$ , is shown graphically in Fig. 1. Estimated changes in cell size with composition have been considered in the ferroan dolomite computations, but these computations do not allow for departure of  $\text{CaCO}_3$  content from 50 mol percent.

These intensities are simply the products of  $F^2$  times multiplicity times the combined Lorentz and polarization correction for Debye-Scherrer lines on a cylindrical film,

$$\frac{1 + \cos^2 2\theta}{\sin^2 \theta \cos \theta}$$

Absorption and temperature factors have not been considered, but could be added as corrective multipliers suitable for a given experimental situation. The scattering factors given by Berghius *et al.* (1955) were used for C, O, Ca, and  $\text{Mg}^{++}$ , all self-consistent field data with exchange, with the curve for  $\text{Mg}^{++}$  at  $(\sin \theta/\lambda) < 0.25$  diverted toward the value for the neutral Mg atom at  $\sin \theta/\lambda = 0$ . Watson and Freeman (1961) give self-consistent field data with exchange for Mn, Fe, Co, Ni, and  $\text{Cu}^+$ ; the latter curve at  $(\sin \theta/\lambda) < 0.25$  has been diverted toward the value for the neutral Cu atom at  $\sin \theta/\lambda = 0$ .

The curve of Berghius *et al.* for Zn, based on self-consistent field data *without* exchange, gives expectably low values relative to the curves computed with exchange; it is essentially coincident with the Cu curve over part of the  $\sin \theta/\lambda$  range. The values for Zn used in this paper were taken from a curve drawn, at each  $\sin \theta/\lambda$  value, the same distance above the Cu curve as the separation between the Cu and Ni curves at that point. The scattering factor curve used for Cd, the only recent one available, was computed by Thomas and Umeda (1957) from the Thomas-Fermi-Dirac model.

These scattering factor curves fall off in generally concordant fashion and make it possible to observe the effect of progressively heavier cations upon the relative intensities of the various carbonate reflections. These

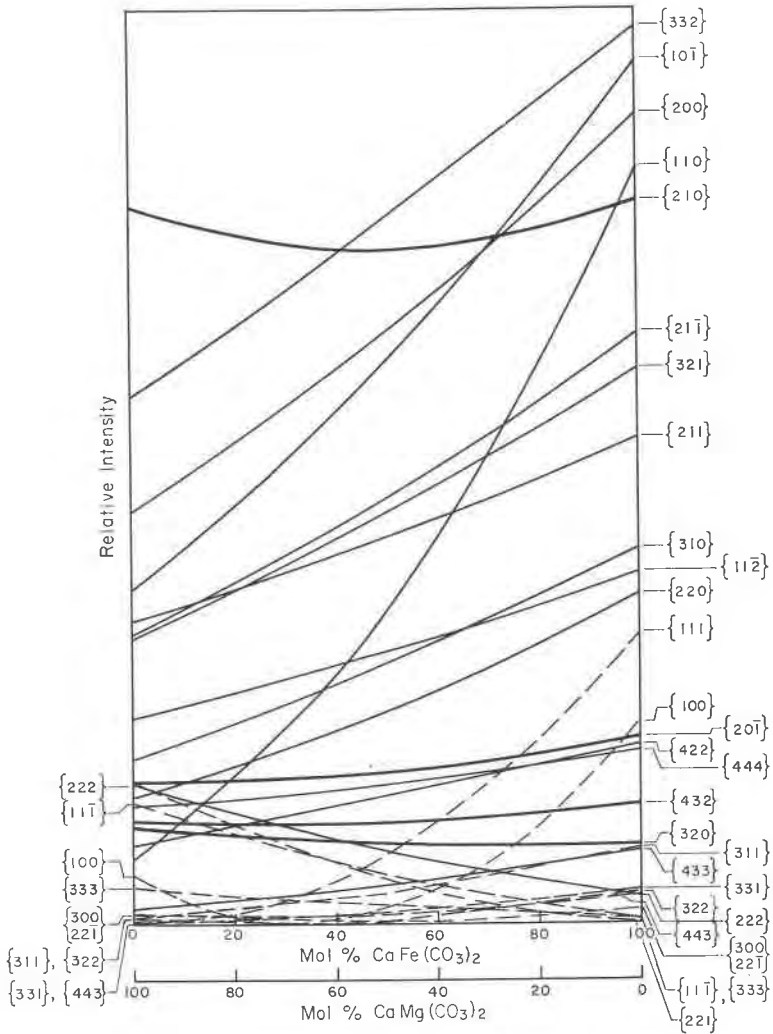


FIG. 1. Computed relative intensities for powder reflections in the front reflection region, using copper radiation, for the solid solution series between  $\text{CaMg}(\text{CO}_3)_2$  and the hypothetical end-member,  $\text{CaFe}(\text{CO}_3)_2$ . Order reflections are shown by dashed lines, strong oxygen reflections by heavy lines. The intensity of the very strong {211} reflection is plotted reduced by a factor of ten relative to those of the other reflections; that of {321}, reduced by a factor of two.

relations are modified somewhat by differences in atomic arrangement in the related calcite, dolomite, and huntite structures. The increase in intensity of the  $\text{CdMg}(\text{CO}_3)_2$  order reflections relative to those of the other ordered 1:1 carbonates is noteworthy.

The computed intensities of Table 4 and Fig. 1 are based upon a simplified model essentially involving spherical neutral atoms at rest, in accord with the empirical observation that observed intensities are better explained using neutral-atom scattering factor curves than those for ions. The radically different solubility rates of, for example,  $\text{CaCO}_3$  and  $\text{NiCO}_3$  in HCl solution indicate that an error is introduced for reflections at  $(\sin \theta/\lambda) < 0.25$  by this uniform bonding approximation. The determination of scattering factor curves appropriate for specific carbonate structures is, however, beyond the scope of this paper. The third figure given in the computed intensities is obviously not generally significant, but may have meaning, for example, in computing an intensity ratio for two reflections of the same compound which lie at about the same  $2\theta$  angle and have similar structure factors.

It should be noted, in comparing observed intensities of two or more carbonates with the equivalent computed values in Table 4, that the observed values must be suitably corrected so that they all represent intensity diffracted from the same number of unit cells.

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