Crystal-structure refinements of IM plutonic biotites

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ABSTRACT

Crystal-structure refinements were performed on five plutonic IM biotite crystals from the three main lithologic complexes (granitic, syenitic, and monzonitic) and from a rock transitional between the granitic and monzonitic complexes of the same plutonic body in the Valle del Cervo (Vercelli, northwestern Italy). All refinements were carried out in the space group C2/m (R: 0.02-0.03 for four samples; R = 0.06 for one sample).

Although the Valle del Cervo biotite samples show similar chemical composition and crystal-chemical features, structural details as deduced from ΔF maps suggest different orientations of OH- groups in samples from different plutonic complexes.

Structural details of the biotites show that (1) octahedral-layer distortion in more Mg-rich biotites is greater (and analogous in M1 and M2 sites) than that in more Fe-rich biotites, where the “average” distortion of the octahedral layer decreases with increasing Fe content and the M1 site is more distorted and larger than the M2 site; (2) the reduction in (M-O) distance in the two octahedra causes a more marked reduction in the size of the M2 sites as compared with the M1 site; (3) octahedral geometrical parameters are affected both by their chemical composition and by the constraints of close packing within the layer; and (4) tetrahedral-ring distortion is not affected by the octahedral composition, whereas it is linked to the geometry of the ditrigonal cavity occupied by the interlayer cation.

INTRODUCTION

The basic mica structure was outlined by Pauling (1930) and refined many times. Although much attention has been given to the crystal chemistry of dioctahedral micas, the various trioctahedral Fe-Mg micas have received less attention (Bergerhoff et al., 1986). Of the latter, phlogopite has been studied most extensively, whereas annite, as well as micas along the phlogopite-annite join (biotites), are less understood. The recent literature contains no studies of crystal refinements of biotite from plutonic rocks; only biotites from volcanic and metamorphic rocks have been reported (Takeda and Ross, 1975; Bohlen et al., 1980), and only one IM biotite has been described (Takeda and Ross, 1975; Ohta et al., 1982). A detailed crystal-chemical study of five IM biotite samples from three lithologic complexes (granitic, syenitic, and monzonitic) and from a rock transitional between the granitic and monzonitic complexes in the same plutonic body is reported in order to assess to what extent petrologic conditions affect the crystal-chemical features of biotite.

EXPERIMENTAL

Samples

The five IM biotite crystals used for structure refinements were chosen from the three main lithologic complexes of the Valle del Cervo pluton (Vercelli, northwestern Italy): granitic (sample M13), syenitic (sample M32), monzonitic (samples M14 and M73), and a rock transitional between the granitic and monzonitic complexes (sample M62). The bulk chemical compositions of the rocks cover a wide range (Table 1).

X-ray single-crystal diffractometry

Single-crystal diffraction analysis is more difficult for micas than for many other rock-forming silicates because the mica crystals are often deformed and are very thin and platy. These features cause the diffraction peaks to be broad and to require relatively significant corrections for absorption. Special attention was therefore paid to experimental procedures, sample selection, and collection parameters in order to ensure reliable data and refinement results.

About 70 biotite crystals were examined preliminarily by Weissenberg or precession photography and by single-crystal diffractometry to select samples with well-defined periodicity along c*. In all five rock samples 1M, 2M, and disordered stacking sequences were found; in granitic and syenitic rock samples, the 3T polytype was also found.

The cell parameters and the diffraction intensities were measured for each of the five samples. Each was mounted along the b axis. Intensity data were measured with an ENRAF-NOMIUS CAD4 diffractometer using MoKα radiation and a flat graphite crystal monochromator. During inten-
sity collection the maximum variation of selected standard reflections did not exceed 2.5%. The equivalent monoclinic pairs $hkl$ and $h\bar{k}l$ were measured from $\theta = 2^\circ$ to $\theta = 30^\circ$ (starting from $l = 0$).

The $\Delta\omega$, $\Delta\theta$ plots (Einstein, 1974) showed a high degree of broadening along $\Delta\omega$ direction, and therefore the omega scan mode was chosen to ensure complete measurement of each peak intensity; the choice of a horizontal detector aperture as small as possible (between 0.3" and 1.0", as the angle is viewed from the crystal) ensured a high peak to background resolution (Davoli, 1989). Scan widths were $5^\circ$-$6^\circ$ in $\omega$ for samples M14, M32, M73, and M62 and $10^\circ$ in $\omega$ for sample M13.

The intensities were corrected for Lorentz-polarization and absorption effects following the semiempirical method of North et al. (1968); intensity data of symmetrically equivalent reflections were averaged. The resulting discrepancy factor $R_{sym}$ was calculated as reported in Table 3.

### Chemical analyses

Electron-probe microanalyses (EPMA) were performed with an ARS-SEMQ instrument using wavelength-dispersive techniques. Operating conditions were a 15-kV accelerating voltage, a 15-nA sample current, and a defocused electron beam (spot size of about 3 $\mu$m). Spectrometer data were reduced using the method of Ziebold and Ogilvie (1964) with correction factors of Albee and Ray (1970). Six analyses from different points on the same crystal showed high chemical homogeneity, and therefore these were averaged.

Atomic absorption analysis revealed that the amount of Li never exceeded 0.05 wt%. OH was determined by means of thermogravimetric analysis (TG and DTA) on crystals from the same rock. A Du Pont 990 thermal analyzer was used on about 10 mg of powder heated at the rate of 10$^\circ$/min in Ar gas (flow rate, 30 ml/min) to prevent Fe oxidation. Fe$^{3+}$ was determined by a semi-microvolumetric method (Meyrowitz, 1963). Structural formulae were calculated on the basis of $O + OH + Cl = 24$ (Table 2).

### Crystal-structure refinement

The crystal-structure refinements of $1M$ biotites were carried out without chemical constraints, using a version of the least-squares program ORFLS (Busing et al., 1962), rewritten at the Centro di Studio per la Cristallografia Strutturale of Pavia and revised locally. The program allows the assignment of two scattering curves $f_1$ and $f_2$ to every site affected by isomorphous replacement and refinement of the site occupancy $X(f)$ with the constraint that $X(f_1) + X(f_2) = 1$. The choice of the scattering factors was Fe$^{2+}$ versus Mg$^{2+}$ for M1 and M2, a composite of 75% Si and 25% Al versus 75% Si$^{4+}$ and 25% Al$^{3+}$ in site T, and O versus O$^{2-}$ (Tokonami, 1965) for anion sites. Fully ionized atomic scattering factors were used for sites M1 and M2 in order to obtain better final $R$ factors and estimated standard deviations of the refined parameters. It was assumed, on the basis of chemical analyses and bond lengths, that T is occupied by 0.75 Si and 0.25 Al, and, owing to the small difference between Al and Si scattering curves, no least-squares refinement of Al versus Si was carried out.
All the refinements were carried out in space group C2/m in the same coordinate setting as reported by Take
da and Ross (1975). Only reflections with $I > 5e(I)$ were used in order to reduce the standard deviations of the refined parameters without loss of statistically significant $F_{\text{obs}}$ in least-square cycles. (For applications of these refinement procedures to other rock-forming minerals, see Ungaretti, 1980; Ungaretti et al., 1983; Davoli, 1987.)

During refinement cycles, occupancy factors and thermal parameters were varied separately; attempts to vary all parameters simultaneously gave a higher $R$ factor and higher estimated standard deviations and correlation coefficients.

An attempt was made to refine sample M13 in space groups C2 and Cm. In order to avoid false $R$ minima or high correlations between couples of pseudo-related atoms in the lower-symmetry space groups, atoms related by pseudo-symmetry elements were shifted from their positions and refined in separate least-squares cycles. No enhanced results (Hamilton, 1965) were found.

Unit-cell parameters (obtained by least-squares refinement of 25 automatically centered reflections in the range $15^\circ \leq \theta \leq 30^\circ$) and some refinement data are in Table 3. Crystallographic coordinates and equivalent isotropic and anisotropic temperature factors are in Table 4. A list of observed and calculated structure factors for all samples is in Table 5. Relevant bond distances, angles, and polyhedral distortion parameters are in Table 6. Mean atomic numbers of cation sites, as estimated by structure refinement and EPM, are also reported and compared in Table 7.

**Some structural features by $\Delta F$ Fourier map analysis**

At the end of the anisotropic refinement a difference ($\Delta F$) Fourier synthesis was computed. The standard deviation for the estimation of electron density (as calculated by Lipson and Cochran, 1953) for the samples under inspection ranges between 0.04 and 0.08 e/Å³. A careful examination of the final $\Delta F$ maps shows significant peaks that can result from two different causes: positions of H atoms and disorder or twinning phenomena.

**Samples M73, M14, M32**

According to Bailey (1984), the position of H is expected to be $0.90-0.95$ Å from the O4 location. The OH vector is perpendicular to the octahedral sheet and is directed toward the dirigional cavity in trioctahedral micas, whereas this vector is expected to lie in the (001) plane toward the vacant M1 octahedron in dioctahedral micas; e.g., in a neutron refinement of a phlogopite, Joswig (1972) located the H proton at $(0.098, 0.5, 0.3007)$ at $1.003$ Å from O4, with the OH vector normal to plane (001).

In both samples M73 and M14 (monzonitic complex) the most relevant $\Delta F$ peak (1.0 e/Å³ in both samples) suggests a plausible H location with atomic coordinates $(0.09, 0.5, 0.315)$ at $0.81$ Å from O4, with the OH vector almost normal to plane (001). In sample M32 (syenitic complex) the most relevant $\Delta F$ peak (0.94 e/Å³) suggests a possible H location with atomic coordinates $(0.010, 0.5, 0.315)$ at $0.97$ Å from O4, with the OH vector slightly tilted to (001) plane.

**Sample M13**

Sample M13 shows the worst refinement results: at the end of anisotropic refinement the $R$ value was 0.06 and the esd's are considerably higher than those of other samples. $\Delta F$ map shows unusual features, with a peak (1.2 e/Å³) in a position corresponding to a shift of b/3 for atom T along the b axis, and a smaller peak (0.9 e/Å³) in a position corresponding to a K-site shift of ±b/3.

A sample from the same rock type (sample M105, whose refinement is not reported since the $R$ value cannot be reduced below 0.11 in the standard $J M$ model) exhibits similar behavior with enhanced features: the $\Delta F$ map shows peaks corresponding to a complete superimposition of a 2:1 layer structure shifted by ±b/3 to the basic mica structure. The following five peaks are found: T + b/3, K + b/3 (and K - b/3 due to the m plane), O2...
TABLE 4. Crystallographic coordinates and equivalent isotropic (Å²) and anisotropic (Å² x 10⁻⁴) temperature factors for 1M biotites studied

| Sample M14 | O1 | 0.0268(8) | 0.0 | 0.1690(4) | 2.3(1) | 286(18) | 41(4) | 57(5) | 0 | 21(8) | 0 |
| Sample M32 | O1 | 0.0236(12) | 0.0 | 0.1681(6) | 2.1(2) | 172(14) | 48(6) | 29(6) | 0 | 31(3) | 0 |
| Sample M13 | O1 | 0.0241(18) | 0.0 | 0.1694(9) | 2.6(2) | 242(37) | 71(12) | 65(10) | 0 | 56(6) | 0 |
| Sample M73 | O1 | 0.0267(6) | 0.0 | 0.1687(3) | 1.7(1) | 224(13) | 35(5) | 33(5) | 0 | 16(1) | 0 |
| Sample M62 | O1 | 0.0239(14) | 0.0 | 0.1689(9) | 2.0(2) | 220(31) | 32(8) | 57(10) | 0 | 16(14) | 0 |

Note: Esd's on the last significant digit are in parentheses.

* exp[-i(hk) + · · · + 2hk] · [i^n + · · ·].

Smith and Yoder (1956) emphasized that a [310] or [310] twin axis causes two structures with a reciprocal ±b/3 shift. Bell and Wilson (1977, 1981), on the basis of TEM observations, found growth defects in metamorphic biotites with stacking modes, among which ±b/3 is present, corresponding to microtwins of a few unit cells. On the basis of energetic considerations, they suggested that the shift should occur in the octahedral layer. On the other hand, Gregorkiewicz and Rausell-Colom (1987) report a new synthetic 2:1 layer silicate with a suggested ±b/3 shift in the interlayer region between the bases of two adjacent tetrahedral layers.

In samples M13 and M105 no macroscopic twin was observed, but preliminary TEM observations (S. Bigi, personal communication) of samples from the same granite complex as M105 show a predominate 1M structure with small domains containing microtwins on one of the following axes: [310] and [310] or [110] and [110]. In samples M13 and M105 the presence of peaks in the ΔF map that are related by ±b/3 can therefore be explained as coherently diffracting small domains with a ±b/3 shift with respect to the dominant 1M matrix (Rule et al., 1987). According to this hypothesis, and referring to the "complete" set of ΔF maxima of sample M105, it should be noted that, owing to the (010) symmetry plane, no other ΔF maximum corresponding to an atomic ±b/3 shift is to be expected. The presence of these microtwins does not invalidate the substantial correctness of the crys-
TABLE 6. Selected data from structure refinements of 1M biotites

<table>
<thead>
<tr>
<th></th>
<th>M14</th>
<th>M32</th>
<th>M13</th>
<th>M73</th>
<th>M62</th>
</tr>
</thead>
<tbody>
<tr>
<td>T-O1</td>
<td>1.654(2)</td>
<td>1.665(3)</td>
<td>1.651(4)</td>
<td>1.655(1)</td>
<td>1.648(4)</td>
</tr>
<tr>
<td>T-O2</td>
<td>1.653(3)</td>
<td>1.652(5)</td>
<td>1.686(4)</td>
<td>1.659(2)</td>
<td>1.657(5)</td>
</tr>
<tr>
<td>T-O2'</td>
<td>1.656(3)</td>
<td>1.652(5)</td>
<td>1.681(6)</td>
<td>1.652(2)</td>
<td>1.657(5)</td>
</tr>
<tr>
<td>T-O3</td>
<td>1.664(3)</td>
<td>1.662(4)</td>
<td>1.674(6)</td>
<td>1.662(2)</td>
<td>1.662(5)</td>
</tr>
<tr>
<td>(T-O)</td>
<td>1.657</td>
<td>1.657</td>
<td>1.663</td>
<td>1.658</td>
<td>1.654</td>
</tr>
<tr>
<td>TQE</td>
<td>1.0003</td>
<td>1.0003</td>
<td>1.0006</td>
<td>1.0003</td>
<td>1.0002</td>
</tr>
<tr>
<td>γ (%)</td>
<td>5.66</td>
<td>6.37</td>
<td>5.72</td>
<td>5.50</td>
<td>6.31</td>
</tr>
<tr>
<td>M1-O3 (x4)</td>
<td>2.104(3)</td>
<td>2.098(5)</td>
<td>2.104(5)</td>
<td>2.105(2)</td>
<td>2.097(6)</td>
</tr>
<tr>
<td>M1-O4 (x2)</td>
<td>2.079(4)</td>
<td>2.080(7)</td>
<td>2.080(7)</td>
<td>2.081(3)</td>
<td>2.071(7)</td>
</tr>
<tr>
<td>(M1-O)</td>
<td>2.095</td>
<td>2.092</td>
<td>2.096</td>
<td>2.097</td>
<td>2.089</td>
</tr>
<tr>
<td>OQE</td>
<td>1.0114</td>
<td>1.0107</td>
<td>1.0110</td>
<td>1.0106</td>
<td>1.0103</td>
</tr>
<tr>
<td>(K-O)outer'</td>
<td>58.98</td>
<td>58.86</td>
<td>58.90</td>
<td>58.85</td>
<td>58.79</td>
</tr>
<tr>
<td>ε/ε</td>
<td>1.1073</td>
<td>1.1041</td>
<td>1.1055</td>
<td>1.1036</td>
<td>1.1024</td>
</tr>
<tr>
<td>M2-O3 (x2)</td>
<td>2.097(3)</td>
<td>2.094(5)</td>
<td>2.096(5)</td>
<td>2.100(2)</td>
<td>2.096(6)</td>
</tr>
<tr>
<td>M2-O3' (x2)</td>
<td>2.083(3)</td>
<td>2.092(4)</td>
<td>2.085(5)</td>
<td>2.084(2)</td>
<td>2.088(4)</td>
</tr>
<tr>
<td>M2-O4 (x2)</td>
<td>2.051(3)</td>
<td>2.056(6)</td>
<td>2.065(5)</td>
<td>2.059(2)</td>
<td>2.054(5)</td>
</tr>
<tr>
<td>(M2-O)</td>
<td>2.077</td>
<td>2.080</td>
<td>2.081</td>
<td>2.081</td>
<td>2.079</td>
</tr>
<tr>
<td>OQE</td>
<td>1.0099</td>
<td>1.0098</td>
<td>1.0097</td>
<td>1.0093</td>
<td>1.0096</td>
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<tr>
<td>γ (%)</td>
<td>58.66</td>
<td>58.66</td>
<td>58.66</td>
<td>58.58</td>
<td>58.62</td>
</tr>
<tr>
<td>ε/ε</td>
<td>1.0996</td>
<td>1.0992</td>
<td>1.0988</td>
<td>1.0969</td>
<td>1.0982</td>
</tr>
<tr>
<td>K-O1 (x2)</td>
<td>3.209(6)</td>
<td>3.202(6)</td>
<td>3.209(9)</td>
<td>3.209(9)</td>
<td>3.019(8)</td>
</tr>
<tr>
<td>K-O1' (x2)</td>
<td>3.207(5)</td>
<td>3.313(7)</td>
<td>3.323(7)</td>
<td>3.305(3)</td>
<td>3.318(8)</td>
</tr>
<tr>
<td>K-O2 (x4)</td>
<td>3.288(3)</td>
<td>3.317(4)</td>
<td>3.288(7)</td>
<td>3.305(3)</td>
<td>3.298(6)</td>
</tr>
<tr>
<td>K-O2' (x2)</td>
<td>3.041(3)</td>
<td>3.029(5)</td>
<td>3.028(6)</td>
<td>3.041(2)</td>
<td>3.020(6)</td>
</tr>
<tr>
<td>(K-O)inner</td>
<td>3.037</td>
<td>3.026</td>
<td>3.029</td>
<td>3.037</td>
<td>3.020</td>
</tr>
<tr>
<td>(K-O)outer</td>
<td>3.294</td>
<td>3.316</td>
<td>3.308</td>
<td>3.292</td>
<td>3.306</td>
</tr>
<tr>
<td>Δ(K-O)</td>
<td>0.257</td>
<td>0.290</td>
<td>0.273</td>
<td>0.255</td>
<td>0.286</td>
</tr>
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</table>

Note: Entries in column 1 are bond distances (Å); TQE, OQE (after Robinson et al., 1971); octahedral flattening angles γ and tetrahedral rotation angle α (after Hazen and Burnham, 1973); ε/ε (after Toraya, 1981). Esd's on the last significant digit are in parentheses.

The number of electrons associated with each cation site, as calculated by EPMA, corresponds well with that calculated by X-ray refinement. The agreement is not as good for sample M13; the above discussion on microtwins related to ±b/3 shifts could suggest the presence of microdomains with a slightly different composition in the sample.

The discussion of thermal factors is sometimes neglected in crystal chemical works because many authors think they only incorporate the errors of data collection and structure refinement. Even if this statement is largely true, some useful auxiliary information can, nevertheless, be deduced from their analysis. Reference should be made.

TABLE 7. Mean atomic number of octahedral and interlayer sites as determined by structure refinement and microprobe analysis for 1M biotites studied

<table>
<thead>
<tr>
<th></th>
<th>M14</th>
<th>M32</th>
<th>M13</th>
<th>M73</th>
<th>M62</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1+</td>
<td>18.61(8)</td>
<td>17.9(1)</td>
<td>20.4(1)</td>
<td>18.9(6)</td>
<td>20.4(1)</td>
</tr>
<tr>
<td>M2+</td>
<td>17.8(1)</td>
<td>17.1(2)</td>
<td>19.8(2)</td>
<td>18.2(1)</td>
<td>19.6(2)</td>
</tr>
<tr>
<td>K+</td>
<td>18.66(6)</td>
<td>18.8(1)</td>
<td>18.5(1)</td>
<td>18.9(2)</td>
<td>19.4(1)</td>
</tr>
<tr>
<td>(M1 + M2)+</td>
<td>54.2</td>
<td>52.1</td>
<td>60.0</td>
<td>55.4</td>
<td>59.8</td>
</tr>
<tr>
<td>(M1 + M2)+</td>
<td>54.7</td>
<td>52.7</td>
<td>55.2</td>
<td>54.2</td>
<td>57.1</td>
</tr>
<tr>
<td>K+</td>
<td>17.3</td>
<td>17.7</td>
<td>19.0</td>
<td>17.4</td>
<td>18.0</td>
</tr>
</tbody>
</table>

Note: Esd's on the last significant digit are in parentheses.

x X-ray refinement.
 Electron-microprobe analysis.
 Electron-microprobe analysis.
 (2 × M2) + M1.
 Sum of octahedral-cation electrons.
however, only to their relative and not their absolute values.

In all the samples, thermal factors are quite high, probably due to layer disorder, but they do not show distinct anisotropies. They are also remarkably consistent with the crystal-chemical nature of the respective sites (Vainshtein, 1981, p. 233; Stout and Jensen, 1968, p. 206): the tetrahedral atoms (T) show the lowest $B_{eq}$, K the greatest, and the M1 and M2 atoms have $B_{eq}$ just slightly higher than those of the tetrahedral sites, in accordance with the stronger or weaker bonds affecting each site (Table 4). Of the oxygens, the O1 and O2 basal pair, which coordinate tetrahedral and interlayer atoms, exhibit higher thermal factors than the O3 and O4 pair, which coordinate the tetrahedral and octahedral atoms. This suggests that the atomic position of the former is less well defined than that of the latter (see discussion on $\psi$ and $\alpha$ below).

**Octahedral layer**

The parameters we used to measure octahedral distortions are (1) $e_u/e_h$ (Donnay et al., 1964; formula as in Hazen and Burnham, 1973)—$\psi$ is the octahedral flattening angle; (2) $e_u/e_h$ (Toraya, 1981)—$e_u$ and $e_h$ are the mean lengths of unshared and shared octahedral edges, respectively, and their ratio measures the distortion that each octahedron undergoes by being inserted into layers with shared edges; and (3) OQE (Robinson et al., 1971)—octahedral quadratic elongation, a distortion parameter widely used for chain-silicate minerals (e.g., Rossi et al., 1983; Rossi, 1987; Davoli, 1987).

In order to study the variation of geometric parameters in the phlogopite-annite series, of which the studied samples are intermediate in chemistry, we examined data reported in the literature (Fig. 1). Toraya (1981) showed an excellent correlation between $e_u/e_h$ and $\psi$ for IM end-member silicate and germanate micas. This correlation exists also for the intermediate samples examined, as shown in Figure 1a (regression equation: $e_u/e_h = -0.4276 + (2.603 \times 10^{-3})\psi$; $r = 0.999$, in accordance with Toraya, 1981). In Figure 1b, OQE is plotted against $\psi$ and shows a trend similar to that in 1a, although with a slightly lower correlation (regression equation: OQE = $0.660 + (5.96 \times 10^{-3})\psi$; $r = 0.982$).

Figure 2 shows the OQE distortion trend versus the mean distance $\langle M-O \rangle$ in M1 and M2, respectively.

Figure 3 plots the graph $\Delta(M-O) = (\langle M1-O \rangle - \langle M2-O \rangle)$ against $\Delta(e_u/e_h) = (e_u/e_h)_{M1} - (e_u/e_h)_{M2}$ (regression equation: $\Delta(e_u/e_h) = 0.42\Delta(M-O)$; $r = 0.998$).

Figure 1 shows that the octahedral-sheet distortion is similar in both M1 and M2. As the Fe content increases, the average distortion of the layer decreases and the two octahedra become more distinct: M1 is more distorted and larger than M2 (Fig. 2). The number of electrons associated with site M1 is slightly higher than that associated with M2 (Table 7), thereby suggesting a slight pref-
ereference of Fe$^{2+}$ for M1, in accordance with the observation of Bohlen et al. (1980) for a $2M_1$ polytype biotite.

Figure 2 clearly shows the difference in the rate of decrease of the OQE distortion in the two octahedra as a result of an increase in the average M-O distances. This difference between M1 and M2 is also evident in Figure 3, where the effect of a difference in the octahedra distortion $\Delta(e'/e)$ resulting from size differences $\Delta(M-O)$ is shown. The correlation is high ($r = 0.998$). Phlogopites, biotites, and annites are found in fairly well-defined fields.

Some observations can be made about structural details of the octahedral layer. First, in annite (sample 2) the two octahedra have a similar composition but different topology (size and distortion) (Figs. 1, 2). The converse can be observed in Figures 1 and 3 where it is shown that the biotite samples with small amounts of small, highly charged octahedral cations (Al, Ti$^{4+}$, Fe$^{3+}$) behave like those with large amounts (and therefore a different composition) and therefore fall on the same linear trends. Finally, chain silicates with less closely packed octahedral structures exhibit geometrical distortions in contrast with those observed in this study for M1 and M2 in biotites, showing octahedra with distortions that vary inversely with the size of occupying cation (Ghose et al., 1986; Davoli, 1987; Rossi, 1987). These observations suggest that the structural topology in trioctahedral micas is influenced not only by composition but also by the constraints of closest packing within the layer and the confinement of the octahedron between opposite tetrahedral sheets (see also Weiss et al., 1985; Lin and Guggenheim, 1983).

Fig. 3. $\Delta(e'/e) = (e'/e)_M1 - (e'/e)_M2$ vs. $\Delta(M-O) = ((M1-O) - (M2-O))$. Samples as in Fig. 1.

Fig. 4. $(M-O)$ (in Å) distance vs. mean $(T-O)$ (in Å) distance for M1 and M2 octahedra. Symbols and samples as in Fig. 1. Vertical lines: phlogopite field; horizontal lines: biotite and aninite field.

**Tetrahedral layer and interlayer**

The tetrahedral geometrical parameters we used are (1) $\alpha$ (Newnham and Brindley, 1956; formula as in Hazen and Burnham, 1973)—the tetrahedral rotation angle and (2) TQE (Robinson et al., 1971)—the tetrahedral quadratic elongation, similar to OQE.

The tetrahedra in the biotites analyzed are very regular, as indicated by the tetrahedral distortion parameter (TQE) with values between 1.0003 and 1.0005. These values are similar to those of phlogopites and annites reported elsewhere. The tetrahedral distortion is not affected by the octahedral composition.

Figure 4 gives the mean distance $(T-O)$ versus $(M-O)$ and $(M2-O)$ and shows two fields for phlogopites and biotites; the former fall into the field $(T-O)$ and $(M-O)$ less than 1.655 Å and 2.067 Å respectively, the latter into a field of higher values. The difference in the mean $(T-O)$ distance reported in Figure 4 does not seem to be due solely to slight differences in the amount of tetrahedral Al (viz. the data reported in Table 2 and the literature quoted in the caption to Fig. 1). Thus, an increase in the $(T-O)$ dimension seems to be linked to an increase in $(M-O)$, although only qualitatively.

Various authors (e.g., Toraya, 1981; Takeda and Morosin, 1975; Hazen and Burnham, 1973) have suggested a close relationship between the tetrahedral ring rotation angle, $\alpha$, with both the flattening angle, $\psi$, and the composition of the octahedral sheet. Figure 5, however, shows that a significant correlation between $\psi$ and $\alpha$ does not exist. This is not surprising. First, the greater thermal parameters of basal oxygens O1 and O2 as compared with octahedral oxygens O3 and O4 (see above) suggest that, because of the less close and rigid packing of the tetrahedral layer, O1 and O2 have less well-defined atomic positions than O3 and O4, and the parameter $\alpha$ would
therefore be more affected than the parameter \( \psi \) (or \( e'/e_0 \)). Secondly, it can be seen that \( \alpha \) does not distinguish crystals with different octahedral compositions, such as phlogopites (\( \alpha = 5.7-7.7 \), samples 1, 4–7) and biotites (\( \alpha = 5.5-7.5 \), samples 3, M32, M73, M14, M13, M62).

As a consequence, a statistical regression analysis between \( \alpha \) and the main octahedral geometric parameters does not show a correlation, and angle \( \alpha \), therefore, appears to be less significant in describing structural modifications linked with the chemistry of the crystal than \( \psi \) (or \( e'/e' \)) (Figs. 1 and 3).

Angle \( \alpha \) is, however, linked to the geometry of the trigonal cavity occupied by the interlayer cation. Since \( \Delta(K-O) \) is the difference between mean distance K-O outer and K-O inner, a good positive correlation with \( \alpha \) is found (regression equation \( \Delta(K-O) = (-4.29 \times 10^{-3}) + (4.62 \times 10^{-3}) \alpha; r = 0.997 \)). Phlogopites and biotites are not found in distinct fields, confirming the poor relationship between \( \alpha \) and the octahedral chemical composition.

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