VIBRATIONAL SPECTRA OF THE COMMON SILICATES: I. THE GARNETS

RAYMOND K. MOORE AND WILLIAM B. WHITE, Materials
Research Laboratory and Department of
Geochemistry and Mineralogy,

AND

THOMAS V. LONG, Department of Chemistry, The Pennsylvania State University, University Park, Pennsylvania 16802.

ABSTRACT

Infrared spectra have been measured on 22 specimens of silicate garnet and Raman spectra on 6 specimens. Seventeen IR modes were found as predicted by a factor group analysis. Not all of the predicted 25 Raman lines were found. The factor group splitting of the tetrahedral vibrations correlates with the occupancies of the octahedral and cubal sites. The site group splitting was used to measure the distortion of the garnet tetrahedral site.

Introduction

The number of papers presenting infrared spectra of silicate minerals is immense. Many of these are listed in Lyon's (1962-a) bibliography. One of the most recent and complete such collections is Lyon's (1962-b) unpublished catalog of infrared spectra of silicate minerals prepared in connection with lunar exploration techniques. Interpretation of these spectra has been by mainly empirical arguments. Shifts in frequency and intensity with composition can be measured and form the most rigorous approach developed to date. This technique was applied systematically to the layer silicates by Stubican and Roy (1961) and to the olivine and spinel families independently by Tarte (1962). It has become known as the "method of isomorphous substitution."

The justifications for beginning a new round of refinements on the vibrational spectra of the common silicates are the following:

- 1. Infrared data can now be obtained in the range of 400–50 cm⁻¹ thus providing information on the low-frequency vibrations not usually available in the earlier studies.
- 2. Measurement of the Raman spectra yields a whole new set of information which, in centro-symmetric crystals, is nonoverlapping with any of the infrared frequencies.
- 3. Theoretical methods can be used which will predict the number and selection rules of all vibrational modes.

This paper presents vibrational spectra and interpretation for silicate minerals with the garnet structure. The high symmetry and presence of only isolated SiO₄ tetrahedra in garnet make the theoretical analysis of

the vibrations more useful than would be the case with most other silicates.

Compared with other silicates, the infrared spectra of silicate garnets have been little investigated. Only the recent paper by Griffith (1969) reports the Raman spectra of the silicate garnets. Infrared spectra have been reported by Launer (1952), Wickersheim, Lefever, and Hanking (1960), Wickersheim (1961) and Tarte (1965). The first two papers deal qualitatively with spectra in the range 650 to 1200 cm⁻¹ in which only two to five of the infrared bands are observed. Wickersheim (1961) presents the infrared spectrum of one natural silicate garnet (almandine) in the range 250 to 1200 cm⁻¹ and the spectra of impurity SiO₄ bands in YIG in the range 600 to 1000 cm⁻¹. Tarte's paper is the most comprehensive and presents spectra (in the range of 300 to 1000 cm⁻¹) of a large number of natural silicate garnets (including high-titanium garnets) as well as that of synthetic germanate garnets. Only qualitative interpretations were attempted on an incomplete set of bands.

Investigations of the infrared spectra of the yttrium and rare earth garnets have been carried out by Wickersheim (1961) and McDevitt (1969). Excellent papers on rare earth garnets utilizing factor group and site group methods for the analysis of Raman spectra have been published very recently. (Hurrell, Porto, Chang, Mitra, and Bauman, 1968, Koningstein and Toaning-Ng, 1968, and Koningstein and Mortensen, 1968).

EXPERIMENTAL METHODS

A suite of 19 garnets of varying composition was assembled. Elemental analyses were performed by emission spectrographic methods, and ferrous/ferric ratio determined by wet analytic methods. Cell edges and refractive indices were measured. The chemical composition was normalized into mole ratios of the three dominant end members of the pyrope (Py)-almandine (Al)-spessarite (Sp) series and the grossularite (Gr)-andradite (An)-uvarovite (Uv) series. A code name was attached to each specimen according to the dominant end member. The code names, the cell edges, and the molecular proportions are listed in Table 1. These same garnet crystals were used to investigate the optical spectra of the transition metal ions and full details of the characterization are reported there (Moore and White, in preparation).

Specimens for infrared measurements were ground to fine powders. Spectra in the range of 2000–300 cm⁻¹ were obtained on a Perkin Elmer Model 621 spectrophotometer using the powders vacuum-pressed into KBr discs. Spectra in the range of 600–50 cm⁻¹ were obtained on a Beckmann IR-11 spectrophotometer from powders slurried directly onto polyethylene slabs.

Raman spectra were measured from 2–3 mm cubes of single crystal oriented to have {100} faces. A Spex model 1400 double monochromator was used with a 30 mW Spectra-Physics Model 112 He-Ne laser as a source. The He-Ne excitation wavelength of 6328 Å occurs in a transmission window of the optical spectrum. Measurement of the Raman spectra of iron-containing garnets would have been very difficult with conventional sources because of the high absorbance in the blue. Polarization measurements were made by in-

Sample	Lattice parameter	Ру	Al	Sp	Gr	An	Uv
Al-77	11.499	18.0	77.0		4.6	0.4	-
Al-76	11.521	8.0	76.0	3.6	13.0	_	-
Al-68	11.533	22.6	67.8	5.0	3.3	1.3	====
Al-67	11.523	23.0	67.5	3.0	6.4	-	-
Al-51	11.530	33.6	51.0	0.9	13.1	1.4	200
Py-71	11.525	71,4	16.0	0.9	3.4	1.0	7.3
Py-59	11.502	59.1	37.5	1.7	1.7	-	_
Sp-70	11.607	6.8	22.4	70.0		0.8	-
Sp-53	11.571	0.9	45.5	53.0	0.7		-
Gr-92	11.844	3.1	0.5	27.5	92.0	4.6	-
Gr-92B	11.848	3.0	0.7	-	92.1	4.4	-
Gr-90	11.843	-	3.2	0.6	89.9	6.4	-
Gr-89	11.847	-	4.3	0.5	89.0	6.3	-
Gr-87	11.843	-	6.0	0.6	87.3	6.4	-
Gr-74	11.857	0.5	4.7	2.6	73.6	18.4	-
An-94	12.033	1,2	-	0.5	4.5	94.0	-
An-93	12.049	-	1.0	0.5	5.5	93.0	-
AnTi-84	12.101	4.0	-	0.4	11.5	84.0	_
Uv-44	11.920	6.6	_	1.4	29.0	19.0	44.0

TABLE 1. LATTICE PARAMETER AND MOLECULAR PROPORTIONS OF THE END-MEMBERS FOR EACH SPECIMEN

serting a half-wave plate in the laser beam and rotating a polarizer placed between the polarization scrambler and the entrance slit.

RESULTS

Infrared Spectra. The IR spectra of all pyralspites are similar, as are the spectra of all ugrandites. Typical examples, the spectrum of an almandine, Al-77, and an andradite, An-93 are shown in Figure 1. The bands are given a simple alphabetical label for identification. Band frequencies for all 19 specimens are listed in Table 2. Two weak bands appear between the D and E bands in the high-titanium and high-chromium garnets. Other than these, a maximum of 17 bands are observed in the infrared.

No previous author has examined the full infrared range for the natural silicate garnets; the most complete previous work is that of Tarte (1965) in which he reports twelve bands in the range 300 to 4000 cm⁻¹. The same number of bands was found in this range in the present study.

Hurrel et al. (1968) obtained the infrared spectrum of yttrium aluminum garnet over the entire infrared range and observed a total of fifteen

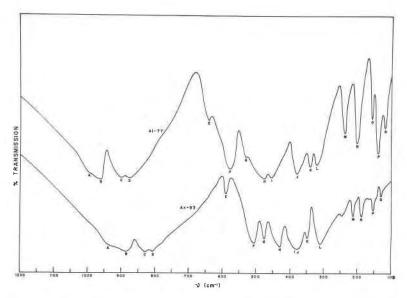


Fig. 1. Typical infrared spectra for an almandine (Al-77) and an andradite (An-93). The letter code on the bands refers to Table 2.

bands. They postulated that the two missing bands are weak and possibly degenerate with other modes. Their data for YAG are also listed in Table 2.

Raman Spectra. Only six samples were examined by Raman experiments. The band frequencies are presented in Table 3. The spectra of samples Al-68 and An-93 as typical examples are shown in Figure 2. A maximum of twenty bands were observed in the spectra (Gr-90).

Koningstein and Mortensen (1968) report the Raman spectra of YAG, YbAG and YGaG at room temperature and 100°K. They observed a maximum of 22 bands in the YAG sample. Koningstein and Toaning-Ng (1968) obtained the spectrum of a Thulium Gallium Garnet at 80–85°K and observed a maximum of 12 bands. Hurrel et al. (1968) obtained the spectrum of YAG at 90°K and observed all but three of the predicted 25 modes. In the latter two papers, polarization data for the Raman spectra were obtained and bands were assigned to particular irreducible representations.

THEORETICAL ANALYSIS

The Factor Group Method. The first necessity in analyzing the garnet spectra is to determine the number of vibrational modes and the selection

Table 2, Infrared Band Frequencies (in cm⁻¹) for All Specimens Measured

,	AI-	AI-	Al-	Al-	Al-	Py-	Py-	Sp-	Sp-	Gr-	Gr-	Gr-	Ğ	Ğr	Gr-	An-	An-	Uv-	AnTi-	
Band	77	76	89	29	51	71	29	70	53	92	92B	06	68	87	74	94	93	44	84	YAG^a
A	991	066	988	066	186	995	966	926	983	951	952	948	951	956	950	929	929	961	924	1
В	096	962	096	096	196	965	964	949	951	905	200	911	912	915	910	888	888	899	998	812
C	897	897	668	968	968	268	268	895	888	852	855	858	858	860	854	831	831	839	826	738
О	870	873	863	870	869	870	870	861	863	834	835	840	841	841	835	812	811	826	810	069
	1			-			1	1		750	754	l	1			1		748	734	
	1					1	1											675	029	
Ħ	635	636	636	638	040	1		631	631	617	617	619	619	619	616	591	589	617	589	570
H	571	571	569	570	574	580	577	565	565	540	539	544	547	553	543	512	510	542	513	521
Ö	526	528	526	526	528	536	530	495	521	502	502	500	505	505	502	479	477	484	477	483
H	469	476	475	478	481	492	481	470	471	476	471	473	471	478	471	439	438	463	435	467
Н	448	452	451	452	457	458	455	447	447	445	442	451	450	453	445		400	432	398	430
-	376	377	378	378	381	386	379	379	377	385	387	393	392	390	387	390	383	375	385	392
M	338	339	340	340	342	345		341	342			347	345		343	352	348		345	371
T	317	316	317	314	324		327	308	314	1		1	1		296	309	310		308	330
M	237	238	236	234	240	248	243	242	246	238	240	240	240	241	236	211	211	229	215	290
Z	192	200	199	197	203	209	196	203	210	200	202	203	202	203	200	186	187	198	187	219
0	156	159	157	157	160		-	165	1	180	179	183	183	183	179		1	170		165
ď	137	138	137	137	140	149	141	140	138	-	1		140		153	133	132		127	120
0	116	116	116	115	119]	125	113	112				117		125	113				1

^a Spectrum of yttrium aluminum garnet from Hurrel et al. (1968).

TABLE 3. RAMAN SHIFTS (IN CM-1) OF GARNETS

Band	Al-77	Al-68	Al-67	Sp-70	Gr-90	An-93
1	917	918	890	896	888	875
2	839	841	843	_	859	844
3	796	798	806	-	826	816
4		-	-		759	751
5	749	748	745	743	734	728
6	_	-	695	_	695	700
7	665	659	644	-	662	679
8	625		-	-	638	659
9	_	600	611	617	592	631
10	566	571	562	-	570	581
11	_	-	-	_	557	562
12	_	-	-	-	533	552
13	505	509	517	503	516	501
14	_		468	-	483	476
15	_	-	400		426	461
16	_	-			416	425
17	-	390	-		378	373
18	_	_			348	358
19	_	-	-		330	317
20	_	_	307		312	_
21	_	-	-	-	287	-
22	-	-	266		257	241
23	-	_	_	-	160	_
24	_	-	-	-	128	_

rules that control them. Crystalline solids that do not contain well defined molecular units can best be analyzed by the factor group method. Factor group analysis takes into account all atoms in the solid whereas the more commonly used site group method [cf. Duke and Stephens (1964) for an analysis of the vibrations of the isolated SiO₄ groups in olivine using the site group method] accounts only for the motions of the molecular units. Although factor group analysis is commonly used in the Physics literature for analysis of the vibrational spectra of crystals, it is difficult to point to a satisfactory review article. Mitra and Gielisse (1964) and White and DeAngelis (1967) discuss the method in some detail. For a complete mathematical treatment see Maradudin and Vosko (1968).

Application to the Garnet Structure. Garnet is cubic, space group $Ia3d(O_h^{10})$, with $8A_3B_2(CO_4)_3$ units per unit cell. The smallest Bravais cell is primitive with 4 formula units per unit cell. In the garnet structure the A atoms are 8-fold coordinated with D_2 site symmetry, the B atoms

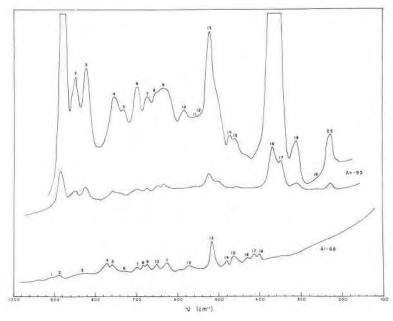


Fig. 2. Raman spectra for an almandine (Al-68) and an andradite (An-93). The two spectra of andradite represent two intensity settings of the spectrometer. The numbers on the bands refer to Table 3.

are 6-fold coordinated with S_6 site symmetry, and the C atoms (primarily Si) are 4-fold coordinated with S_4 site symmetry.

There are 3n degrees of freedom in a crystal, where n is the number of atoms in the unit cell. The full body-centered cell contains 480 degrees of freedom or 240 degrees of freedom in the primitive cell. It is convenient to perform the analysis on the full cell with factor group O_h .

The invariance conditions for the atoms in the garnet structure and the reducible representations are tabulated in Table 4. From the reducible representation of the primitive cell, the vibrational degrees of freedom are classified among the irreducible representations of the factor group in Table 5. Seventeen infrared and twenty-five Raman active modes are predicted by the selection rules. Similar methods of classifying the normal modes for the garnet structure were apparently used by Hurrel et al. (1968), and Koningstein and Mortensen (1968).

Site Group Analysis. The complete factor group analysis yields the true symmetry of the various normal modes and the correct selection rules, but it is not very instructive when one wants to assign the normal modes to specific atomic motions.

Table 4. Invariance Conditions for Garnet Space Group Ia3d, $O_{\rm h}{}^{10}$

Oh	E	$8C_3$	$6C_2$	$6C_4$	$3C_2$	i	6.54	856	$3\sigma_h$	6σ,
a -site, S_6	E	C_3, C_3^2	_	_	_	i		S_6^5, S_6		_
ω_{ρ} (16Al)	16	4	0	0	0	16	0	4	0	0
d -site, S_4	E		_		C_2	-	S_4, S_4^3	_	_	
ω_{ρ} (24Si)	24	0	0	0	8	0	8	0	0	0
c -site, D_2	E	_	$C_{2(z)}, C_{2(y)}$, —	$C_{2(x)}$			_	_	_
ω_{ρ} (24Ca)	24	0	8	c	8	0	0	0	0	0
h -site, C_1	E		_	_	_	_	_			_
ω_{ρ} (960)	96	0	0	0	0	0	0	0	0	0
ω_{p}	160	4	8	0	16	16	8	4	0	0
χ_{ρ}	480	0	-8	0	-16	-48	-8	0	0	0
$\Gamma_{ m RED} = \chi_{ ho/2}$	240	0	-4	0	-8	-24	-4	0	0	0

The garnet structure contains discreet SiO₄ tetrahedra which behave nearly independently of the other components of the structure. The binding of the SiO₄ tetrahedra by the 6- and 8-fold cations can be considered weak compared to the binding of the Si–O bonds themselves. This model, although only a very rough approximation in the garnet

Table 5. Classification and Selection Rules for Fundamental Modes of Garnet

0	A7	A	Tra	ansla	torya	There a	Detectors	(SiO ₄)	Selection
O_{h}	N_{T}	Acous.	S_4	D_2	S_6	- Trans.b	Rotatory	Internal	rules
A_{1g}	3	0	0	0	0	0	1	2	Raman
A_{2g}	5	0	1	1	0	2	0	3	Inactive
$E_{\mathbf{g}}$	8	0	1	1	0	2	1	5	Raman
T_{1g}	14	0	2	3	0	5	3	6	Inactive
$T_{2\mathbf{g}}$	14	0	3	2	0	5	2	7	Raman
A_{1u}	5	0	1	0	1	2	0	3	Inactive
A_{2u}	5	0	0	1	1	2	1	2	Inactive
$E_{\mathbf{u}}$	10	0	1	1	2	4	1	5	Inactive
T_{1u}	18	1	3	3	3	8	2	7	Infrared
$T_{2\mathbf{u}}$	16	0	2	2	3	7	3	6	Inactive

^a Translatory motions of individual cation sub-lattices.

^b Total translatory modes=sum of $S_4+D_2+S_6$.

structure, can be used as a starting point to determine the behavior of independent SiO₄ tetrahedra.

Using this model, the number of translatory (essentially cation motions), rotatory (tetrahedral rocking motions) and internal degrees of freedom (tetrahedral independent motions) are:

Units	Internal	Translatory	Rotatory
12(SiO ₄)	108	36	36
8B	0	24	0
12A	0	36	0

The classification of each type of mode is given in Table 5.

The site symmetry of the tetrahedral site in garnet is S_4 whereas the normal molecular group is T_d . It is possible therefore to determine the site splitting or removal of degeneracy by a descent in symmetry method:

$T_{ m d}$	S_4
$12A_{1g}$	12A
$12E_{ m g}$	12A + 12B
$12T_{2g}$	12B + 12E
$12T_{2g}$	12B + 12E
	$12A_{1\mathbf{g}} \\ 12E_{\mathbf{g}} \\ 12T_{2\mathbf{g}}$

The degeneracies of the $T_{\rm d}$ modes are removed to some extent by the lowering of the symmetry of the site. In addition, the selection rules are changed. Therefore in the limiting case where the tetrahedra act independently of the lattice, we would expect 5 IR active internal modes and 9 Raman active internal modes.

By the reversal of the above process the factor group representations to which these internal modes belong can be determined. An example of this method for ν_1 mode is given below:

Mode	S_4	$T_{\mathbf{d}}$	O_{h}
ν_1	12A	$2A_{1g}$	A_{1g}
		$2E_{f g}$	$\begin{cases} A_{2u} \\ E_{g} \end{cases}$
		$2T_{1\mathrm{g}}$	$\begin{cases} E_{\mathbf{u}} \\ T_{\mathbf{1g}} \\ T_{\mathbf{2u}} \end{cases}$

This information for all tetrahedral modes is summarized in Table 6.

ASSIGNMENTS

Raman Spectra. The assignments of the Raman spectra were based on polarization data obtained from a single crystal of sample Gr-90. The crystal was cut into a cube with {001} faces. The crystal was placed in the sample holder such that the incident beam direction was parallel to a crystallographic axis, and the scattered radiation parallel to an orthogonal axis. Polarizers were inserted in the incident beam and in the

TABLE 6. INTERNAL MODE DISTRIBU	BLE 6 INTERNA	. Mode Distribution	N
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O_{h}	Internal	ν_1	ν_{2}	ν_3	ν_4
A_{1g}	2	1	1	0	0
A_{2g}	3	0	1	1	1
$E_{\mathbf{g}}$	5	1	2	1	1
T_{1g}	6	1	1	2	2
T_{2g}	7	0	1	3	3
A_{1u}	3	0	1	1	1
$A_{2\mathrm{u}}$	2	1	1	0	0
$E_{\mathbf{u}}$	5	1	2	1	1
T_{1u}	7	0	1	3	3
T_{2u}	6	1	t	2	2

 $^{^{}a}$ ν_{1} , ν_{2} etc. are Herzberg's (1945) notation for the vibrational motions of a regular tetrahedral molecule. ν_{1} is the symmetric stretch, ν_{2} the symmetric bend, ν_{3} the antisymmetric stretch, and ν_{4} the antisymmetric bend.

scattered beam. By rotating the analyzer 90° the polarizability components of the scattered radiation could be observed parallel and perpendicular to the plane of polarization of the incident beam. These two experimental conditions are summarized by the notation x(yy)z and x(yx)z (This notation is due to S. P. S. Porto and is widely used). The two letters inside the brackets represent the directions of polarization for the incident and scattered beams respectively, and the letters outside the brackets represent the direction of the incident and scattered beams respectively. Under the experimental conditions, the A_{1g} and E_{g} modes are observable under parallel polarizers but not under crossed polarizers, while the T_{2g} modes are observable under crossed, but not parallel polarizers. A summary of the experimental conditions for the observation of these modes is presented in Table 7.

Examples of the polarized spectra are presented in Figure 3. The $A_{\rm lg}$ and $E_{\rm g}$ modes do not completely extinct when the polarizers are

Table 7. Polarizability Components and Conditions for the Experimental Observation of the Raman Modes

	Polarizability	Experimenta	lly observable
Mode	component	y(xx)z	y(xy)z
A_{1g}	xx, yy, zz	yes	no
$E_{\mathbf{g}}$	yy, xx+yy-2zz	yes	no
T_{2g}	xy, xz , yz	no	yes

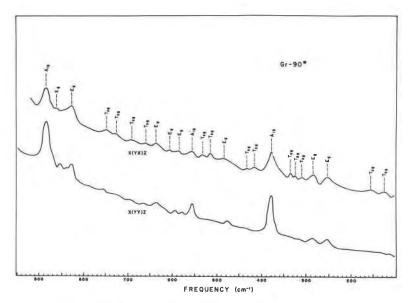


Fig. 3. Raman spectra of a grossularite (Gr-90) garnet in two polarization directions.

crossed [x(yx)z]. This is partly due to internal reflections, caused by internal fractures in the crystal, and to misalignment of the crystal (intentional in this case). Koningstein and Toaning-Ng (1968) have shown that, when a garnet crystal is rotated away from axis alignment with the incident and scattered radiation, the $E_{\rm g}$ polarizability components transform to all possible quadratic combinations, whereas the $A_{\rm lg}$ polarizability components remain the same. In Figure 3, the $E_{\rm g}$ modes have nearly the same intensity under both experimental conditions, while the three $A_{\rm lg}$ modes decrease in intensity markedly under crossed polarizers [x(yx)z]. The spectra were run numerous times with more precise alignment of the crystal, and the experimental conditions outlined in Table 7 were nearly attained. The spectra in Figure 3 are used for illustration because they exhibit the most complete set of observed bands.

A summary of the assignments is given in Table 8, along with the results for YAG as determined by Hurrel et al. (1968). These assignments are tentative. The frequencies of the observed bands are plotted as a function of the lattice parameter in Figure 4. The lines indicate possible correlations. The assignment of these Raman bands to particular site motions is based partly on the consensus that the high-frequency bands represent molecular motions of the tetrahedra and on the site group characteristics.

TABLE 8. RAMAN ASSIGNMENTS

Band (Gr-90)	Representation	Site motion	Band (YAG)a	Representation
888	A_{1g}		857	$T_{ m 2g}$
859	$E_{\mathbf{g}}$		783	$A_{1\mathrm{g}}$
826	$E_{\mathbf{g}}$	ν_1 and ν_3	758	$E_{\mathbf{g}}$
759	$T_{2\mathbf{g}}$		719	$T_{2\mathbf{g}}$
734	$T_{2\mathbf{g}}$		714	$E_{\mathbf{g}}$
695	$T_{2\mathbf{g}}$		690	$T_{ m 2g}$
662	$T_{2\mathbf{g}}$		561	$A_{1\mathbf{g}}$
638	$E_{f g}$		544	$T_{2\mathbf{g}}$
592	$E_{\mathbf{g}}$		537	$E_{\mathbf{g}}$
570	$E_{\mathbf{g}}$	ν_2 and ν_4	531	$E_{\mathbf{g}}$
557	$A_{ m 1g}$		436	$T_{2\mathbf{g}}$
533	$T_{ m 2g}$		408	$T_{2\mathbf{g}}$
516	$T_{2\mathbf{g}}$		403	E_{g}
483	$E_{\mathbf{g}}$		373	$A_{ 1 {f g}}$
426	$T_{2\mathbf{g}}$	Rotatory	340	$E_{\mathbf{g}}$
416	$T_{ m 2g}$		310	$E_{\mathbf{g}}$
378	$A_{1\mathbf{g}}$		296	$T_{2\mathrm{g}}$
348	$T_{ m 2g}$		243	$T_{2\mathbf{g}}$
330	$T_{ m 2g}$	S_4 Trans.	218	$T_{2\mathbf{g}}$
312	$T_{2\mathbf{g}}$		162	$E_{\mathbf{g}}$
287	$E_{\mathbf{g}}$		144	$T_{2\mathrm{g}}$
257	$E_{\mathbf{g}}$		-	-
160	$T_{ m 2g}$	D_2 Trans.	-	-
128	$T_{ m 2g}$		-	-

^a Hurrel et al. (1968).

Two of the three A_{1g} Raman active modes arise from internal tetrahedral motions, one from ν_1 and one from ν_2 . The third A_{1g} mode arises from rotatory or rocking motions of the tetrahedra. There is general agreement that the ν_1 would be higher in frequency than ν_2 , and that the rotatory modes are generally the lowest frequency. Based on this assumption, we can assign the three A_{1g} modes to the site and rotatory motions. ν_1 and ν_3 may be tentatively listed together for purposes of illustration. The ν_1 symmetric stretch yields an A_{1g} and an E_g type Raman active mode, while ν_3 yields an E_g and three T_{2g} type Raman active modes. Therefore, six modes are predicted in the Raman spectra $(A_{1g}, 2E_g, \text{ and } 3T_{2g})$. Hurrel et al.'s work on YAG, where the grouping of the high-frequency bands is more obvious, shows this aggregate of the six modes of ν_1 and ν_3 quite clearly. In the Gr-90 sample the six highest frequency modes also contain this set of ν_1 and ν_3 modes.

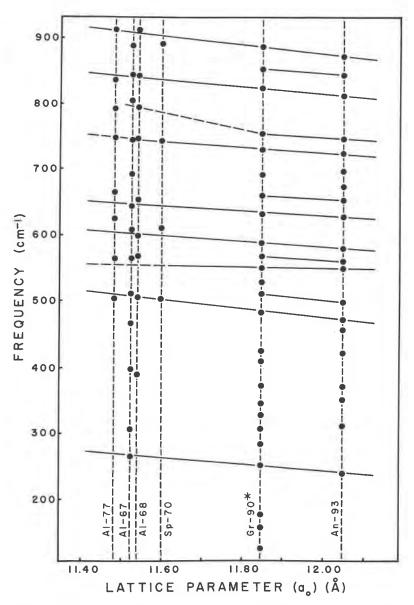


Fig. 4. Raman frequencies of garnets as a function of cell edge. Near-horizontal lines are intended to match corresponding bands.

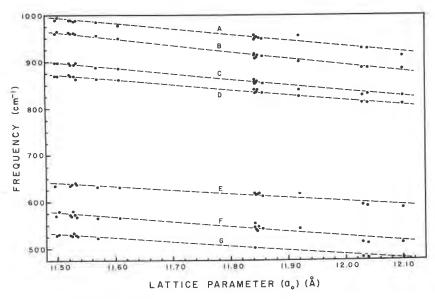


Fig. 5. Infrared frequencies of garnets as a function of cell edge.

To assign the remaining bands to specific motions as was done for ν_1 and ν_3 is less valid, since for these lower frequency bands the interaction between site motions could be an important factor. However, the assignment is tentatively completed by the same method as was outlined above. Such assignments are summarized in Table 8. This table includes the bands and assignments of YAG (Hurrel et al. 1968).

Infrared Spectra. Tarte (1965) and others have noted a linear relationship of the frequencies of the high-frequency infrared bands to the lattice parameter. Such plots for the first seven bands (A-G) are presented in Figure 5. It is seen that a linear relationship is indeed obtained. Bands below the frequency of G do not plot linearly. The tetrahedron in the natural silicate garnets remains nearly compositionally pure with the possible exception of the high-titanium garnets. It would be expected, therefore, that frequency changes of those bands representing essentially pure internal motions of the tetrahedra would be due to bond length changes, and as shown later, to differences in factor group splitting (also related to bond length changes). Bond length changes should result in linear frequency shifts of the bands as a function of the lattice parameter. Therefore, the seven bands A-G can reasonably be assigned to the tetrahedral site.

Similar plots of the frequencies of the remaining bands against the

TABLE 9. INFRARED ASSIGNMENTS

Band	Site	Site motion
A	S ₄	
В	S_4	ν_3
C	S_4	7.0
D	S_4	
E	S ₄	
F	S_4	ν_2 and ν_4
G	S_4	, , , , , , ,
Н	S ₆	
I	S_6	_
J	$\mathbf{D_2}$	_
K	D_2	
L		_
\mathbf{M}	_	_
N	-	_
O	_	_
P	_	_
Q	-	

average radii of the ions occupying the octahedral and dodecahedral (cubal) sites and against the average weight of the ions occupying these sites indicate that bands H and I can be related to the octahedral site, and bands J and K to the dodecahedral (cubal) site. The remaining bands do not yield reasonable plots for any parameter or are observed in too few specimens to observe valid variations, and thus cannot be assigned. These site assignments are summarized in Table 9 and are similar to those found by Tarte (1965).

Based on the assignments of Table 6, we would expect three infrared-active tetrahedral stretching vibrations at high frequencies. The group of four bands (A-D) at high frequencies consist of three very strong bands (B, C and D) and a weak shoulder (A) [Fig. 1]. The origin of the A band is not clear at the present time. The various rare earth garnets (McDevitt, 1969) exhibit only the expected 3 bands in this region.

The bands E-G can be related to the ν_2 and ν_4 infrared-active modes by analogy to the Raman spectra. Four bands are predicted from these modes; however, due to the strong interactions of the lower bands between site motions, the fourth member cannot be definitely identified.

STRUCTURAL CORRELATIONS

Based on the assignments in the previous sections, some structural characteristics of the tetrahedral site can be determined. The infrared

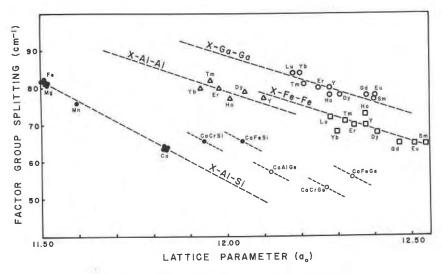


Fig. 6. The relation of the factor group splitting to cell edge for various garnets.

bands (B, C and D) assigned to ν_3 are of particular interest. The site and factor group splitting characteristics of this mode have been discussed. In the garnets in which the tetrahedral sites are coupled through octahedral and dodecahedral (cubal) cations, the factor group splitting would be expected to be of a larger magnitude than the site group splitting. The S4 site in natural silicate garnets is only slightly distorted from true $T_{\rm d}$ symmetry. Based on this, the three strong high-frequency bands in the infrared can be assigned to the two types of splitting as follows [C-D] is the site group splitting, and [B-(C+D)/2] is the factor group splitting. The factor group splitting values have been plotted against the lattice parameter in Figure 6. In addition, values calculated from the reported frequencies of these bands for various rare-earth garnets (McDevitt, 1969) as well as for a few germanium garnets (Tarte, 1965) are also plotted. Our data are shown as filled circles. When the 8fold cation is varied, the factor group splittings fall onto rather nice curves for each octahedral cation. The smallest dodecahedral cations correspond to the largest factor group splitting. This implies that the coupling between tetrahedral motions is stronger when the dodecahedral distances are smaller. On the other hand, variations in the octahedral cation seem to have little effect on the factor group splitting. The series Ca-B-Si and Ca-B-Ga in Figure 6 form nearly horizontal lines, the factor group splitting being nearly constant for each set of data.

The tetrahedral site in garnets shares two of its edges with the dodeca-

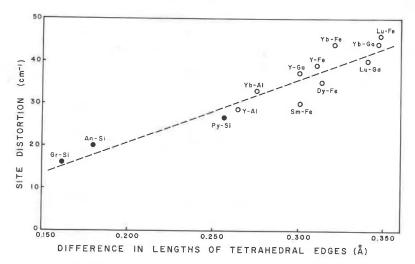


Fig. 7. Relation of the site group splitting to the distortion of the CO₄ tetrahedron of various garnets.

hedral (cubal) site and has four unshared edges. The length of the two shared edges is less than the value for the four unshared edges. Therefore, the difference between these two values is a measure of amount of tetrahedral distortion, since in an undistorted tetrahedron $(T_{\rm d})$ all six edges would have the same length.

In Figure 7, the average value for the site group splitting of the grossularite and pyrope samples as well as the value for a number of rareearth garnets (McDevitt, 1969) are plotted against the difference in the tetrahedral edges. The structural data are from Gibbs and Smith (1965) for pyrope, Prandl (1966) for grossularite, Novak (private communication) for andradite, and Euler and Bruce (1965) for the rare-earth garnets. The latter data are only accurate to ± 0.04 Å based on their reported random experimental errors. It is seen that the infrared site splitting provides a measure of the S_4 distortion of the tetrahedral site.

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