

1 **Revision 2**

2 **S₂⁻ and S₃⁻ radicals and the S₄²⁻ polysulfide ion in lazurite, haüyne and synthetic**
3 **ultramarine blue revealed by resonance Raman spectroscopy**

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14
15 **Abstract**

16
17 Taking advantage of the Raman resonance effect, we employed 405 and 532 nm excitations to 1)
18 identify sulfur species present in lazurite, haüyne, and synthetic ultramarine blue pigments and 2)
19 investigate the enigmatic ~485 cm⁻¹ band found previously in Raman spectra of lazurite and
20 haüyne collected with 458 nm excitation. In spectra of lazurite and haüyne, bands of the sulfate
21 ion and S₂⁻ and S₃⁻ radicals can be seen. Spectra collected using 405 nm excitation show the
22 enhancement of intensity of ν₁(S₂⁻) band and its nν₁ (n≤7) progression. Spectra collected using
23 532 nm incident light show the enhancement of intensity of ν₁(S₃⁻), ν₂(S₃⁻), and ν₃(S₃⁻) bands

24 and the ν_1 ($n \leq 9$) and $\nu_2 + \nu_1$ progressions of the $\nu_1(\text{S}_3^-)$ band. In spectra collected with 405 nm
25 excitation, we also found features that we ascribe to the S_4^{2-} polysulfide ion. These include the ν_1
26 symmetric S–S stretching band at $\sim 481 \text{ cm}^{-1}$, the ν_2 symmetric S–S stretching band at $\sim 443 \text{ cm}^{-1}$
27 (only present in spectra of some lazurite samples), the ν_3 symmetric S–S bending at 223 cm^{-1} and
28 the ν_1 ($n \leq 5$) and $\nu_1 + \nu_3$ progressions of the $\nu_1(\text{S}_4^{2-})$ band. We observed that under laser beam,
29 the S_4^{2-} polysulfide ion rapidly decomposes to two S_2^- radicals in lazurite, while it remains stable
30 in haüyne. In spectra of synthetic ultramarine blue pigments, only features of S_2^- and S_3^- radicals
31 were observed. Finally, we verified the identity of the polysulfide ions with *ab initio* molecular
32 dynamics calculations. We conclude that Raman resonance spectroscopy is a powerful
33 qualitative method to detect polysulfide and sulfur radical species with concentrations below the
34 detection limit of conventional analytical techniques. Owing to the high stability of S_4^{2-} in
35 haüyne, this mineral structure appears promising as a host material for S_4^{2-} entrapment, making it
36 potentially useful for applications in optoelectronics.

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Keywords

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40 Haüyne, lapis lazuli, lazurite, molecular dynamics, resonance Raman spectroscopy, sodalite
41 group, sulfur radical, ultramarine blue pigment

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Introduction

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45 Sodalite group minerals, including lazurite $\text{Na}_7\text{Ca}(\text{Al}_6\text{Si}_6\text{O}_{24})(\text{SO}_4)^{2-}(\text{S}_3)^-\cdot\text{H}_2\text{O}$ (Sapozhnikov
46 2021) and haüyne $\text{Na}_{4.5}\text{Ca}_2\text{K}[\text{Al}_6\text{Si}_6\text{O}_{24}](\text{SO}_4)_{1.5}(\text{OH})_{0.5}$ (Hassan and Grundy 1991), are members

47 of the feldspathoid family. Feldspathoids share an aluminosilicate framework consisting of six-
48 membered rings of Si- and Al-centered tetrahedra. The sodalite group is characterized by
49 sodalite-type (ABC) stacking sequence of aluminosilicate layers and the presence of sodalite (β)
50 cages that can accommodate a variety of cations, anions, and neutral molecules (Sapozhnikov
51 2021), including a number of sulfur species (Table 1). Of these, the S_3^- and S_2^- radicals deserve
52 special attention for two reasons. First, the sodalite cage is one of the few environments in which
53 these sulfur species can be stabilized at ambient temperature. In geologic fluids, for instance,
54 sulfur radicals become stable only around 200 °C (Pokrovski and Dubrovinsky 2011). Second,
55 sulfur radicals are chromophores. Whereas the S_3^- radical is a blue chromophore (Chivers 1974)
56 that made lapis lazuli a highly prized gemstone of the Sumerian and Egyptian antiquity (Gaetani
57 et al. 2004) and the ultramarine blue made from lazurite a desired pigment in both Asia and
58 Europe since the 7th–8th century AD (Gettens 1938)(Gaetani et al. 2004), the S_2^- radical is a
59 yellow chromophore and the increasing S_2^-/S_3^- ratio was found to be responsible for greenish
60 shades and eventually green color of ultramarine pigments (Clark and Cobbold 1978)(Reinen
61 and Lindner 1999). Just like lazurite, blue crystals of haüyne also owe their color to S_3^- radicals
62 (Caggiani et al. 2022).

63 Given that the identification of sulfur radicals may be hindered by their low
64 concentrations, we decided to employ Raman spectroscopy in the search for sulfur bearing
65 species and take advantage of the rigorous Raman resonance effect shown by sulfur radicals
66 (Clark and Franks 1975)(Clark and Cobbold 1978)(Clark and Dines 1986)(Picquenard et al.
67 1993). Furthermore, we investigated the enigmatic $\sim 485\text{ cm}^{-1}$ band found previously in Raman
68 spectra of lazurite and haüyne collected with a 458 nm excitation, which was invisible in spectra

69 collected with a 532 nm excitation and was suggested to be related to the ν_1 band of S_2^- radical
 70 (Caggiani et al. 2014).

Locality	Sulfur species	Analytical method	Reference
<i>Lazurite</i>			
Afghanistan Baffin Island, Nunavut, Canada	Sulfate SO_4^{2-} Monosulfide S^{2-}	XRD	(Hassan et al. 1985)
Pamir, Tajikistan	Sulfate SO_4^{2-} S_3^- radical S_2^- radical	Raman, UV-Vis, IR, EPR	(Ostroumov et al. 2002)
Afghanistan Baffin Island, Nunavut, Canada	Sulfate SO_4^{2-} (ma) Monosulfide S^{2-} bound to Na (mi) Elemental sulfur S (mi) Polysulfide (mi)	XANES, XPS	(Fleet et al. 2005)
Malo-Bystrinskoe Deposit, Lake Baikal Region, Russia	Sulfate SO_4^{2-} (ma) Polysulfide (ma) Sulfite SO_3^- (mi) Monosulfide S^{2-} (mi) Thiosulfate $S_2O_3^-$ (mi) Elemental sulfur S (mi)	XANES, XP	(Tauson et al. 2012)
Badakhshan, Afghanistan	Sulfate SO_4^{2-} S_3^- radical S_2^- radical	Raman	(Caggiani et al. 2014)
Many localities	Sulfate SO_4^{2-} S_3^- and/or S_2^- radical S_2^- radical	XANES	(Gambardella et al. 2016)
Malo-Bystrinskoe Deposit, Lake Baikal Region, Russia	Sulfate SO_4^{2-} (ma) S_3^- radical (ma) Monosulfide S^{2-} (mi, not detected directly)	IR, Raman, EPR, XPS	(Sapozhnikov 2021)
<i>Haüyne</i>			
Sacrafano, Italy	Sulfate SO_4^{2-}	XRD	(Hassan and Grundy 1991)
Toppo San Paolo, Italy Near Mount Vulture volcano, Italy	Sulfate SO_4^{2-} S_3^- radical S_2^- radical	Raman	(Caggiani et al. 2014)
Toppo San Paolo, Italy Melfi, Italy	Sulfate SO_4^{2-} S_3^- radical S_2^- radical	Raman	(Caggiani et al. 2022)

71 Table 1. Sulfur species in lazurite and haüyne. ma = major phase, mi = minor phase, EPR =
 72 electron paramagnetic resonance spectroscopy, IR = Infrared spectroscopy, UV-Vis =
 73 Ultraviolet-visible spectroscopy, XANES = X-ray absorption near-edge structure, XPS = X-ray
 74 photoelectron spectroscopy, XRD = X-ray diffraction.

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76 Methods

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78 Samples

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80 Raman spectra were collected on naturally occurring lazurite and haüyne samples provided by
 81 the Natural History Museum, Geneva, Switzerland, and ultramarine blue pigments purchased
 82 from Kremer Pigmente, Germany. The origin of lazurites is as follows: specimen number

83 003.084 Baikal, Russia; 376.002 Tunnel Mt Cenis, Savoie, France; 397.041 Badakhstan, Kabul,
84 Afghanistan; 425.086 Brazil; and 431.065 Sierra d'Ovalle, Coquimbo, Chile. The origin of
85 haüynes is as follows: 333.049 Mount Vesuvius, Italy and 332.018 Laachersee, Eifel, Germany.
86 The pigments analyzed were: 45000 Ultramarine blue, very dark; 45010 Ultramarine blue, dark;
87 45020 Ultramarine blue, reddish; 45030 Ultramarine blue, greenish extra; 45040 Ultramarine
88 blue, greenish light; and 45080 Ultramarine blue, light.

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90 **Diffuse reflectance spectroscopy**

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92 Diffuse reflectance spectra were collected using a UV-visible spectrometer (V-670, JASCO)
93 coupled with an integrating sphere accessory (ARSN-733, JASCO) at the Department of
94 Physical Chemistry, University of Geneva. Each mineral powder sample was mixed with KBr
95 (ca. 1 wt% of a sample in KBr) for the preparation of a 13 mm circular pellet (Specac hydraulic
96 press was used). The pellet was then mounted on the sample holder of the integrated sphere and
97 the diffuse reflectance spectra were measured. Blank KBr pellet was used for obtaining the
98 background spectrum. The measured reflectance (R) was converted to absorbance (A) by
99 calculating $A = -\log R$.

100

101 **Raman spectroscopy**

102

103 Raman spectra collected with 405 and 532 nm excitations were acquired using a confocal
104 LabRAM HR Evolution (HORIBA Scientific) Raman spectrometer with 800 mm focal length at

105 the Department of Earth Sciences, University of Geneva. To emphasise the enhancement of S_2^-
106 and S_3^- bands due to the resonance effect, spectra were also collected with a 785 nm excitation
107 using a Renishaw inVia Raman spectrometer with 250 mm focal length at the Natural History
108 Museum of Geneva. However, the interpretation of previously observed spectral features of
109 lazurite in spectra collected with a 785 nm excitation (e.g., González-Cabrera et al. 2022) is
110 beyond the scope of the current study. Both spectrometers were calibrated using the 521 cm^{-1}
111 line of silicon.

112 The LabRAM spectrometer was equipped with a liquid nitrogen cooled, back illuminated
113 Symphony II CCD detector (1024×256 pixel) and an Olympus BXF_M microscope with a
114 motorized XYZ sample stage. The spectral resolution was $\sim 0.5\text{ cm}^{-1}$. A grating of 1800
115 lines/mm and a confocal pinhole of 100 μm were employed. A TopMode 405 laser source
116 (Toptica Photonics) with a wavelength of 405 nm and a Torus 532 laser source (Laser Quantum)
117 with a wavelength of 532 nm were used for excitation. The spectra were acquired in
118 backscattering geometry using either an Olympus MPlan N 100× objective with numerical
119 aperture of 0.90 and working distance of 0.21 mm (for lazurites and pigments) or an Olympus
120 LMPlanFL N 50× long working distance objective with numerical aperture of 0.50 and working
121 distance of 10.6 mm (for haüynes).

122 The Renishaw spectrometer was equipped with a Peltier cooled CCD detector (400×576
123 pixel) and a DM Leica 2500 microscope with a motorized XYZ sample stage. The spectral
124 resolution was $\sim 1.5\text{ cm}^{-1}$. A grating of 1200 lines/mm and a slit of 65 μm were employed. A
125 HPNIR785 diode laser source (Renishaw) with a wavelength of 785 nm was used for excitation.
126 The spectra were acquired in backscattering geometry using a Leica 50× long working distance
127 objective with numerical aperture of 0.55 and working distance of 8 mm.

128 For each spectrum collected with the 405 nm and 532 nm lasers, three accumulations of
129 10 s each were taken in multiple spectral windows resulting in a final range of 150–5000 cm^{-1} . In
130 addition, spectra with ten accumulations of 10 s each were taken in the spectral window of 400–
131 700 cm^{-1} . To prevent the saturation of the CCD detector while collecting spectra of lazurites and
132 to prevent the burning of pigments, a power filter of 10% was also applied for these
133 measurements, reducing the maximum power of ~ 30 mW measured at the sample to ~ 3 mW.

134 For each spectrum collected with the 785 nm laser, ten accumulations of 10 s each were
135 taken in the spectral window of 400–1200 cm^{-1} . To prevent the saturation of the CCD detector,
136 power filters of 1, 5, or 10% were applied for the measurement of lazurites and haüynes and to
137 prevent the burning of samples, a power filter of 0.1% was applied for the measurement of
138 pigments, significantly reducing the maximum power of ~ 300 mW measured at the sample.

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140 ***Ab initio* molecular dynamics**

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142 Molecular dynamics simulations were performed using the VASP package (Kresse and
143 Hafner 1993)(Kresse and Joubert 1999). The interatomic forces were computed using the planar
144 augmented wavefunction method (Blöchl 1994). The generalized gradient approximation
145 (Perdew et al. 1996) was used to describe the exchange correlation term of the energy. The
146 electronic density and wavefunctions were computed using the sampling of the reciprocal space
147 in the Γ point. The simulations were run for at least 30 picoseconds with a time step of 1
148 femtosecond.

149 The analysis of the simulations was completed using the UMD package (Caracas et al.
150 2021a, 2021b). The geometry of the S–S bonds was monitored computing the pair distribution

151 functions (PDFs). The first minimum of the PDFs yields the maximum bond distance and in a
152 fluid description corresponds to the radius of the first coordination sphere. This distance was
153 used to assess the speciation within the polysulfide ions. The vibrational spectra were obtained as
154 the Fourier transform of the self-correlation function of the atomic velocities.

155

156

Results and discussion

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158 Raman resonance means that when a molecule is excited with a laser with a frequency close to
159 the maximum of an allowed electronic transition, the Raman spectra are characterized by an
160 enhancement in the intensity of a totally symmetric fundamental of the scattering molecule and
161 by high-intensity overtone progressions in this fundamental (Holzer et al. 1970)(Nafie et al.
162 1971)(Clark and Franks 1975). Whereas the S_3^- radical shows a broad absorption band with a
163 maximum around 610-620 nm due to the $X^2B_1 \rightarrow C^2A_2$ transition (Chivers and Drummond
164 1972)(Seel et al. 1977)(Clark and Cobbold 1978)(Reinen and Lindner 1999)(Linguerrri et al.
165 2008)(Shnitko et al. 2008), the S_2^- radical shows an absorption band with a maximum around
166 390-400 nm due to the $^2\Pi_g \rightarrow ^2\Pi_u$ transition (Figure 1)(Holzer et al. 1969)(Clark and Cobbold
167 1978). Therefore, we employed 405 nm excitation that lies inside the absorbance band of the S_2^-
168 radical, 532 nm excitation that lies inside the absorbance band of the S_3^- radical, and 785 nm
169 excitation that lies outside the absorbance bands of either radicals (Figure 1) to collect Raman
170 spectra of five lazurites, two haüynes, and six synthetic ultramarine blue pigments to identify the
171 sulfur species present in each (see Supplementary material). Representative spectra of these are
172 shown in Figures 2, 3, and 4, respectively. In the following section, the observed bands of sulfur
173 species are discussed.

174 *Sulfate bands.* The $\nu_1(\text{SO}_4^{2-})$ bands in the 976 – 1003 cm^{-1} region, corresponding to the
175 S–O stretching mode (Choi and Lockwood 1989), are visible in most lazurite and haüyne spectra
176 (Figures 2 and 3), whereas the $\nu_2(\text{SO}_4^{2-})$ band at 437 cm^{-1} , corresponding to the S–O bending
177 mode (Choi and Lockwood 1989) is only visible in the spectra of haüyne (Figure 3). In haüyne
178 spectra, up to three bands appear in the sulfate region, likely representing different coordination
179 environments in the sodalite (β) cages. In a recent study, five bands related to the silicate and
180 sulfate groups have been documented in the 950-1030 cm^{-1} spectral region in haüyne originating
181 from the Mount Vulture area in Italy (Caggiani et al. 2022). Sulfate bands are absent in spectra
182 of ultramarine blues.

183 *S₃⁻ bands.* The $\nu_1(\text{S}_3^-)$ band at ~546 cm^{-1} , corresponding to the symmetric S–S stretching
184 mode (Holzer et al. 1969)(Chivers and Drummond 1972)(Clark and Franks 1975), is visible in
185 all lazurite, haüyne, and ultramarine blue spectra. Given that the 532 nm excitation line lies
186 inside the absorbance band of the S₃⁻ radical (Figure 1), spectra collected with the 532 nm
187 excitation show a strong enhancement of the intensity of the $\nu_1(\text{S}_3^-)$ band, the $\nu_2(\text{S}_3^-)$ band at
188 ~258 cm^{-1} , corresponding to the symmetric S–S bending mode (Chivers and Drummond
189 1972)(Clark and Franks 1975), and the $\nu_3(\text{S}_3^-)$ band at ~582 cm^{-1} , corresponding to the anti-
190 symmetric S–S stretching mode (Figures 2, 3, and 4)(Table 2)(Ledé et al. 2007). The 532 nm
191 spectra also show $n\nu_1$ and $\nu_2 + n\nu_1$ progressions of the $\nu_1(\text{S}_3^-)$ band (Figures 2, 3, and 4)(Table 2).

192 *S₂⁻ bands.* The position of the $\nu_1(\text{S}_2^-)$ band, corresponding to the symmetric S–S
193 stretching mode (Holzer et al. 1969)(Clark and Franks 1975), coincides with that of the $\nu_3(\text{S}_3^-)$
194 band (Ledé et al. 2007). Given that the concentration of S₃⁻ in the studied materials is high
195 enough that its spectral features are visible even in the non-resonant Raman spectra (i.e., those
196 collected with 405 and 785 nm excitations), a small portion of the ~582 cm^{-1} spectral feature in

197 spectra collected with the 405 nm excitation, correspond to the $\nu_3(\text{S}_3^-)$ band. The dominant
198 contribution of the $\sim 582\text{ cm}^{-1}$ spectral feature is the $\nu_1(\text{S}_2^-)$ band, because the 405 nm excitation
199 line lies inside the absorbance band of the S_2^- radical. The 405 nm spectra of lazurites, haüynes,
200 and ultramarine blues indeed show a greatly enhanced $\nu_1(\text{S}_2^-)$ band and its $n\nu_1$ progression
201 (Figures 2, 3, and 4)(Table 2).

202 *The 481, 443, and 223 cm^{-1} bands.* Bands at 481 and 223 cm^{-1} , along with the
203 progressions of the 481 cm^{-1} band appear in four of the five lazurite spectra and in one of the two
204 haüyne spectra collected with the 405 nm excitation (Figures 2 and 3)(Table 2). In addition, a
205 band at 443 cm^{-1} is visible in the spectrum of lazurite from Brazil (Figure 2)(Table 2). These
206 bands are absent in spectra of ultramarine blues (Figure 4). This observation is consistent with
207 earlier studies in which no $\sim 480\text{ cm}^{-1}$ band has been observed in spectra of synthetic pigments
208 collected with a 405 nm laser (Del Federico et al. 2006). The 481 cm^{-1} band has already been
209 reported in spectra of lazurite and haüyne collected with a 458 nm excitation, but was absent in
210 spectra collected with a 532 nm laser and has not been assigned to any species (Caggiani et al.
211 2014). These previous observations are consistent with ours and suggest that another
212 chromophore species with an absorption maximum in/near the 400-450 nm region is responsible
213 for the 481 and 223 cm^{-1} bands. In all lazurite samples, upon subsequent spectra acquisitions
214 from the same irradiated volume, the 481 and 223 cm^{-1} bands and the progression of the 481 cm^{-1}
215 ν_1 band rapidly lose intensity (Figures 5 and 6). Simultaneously, the area of $\nu_1(\text{S}_2^-)$ band and its
216 progression gradually increases (Figures 5 and 6). The breakdown of the 481 and 223 cm^{-1} bands
217 can be further accelerated with increasing laser power as shown in time profiles employing filters
218 that reduce the maximum power to 5, 10, 25, and 50% (Figure 7).

219

220 Our observations indicate a laser-induced reaction of a S-bearing species to S_2^- . Indeed,
221 visible light of suitable wavelengths can lead to the breakage of S–S bonds in polysulfur
222 compounds (Steudel and Chivers 2019). The S-bearing species in question has its strongest
223 Raman bands at 481 and 223 cm^{-1} , an absorption maximum in/near the 400–450 nm region, must
224 contain at least three sulfur atoms to exhibit two Raman bands and must not contain more than
225 six sulfur atoms to fit the sodalite (β) cages of lazurite and haiüyne. The S_4^{2-} polysulfide ion
226 fulfills all these criteria: its ν_1 symmetric S–S stretching vibration is at 480 cm^{-1} (Janz et al.
227 1976)(Chivers and Lau 1982), its absorption maximum is at ~420–430 nm (Martin et al.
228 1973)(Badoz-Lambling et al. 1976) and is small enough to be accommodated in the β cages.
229 Furthermore, the Raman-active vibrational frequencies calculated by Tossell (2012) at the cc-
230 pVTZ CCSD PCM level for S_4^{2-} (482 cm^{-1} for the strongest, 228, 449, and 504 cm^{-1}), are in
231 close agreement with those observed by us. The laser-induced decomposition of S_4^{2-} likely
232 produces S_2^- according to the reaction:



234 Indeed, the dissociation of polysulfides to sulfur radicals upon heating or the dimerization of
235 sulfur radicals upon cooling have been observed previously in dissolution experiments of alkali
236 polysulfides (Giggenbach 1968)(Seel et al. 1977). Moreover, S_4^{2-} has already been successfully
237 trapped in synthetic sodalite structure materials (Ruivo et al. 2018)(Lim et al. 2018). Finally, S_4^{2-}
238 has been suggested as a species contributing to an envelope of peaks between 2470 and 2475 eV
239 in the XANES spectra of lazurite (Gambardella et al. 2016). In contrast to lazurite, the ν_1 band of
240 S_4^{2-} in haiüyne is only slightly affected by the laser beam, even when using full laser power
241 (Figure 8). Moreover, there is no growth of the ν_1 band of S_2^- observed that would indicate the
242 decomposition of S_4^{2-} . S_4^{2-} is therefore much more stable in haiüyne than lazurite.

243 *Ab initio molecular dynamics*. To confirm the nature and stability of the polysulfide ions
244 trapped in the sodalite (β) cages of lazurite, we ran a series of *ab initio* molecular dynamics
245 simulations at 300 K. Lazurite host minerals were modeled using a cubic model host with
246 $[\text{Na}_8\text{Al}_6\text{Si}_6\text{O}_{12}]^{2+}$ stoichiometry within either one unit cell or a 2x2x2 supercell. The S_3^{2-} , S_4^{2-}
247 and S_6^{2-} polysulfide groups were placed inside the large cages of the model lazurite in linear
248 geometry parallel to the diagonals of the cube. Using the first minimum of the PDFs (Figure 9)
249 as the criterion for bonding, the simulations show the large remarkable stability of the S_3^{2-} linear
250 group. In the S_3^{2-} bearing cells, the linear group dominates the sulfur speciation by up to 80%,
251 and the rest of the time it is split into an S_2 group and one isolated S atom. But the lifetime of the
252 isolated $\text{S}_2 + \text{S}$ configuration is less than 30 femtoseconds. In the S_4^{2-} bearing cells, the complete
253 linear group represents about 6% of the total sulfur population and the rest of the time it is split
254 into two S_2 molecules. Finally, the S_6^{2-} polysulfide group is split into two S_3 linear groups for the
255 entire duration of the simulation. The vibrational analysis reveals peaks corresponding to the S_2
256 and S_3 groups, but fails to find any peak corresponding to the S_4^{2-} peak. This is due to the low
257 concentration of the S_4 linear group, which is not enough to leave a signature in the total
258 vibrational spectrum. The actual positions of the S_2 and S_3 peaks are highly dependent on the
259 density of the simulated material and they appear shifted with respect to experiments. Only the
260 relative S_2/S_3 positions are consistent with experiments.

261 Simulations that started with tetrahedral S_4^{2-} groups saw their immediate dissociation in
262 two S_2 molecules. The same phenomenon appeared in simulations of Na_2S_4 , or CaS_4 . Moreover,
263 if the density of these systems is too low, the DFT simulations tend to dissociate the molecules
264 and transform them into an amorphous phase, similar to a gas.

265 *Geometry of the S₄²⁻ polysulfide ion and the assignment of observed bands.* The S₄²⁻
 266 polysulfide ion may exist in several geometries, including chain (Tegman 1973), ring (Mealli et
 267 al. 2008)(Poduska et al. 2009), and branched geometry (Lim et al. 2018). An example of a chain
 268 geometry is solid Na₂S₄ (Tegman 1973) that has two symmetric stretching modes: a ν_1
 269 symmetric S–S stretching vibration, involving a terminal S atom at 482 cm⁻¹ and a ν_2 symmetric
 270 S–S stretching vibration involving two central S atoms at 445 cm⁻¹ (Janz et al. 1976). While in
 271 the lazurite from Brazil there is a prominent shoulder present at ~443 cm⁻¹ that may be
 272 associated with the ν_2 symmetric S–S stretching vibration, no ~445 cm⁻¹ shoulder is present in
 273 the lazurite from Russia (Figure 6). The absence of the ν_2 symmetric S–S stretching vibration in
 274 the lazurite from Russia may indicate the presence of S₄²⁻ rings rather than linear S₄²⁻ units, in
 275 which all S–S bonds are equivalent leading to only one symmetric S–S stretching vibration. MD
 276 simulation indicates the preference of S₄²⁻ to form linear units rather than rings and therefore we
 277 propose a chain geometry of S₄²⁻ polysulfide ion in the cage, and follow the assignment of
 278 vibrational modes proposed by Janz et al. (1976)(Table 2). However, we do not discard the
 279 possibility of the existence of S₄²⁻ rings in the sodalite (β) cages of lazurite and haüyne.

280 *Other S-bearing species.* Several additional bands appear in the 230-280 cm⁻¹ and 600-
 281 650 cm⁻¹ regions of certain lazurite and haüyne spectra that may be associated with other S-
 282 bearing species. However, the assignment of these is not trivial and is beyond the scope of this
 283 study.

284

Vibrational mode	Sample												Reference for assignment
	Lazurite (Russia)			Lazurite (Brazil)			Haüyne (Italy)			Synthetic ultramarine blue			
	Laser wavelength (nm)												
	405	532	785	405	532	785	405	532	785	405	532	785	
	S ₄ ²⁻												
ν_1 symmetric S–S stretching	582			581			586			583			(Holzer et al. 1969)
2 ν_1 overtone	1163			1162			1171			1164			(Holzer et al. 1969)
3 ν_1 overtone	1740			1739						1736			(Holzer et al. 1969)
4 ν_1 overtone	2314			2313						2310			(Clark and Franks 1975)
5 ν_1 overtone	2882			2879						2879			
6 ν_1 overtone	3448			3447						3445			
7 ν_1 overtone										3967			

8v1 overtone													4516		
S_2^-															
v1 symmetric S-S stretching	546	546	546	545	545	545	547	547	547	545	545	545			(Holzer et al. 1969)
2v1 overtone		1093			1089			1100			1098				(Holzer et al. 1969)
3v1 overtone		1643			1638						1645				(Holzer et al. 1969)
4v1 overtone		2187			2182						2181				(Holzer et al. 1969)
5v1 overtone		2731			2723						2728				(Holzer et al. 1969)
6v1 overtone		3264			3256						3266				(Holzer et al. 1969)
7v1 overtone		3795			3789						3797				
8v1 overtone		4317			4314						4311				
v2 symmetric S-S bending		258			258			260			254				(Chivers and Drummond 1972)
v1+ v2 overtone		805			805			813			801				(Clark and Franks 1975)
2v1+ v2 overtone		1355			1353						1354				(Clark and Franks 1975)
3v1+ v2 overtone		1895			1898						1895				(Clark and Franks 1975)
4v1+ v2 overtone		2448			2441										
5v1+ v2 overtone		2986			2977										
6v1+ v2 overtone		3512			3509										
7v1+ v2 overtone		4049			4046										
v3 antisymmetric S-S stretching		585			582			587							(Ledé et al. 2007)
S_4^{2-}															
v1 symmetric Scentral-Sterminal stretching	483			481			483								(Janz et al. 1976)
2v1 overtone	962			960											
3v1 overtone	1439			1442											
4v1 overtone				1921											
5v1 overtone				2394											
v2 symmetric Scentral-Scentral stretching				443											(Janz et al. 1976)
v3 symmetric S-S bending	222			223											(Janz et al. 1976)
v1-v3 overtone	709			712											
3v1-v3 overtone				1685											

285 Table 2. Observed vibrational frequencies of S_2^- and S_3^- radicals and the S_4^{2-} polysulfide ions in
 286 lazurite, haüyne and ultramarine blue.

287

288

Implications

289

290 The spectral features of the S_4^{2-} polysulfide ion are only visible in Raman resonance spectra
 291 collected with 405 nm excitation that lies inside the absorbance band of S_4^{2-} . The absence of
 292 these peak in the MD simulations and in the observations with other laser wavelengths suggests a
 293 strong Raman resonance effect. This underlines that Raman resonance spectroscopy a powerful
 294 method to detect very low concentrations of S_4^{2-} (and other polysulfides), which are below the
 295 detection limit of Raman spectra collected with different excitations or other conventional
 296 analytical techniques (e.g., X-ray powder diffraction).

297 The intensity of the Raman bands of S_2^- and S_3^- radicals is also very strongly enhanced
 298 when these species are measured with excitations that lie inside their respective absorption
 299 bands, showing that resonance Raman spectroscopy is a powerful qualitative tool to detect very

300 small amounts of sulfur radicals. However, in studies aiming to measure the concentration of
301 sulfur radicals in solutions, Raman resonance should be eliminated and the quantification of
302 sulfur radicals should only be attempted with excitations lying outside their respective absorption
303 bands (Schmidt and Seward 2017). This is critically important for studies aiming to quantify
304 sulfur radical species in high-pressure-temperature fluids resembling geologic fluids and assess
305 their role in metal mobilization, transport, and ore deposit formation. Hackmanite, a variety of
306 sodalite, has been suggested to contain S_2^- radicals (Müller 2017). To confirm this suggestion
307 and to detect polysulfide species in different minerals and materials, resonance Raman
308 spectroscopy seem to be the ideal analytical technique.

309 The laser induced decomposition of the S_4^{2-} polysulfide ion into two S_2^- radicals in
310 lazurite was observed even while using a 5% laser power filter (corresponding to ~ 1.5 mW at the
311 sample). Sulfur species are known for their sensitivity to visible light and high probability for
312 beam damage (Steudel and Chivers 2019). Checks for laser induced reactions and damage and
313 the use of low laser power is therefore recommended when analyzing polysulfides.

314 Given the post-entrapment and post-cooling immobility of most sulfur species in the
315 sodalite cages of lazurite and haüyne, their ratios can potentially reflect the chemical state of
316 metasomatizing fluids (Tauson et al. 2011). The distinct $SO_4^{2-}/(S_2^- + S_4^{2-})/S_3^-$ ratios of the
317 analyzed lazurite samples may also provide hints on the provenance of lazurite used to make
318 ultramarine blue pigments.

319 Finally, there is considerable interest in entrapping S_4^{2-} into synthetic sodalite structure
320 materials, because these show high external quantum efficiency values, large Stokes shifts, and
321 thermal stability, and can find applications in light down-conversion systems or as phosphors in

322 lighting devices (Ruivo et al. 2018). S_4^{2-} in haüyne was found surprisingly stable in comparison
323 with lazurite, making haüyne a potentially interesting host material for S_4^{2-} entrapment.

324

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326

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341

342 **References**

343

344 Badoz-Lambling, J., Bonnaterre, R., Cauquis, G., Delamar, M., and Demange, G. (1976) La

- 345 reduction du soufre en milieu organique. *Electrochimica Acta*, 21, 119–131.
- 346 Blöchl, P.E. (1994) Projector augmented-wave method. *Physical Review B*, 50, 17953–17979.
- 347 Caggiani, M.C., Acquafredda, P., Colomban, P., and Mangone, A. (2014) The source of blue
348 colour of archaeological glass and glazes: the Raman spectroscopy/SEM-EDS answers.
349 *Journal of Raman Spectroscopy*, 45, 1251–1259.
- 350 Caggiani, M.C., Mangone, A., and Acquafredda, P. (2022) Blue coloured haüyne from Mt.
351 Vulture (Italy) volcanic rocks: SEM-EDS and Raman investigation of natural and heated
352 crystals. *Journal of Raman Spectroscopy*, 53, 956–968.
- 353 Caracas, R., Kobsch, A., Solomatova, N. V., Li, Z., Soubiran, F., and Hernandez, J.A. (2021a)
354 Analyzing melts and fluids from Ab initio molecular dynamics simulations with the UMD
355 package. *Journal of Visualized Experiments*, 2021, 1–20.
- 356 ——— (2021b) Analyzing melts and fluids from Ab initio molecular dynamics simulations with
357 the UMD package. *Journal of Visualized Experiments*, 2021.
- 358 Chivers, T. (1974) Ubiquitous trisulphur radical ion S₃⁻. *Nature*, 252, 32–33.
- 359 Chivers, T., and Drummond, I. (1972) Characterization of the Trisulfur Radical Anion S₃⁻ in
360 Blue Solutions of Alkali Polysulfides in Hexamethylphosphoramide. *Inorganic Chemistry*,
361 11, 2525–2527.
- 362 Chivers, T., and Lau, C. (1982) Raman Spectroscopic Identification of the S₄N⁻ and S₃⁻ Ions in
363 Blue Solutions of Sulfur in Liquid Ammonia. *Inorganic Chemistry*, 21, 453–455.
- 364 Choi, B.-K., and Lockwood, D.. (1989) Raman spectrum of Na₂SO₄ (Phase V). *Solid State*
365 *Communications*, 72, 133–137.
- 366 Clark, B.R.J.H., and Dines, T.J. (1986) Resonance Raman Spectroscopy, and Its Application to
367 *Inorganic Chemistry*. *Angewandte Chemie - International Edition*, 25, 131–158.

- 368 Clark, R.J.H., and Cobbold, D.G. (1978) Characterization of Sulfur Radical Anions in Solutions
369 of Alkali Polysulfides in Dimethylformamide and Hexamethylphosphoramide and in the
370 Solid State in Ultramarine Blue, Green, and Red. *Inorganic Chemistry*, 17, 3169–3174.
- 371 Clark, R.J.H., and Franks, M.L. (1975) The resonance Raman spectrum of ultramarine blue.
372 *Chemical Physics Letters*, 34, 69–72.
- 373 Del Federico, E., Shöfberger, W., Schelvis, J., Kapetanaki, S., Tyne, L., and Jerschow, A. (2006)
374 Insight into Framework Destruction in Ultramarine Pigments. *Inorganic Chemistry*, 45,
375 1270–1276.
- 376 Fleet, M.E., Liu, X., Harmer, S.L., and Nesbitt, H.W. (2005) Chemical state of sulfur in natural
377 and synthetic lazurite by S K-edge XANES and X-ray photoelectron spectroscopy. *The*
378 *Canadian Mineralogist*, 43, 1589–1603.
- 379 Gaetani, M.C., Santamaria, U., and Seccaroni, C. (2004) The use of Egyptian blue and lapis
380 lazuli in the middle ages: The wall paintings of the San Saba church in Rome. *Studies in*
381 *Conservation*, 49, 13–22.
- 382 Gambardella, A.A., Schmidt Patterson, C.M., Webb, S.M., and Walton, M.S. (2016) Sulfur K-
383 edge XANES of lazurite: Toward determining the provenance of lapis lazuli.
384 *Microchemical Journal*, 125, 299–307.
- 385 Gettens, R.J. (1938) The materials in the wall paintings of Bamiyan, Afghanistan. *Technical*
386 *studies in the field of the fine arts*, 6, 186–193.
- 387 Giggenbach, W. (1968) On the nature of blue sulfur solutions. *Journal of Inorganic and Nuclear*
388 *Chemistry*, 30, 3189–3201.
- 389 González-Cabrera, M., Wieland, K., Eitenberger, E., Bleier, A., Brunnbauer, L., Limbeck, A.,
390 Hutter, H., Haisch, C., Lendl, B., Domínguez-Vidal, A., and others (2022) Multisensor

- 391 hyperspectral imaging approach for the microchemical analysis of ultramarine blue
392 pigments. *Scientific Reports*, 12, 707.
- 393 Hassan, I., and Grundy, H.D. (1991) The crystal structure of hauyne at 293 and 153 K. *The*
394 *Canadian Mineralogist*, 29, 123–130.
- 395 Hassan, I., Peterson, R.C., and Grundy, H.D. (1985) The Structure of Lazurite, Ideally
396 $\text{Na}_6\text{Ca}_2(\text{Al}_6\text{Si}_6\text{O}_{24})\text{S}_2$, a Member of the Sodalite Group. *Acta Crystallographica*, C41,
397 827–832.
- 398 Holzer, W., Murphy, W.F., and Bernstein, H.J. (1969) Raman Spectra of Negative Molecular
399 Ions Doped in Alkali Halide Crystals. *Journal of Molecular Spectroscopy*, 32, 13–23.
- 400 ——— (1970) Resonance Raman Effect and Resonance Fluorescence in Halogen Gases. *The*
401 *Journal of Chemical Physics*, 52, 399–407.
- 402 Janz, G.J., Downey, J.R., Roduner, E., Wasilczyk, G.J., Coutts, J.W., and Eluard, A. (1976)
403 Raman Studies of Sulfur-Containing Anions in Inorganic Polysulfides. *Sodium. Inorganic*
404 *Chemistry*, 15, 1759–1763.
- 405 Kresse, G., and Hafner, J. (1993) Ab initio molecular dynamics for liquid metals. *Physical*
406 *Review B*, 47, 558–561.
- 407 Kresse, G., and Joubert, D. (1999) From ultrasoft pseudopotentials to the projector augmented-
408 wave method. *Physical Review B - Condensed Matter and Materials Physics*, 59, 1758–
409 1775.
- 410 Ledé, B., Demortier, A., Gobeltz-Hautecœur, N., Lelieur, J.P., Picquenard, E., and Duhayon, C.
411 (2007) Observation of the ν_3 Raman band of S^{3-} inserted into sodalite cages. *Journal of*
412 *Raman Spectroscopy*, 38, 1461–1468.
- 413 Lim, H.S., Heo, N.H., and Seff, K. (2018) Disproportionation of an Element in a Zeolite. III.

- 414 Crystal Structure of a High-Temperature Sulfur Sorption Complex of Zeolite LTA
415 Containing Two New Ions: Perthiosulfite, S₄²⁻, and the Trisulfur Cation, S₃²⁺. Journal of
416 Physical Chemistry C, 122, 28133–28141.
- 417 Linguerri, R., Komiha, N., Fabian, J., and Rosmus, P. (2008) Electronic States of the
418 Ultramarine Chromophore S₃⁻. Zeitschrift für Physikalische Chemie, 222, 163–176.
- 419 Martin, R.P., Doub, W.H., Roberts, J.L., and Sawyer, D.T. (1973) Further Studies of the
420 Electrochemical Reduction of Sulfur in Aprotic Solvents. Inorganic Chemistry, 12, 1921–
421 1925.
- 422 Mealli, C., Ienco, A., Poduska, A., and Hoffmann, R. (2008) S₄²⁻ rings, disulfides, and sulfides
423 in transition-metal complexes: The subtle interplay of oxidation and structure. Angewandte
424 Chemie - International Edition, 47, 2864–2868.
- 425 Müller, H. (2017) La fluorite bleuissante de Tignes, Tarentaise, Savoie. Le Règne Minéral, 42–
426 44.
- 427 Nafie, L.A., Stein, P., and Peticolas, W.L. (1971) Time ordered diagrams for the resonant Raman
428 effect from molecular vibrations. Chemical Physics Letters, 12, 131–136.
- 429 Ostroumov, M., Fritsch, E., Faulques, E., and Chauvet, O. (2002) Etude spectrométrique de la
430 lazurite du Pamir, Tadjikistan. Canadian Mineralogist, 40, 885–893.
- 431 Perdew, J.P., Burke, K., and Ernzerhof, M. (1996) Generalized gradient approximation made
432 simple. Physical Review Letters, 77, 3865–3868.
- 433 Picquenard, E., El Jaroudi, O., and Corset, J. (1993) Resonance Raman spectra of the S₃
434 molecule in sulphur vapour. Journal of Raman Spectroscopy, 24, 11–19.
- 435 Poduska, A., Hoffmann, R., Ienco, A., and Mealli, C. (2009) “Half-bonds” in an unusual
436 coordinated S₄²⁻ rectangle. Chemistry - An Asian Journal, 4, 302–313.

- 437 Pokrovski, G.S., and Dubessy, J. (2015) Stability and abundance of the trisulfur radical ion S₃-
438 in hydrothermal fluids. *Earth and Planetary Science Letters*, 411, 298–309.
- 439 Pokrovski, G.S., and Dubrovinsky, L.S. (2011) The S₃- ion is stable in geological fluids at
440 elevated temperatures and pressures. *Science*, 331, 1052–1054.
- 441 Reinen, D., and Lindner, G.G. (1999) The nature of the chalcogen colour centres in ultramarine-
442 type solids. *Chemical Society Reviews*, 28, 75–84.
- 443 Ruivo, A., Coutino-Gonzalez, E., Santos, M.M., Baekelant, W., Fron, E., Roeffaers, M.B.J.,
444 Pina, F., Hofkens, J., and Laia, C.A.T. (2018) Highly Photoluminescent Sulfide Clusters
445 Confined in Zeolites. *The Journal of Physical Chemistry C*, 122, 14761–14770.
- 446 Sapozhnikov, A.N. (2021) On the crystal chemistry of sulfur-rich lazurite, ideally
447 Na₇Ca(Al₆Si₆O₂₄)(SO₄)(S₃)·nH₂O. *American Mineralogist*, 106, 226–234.
- 448 Schmidt, C., and Seward, T.M. (2017) Raman spectroscopic quantification of sulfur species in
449 aqueous fluids: Ratios of relative molar scattering factors of Raman bands of H₂S, HS⁻,
450 SO₂, HSO₄⁻, SO₄²⁻, S₂O₃²⁻, S₃⁻ and H₂O at ambient conditions and information on
451 changes with pressure and tempe. *Chemical Geology*, 467, 64–75.
- 452 Seel, F., Güttler, H.-J., Simon, G., and Wieckowski, A. (1977) Colored Sulfur Species in EPD-
453 Solvents. *Pure and Applied Chemistry*, 49, 45–54.
- 454 Shnitko, I., Fulara, J., Garkusha, I., Nagy, A., and Maier, J.P. (2008) Electronic transitions of S₂-
455 and S₃- in neon matrixes. *Chemical Physics*, 346, 8–12.
- 456 Steudel, R., and Chivers, T. (2019) The role of polysulfide dianions and radical anions in the
457 chemical, physical and biological sciences, including sulfur-based batteries. *Chemical*
458 *Society Reviews*, 48, 3279–3319.
- 459 Tauson, V.L., Sapozhnikov, A.N., Shinkareva, S.N., and Lustenberg, E.E. (2011) Indicative

- 460 properties of lazurite as a member of clathrasil mineral family. *Doklady Earth Sciences*,
461 441, 1732–1737.
- 462 Tauson, V.L., Goettlicher, J., Sapozhnikov, A.N., Mangold, S., and Lustenberg, E.E. (2012)
463 Sulphur speciation in lazurite-type minerals $(\text{Na,Ca})_8[\text{Al}_6\text{Si}_6\text{O}_{24}](\text{SO}_4,\text{S})_2$ and their
464 annealing products: a comparative XPS and XAS study. *European Journal of Mineralogy*,
465 24, 133–152.
- 466 Tegman, R. (1973) The Crystal Structure of Sodium Tetrasulphide, Na_2S_4 . *Acta*
467 *Crystallographica*, B29, 1463–1469.
- 468 Tossell, J.A. (2012) Calculation of the properties of the S_3^- radical anion and its complexes with
469 Cu^+ in aqueous solution. *Geochimica et Cosmochimica Acta*, 95, 79–92.
- 470

471 **List of figures**

472

473 Figure 1. Diffuse reflectance spectrum of the NHMG425.086 lazurite sample from Brazil
474 showing absorption bands of S_2^- and S_3^- radicals. The 405, 532, and 785 nm excitation lines used
475 in this study are also shown.

476

477 Figure 2. Raman spectra of lazurite samples collected with different excitations: a-b) spectra of
478 the NHMG003.084 sample from Baikal, Russia; c-d) spectra of the NHMG425.086 sample from
479 Brazil. In b) and d) spectra collected with the 405 nm excitation were vertically exaggerated and
480 offset relative to the 532 nm spectra.

481

482 Figure 3. Raman spectra of the NHMG333.049 haüyne sample from Mount Vesuvius, Italy
483 collected with different excitations. In b) the spectrum collected with the 405 nm excitation was
484 vertically exaggerated and offset relative to the 532 nm spectrum.

485

486 Figure 4. Raman spectra of the “45000 Ultramarine blue, very dark” pigment collected with
487 different excitations. In b) the spectrum collected with the 405 nm excitation was vertically
488 exaggerated and offset relative to the 532 nm spectrum.

489

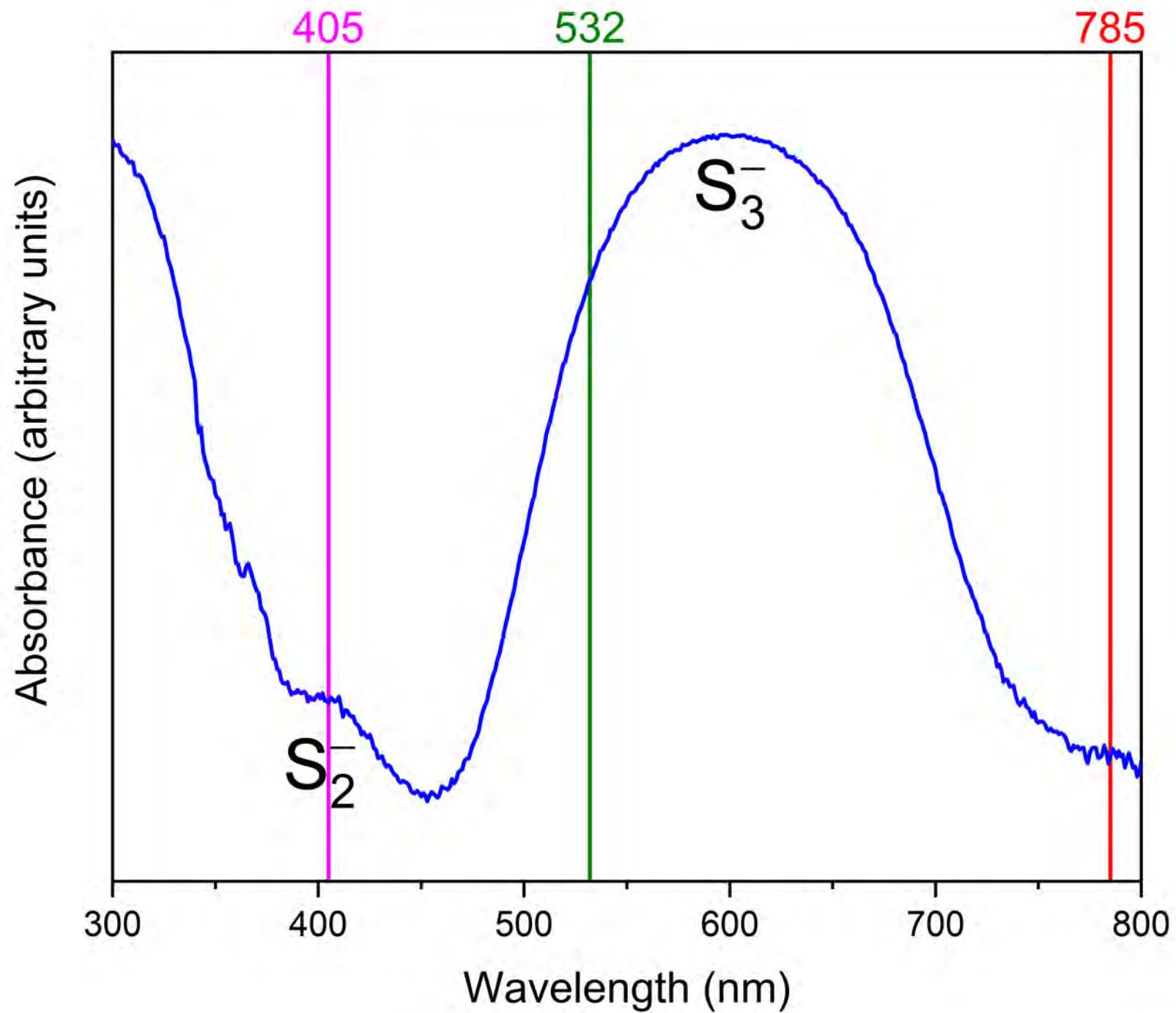
490 Figure 5. Spectra showing the laser-induced decomposition of the S_4^{2-} polysulfide ions into S_2^-
491 radicals in lazurite sample NHMG425.086 from Brazil. Both spectra were collected with 405 nm
492 excitation, 50% laser power filter, and for a duration of 1 s. The red spectrum was collected
493 following a 29 s exposure of sample to laser beam, resulting in 30 s of total exposure time.

494
495 Figure 6. a-b) Time profiles showing the gradual, laser-induced decomposition of the S_4^{2-}
496 polysulfide ions into S_2^- radicals in lazurite samples. All spectra were collected with the 405 nm
497 excitation, 10% laser power filter, and for a duration of 10 s. The numbers in the key indicate
498 total exposure times to laser beam. a) sample NHMG003.084 from Baikal, Russia; b) sample
499 NHMG425.086 from Brazil. Note the difference in initial $\nu_1(S_4^{2-})/\nu_1(S_2^-)$ band ratios. c-d)
500 Corresponding changes in peak areas.

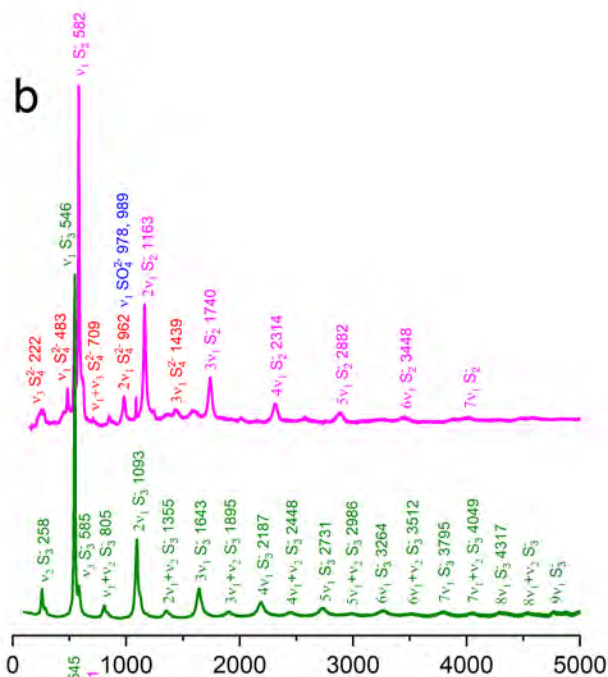
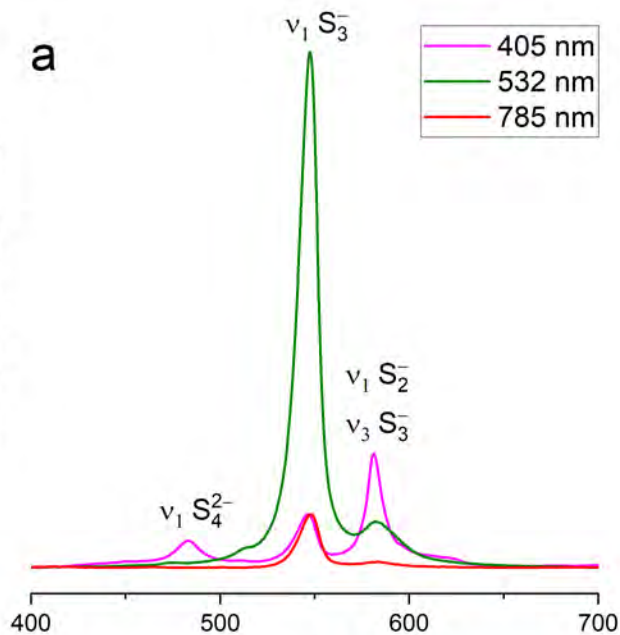
501
502 Figure 7. Time profiles showing the effect of laser power expressed as % of maximum power (30
503 mW at the sample) on the gradual, laser-induced decomposition of the S_4^{2-} polysulfide ions into
504 S_2^- radicals in the NHMG425.086 lazurite sample from Brazil collected with the 405 nm
505 excitation and for a duration of 10 s. The numbers in the key indicate total exposure times to
506 laser beam.

507
508 Figure 8. Time profile showing the stability of S_4^{2-} polysulfide ions in the NHMG333.049
509 haüyne sample from Mount Vesuvius, Italy. All spectra were collected with the 405 nm
510 excitation, at full laser power, and for a duration of 10 s. The numbers in the key indicate total
511 exposure times to laser beam.

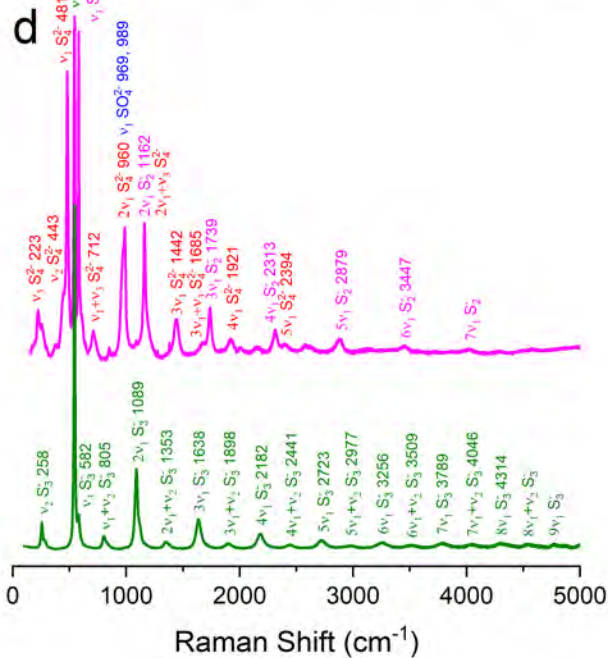
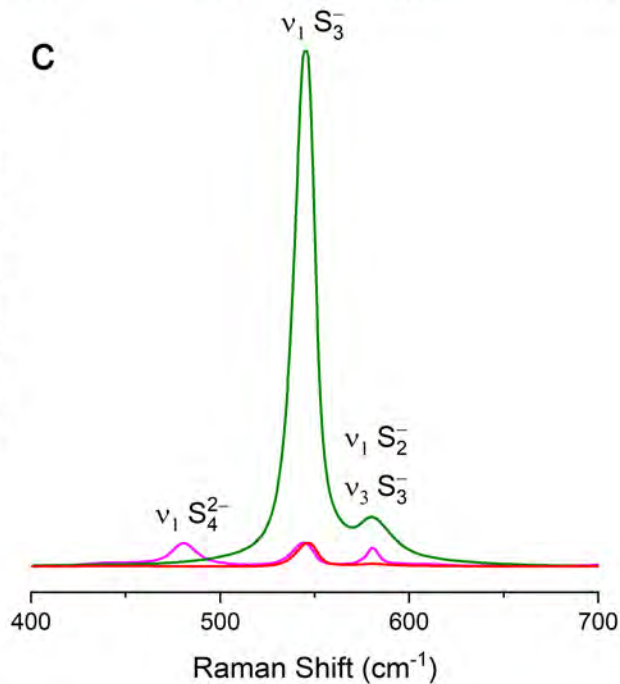
512
513 Figure 9. S–S pair distribution functions computed for the polysulfide groups trapped in lazurite.
514 The first peak corresponds to the average interatomic bond distance. The first minima (which are
515 marked on the plot) correspond to the radius of the first coordination sphere. Atoms are
516 considered bonded if their distance is less than this radius.



Intensity (arbitrary units)

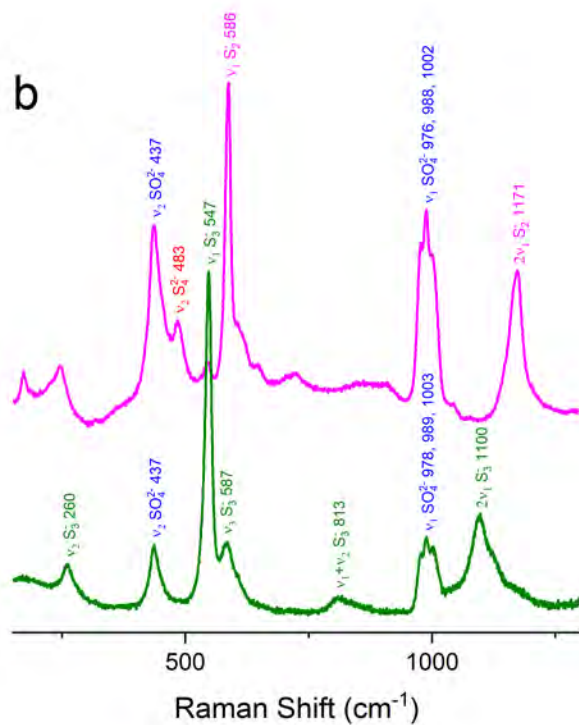
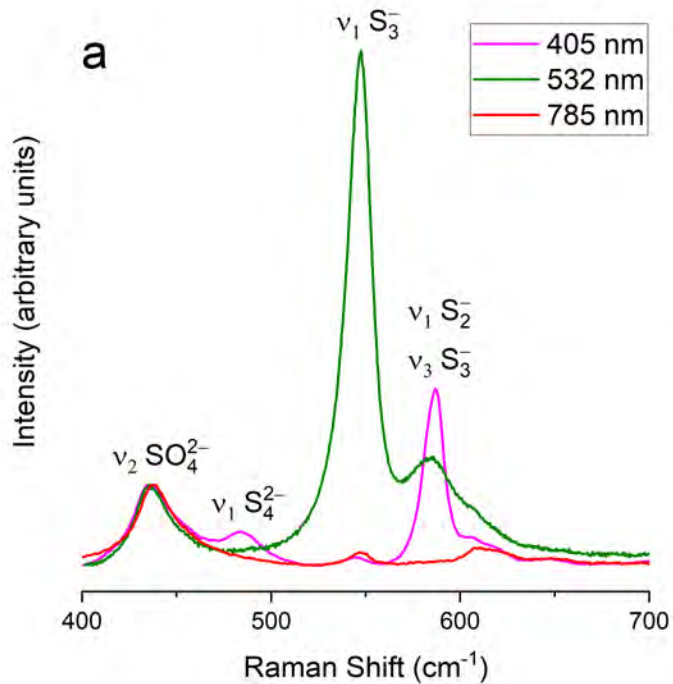


Intensity (arbitrary units)



Raman Shift (cm^{-1})

Raman Shift (cm^{-1})



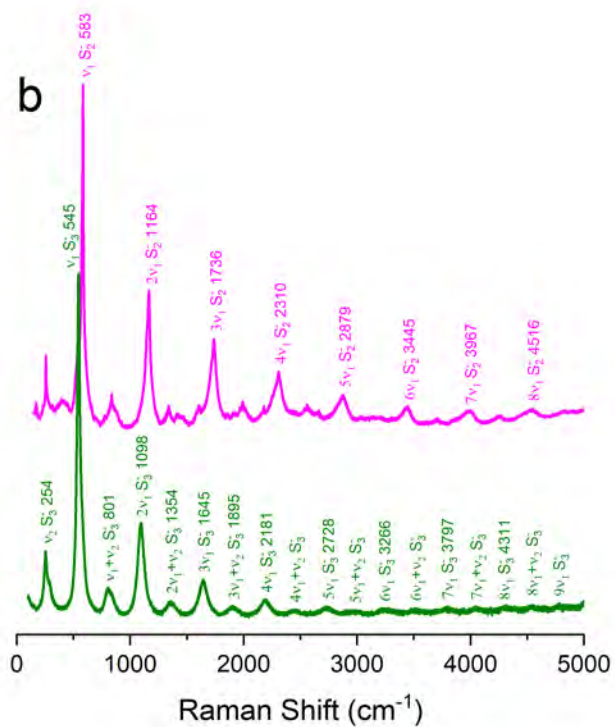
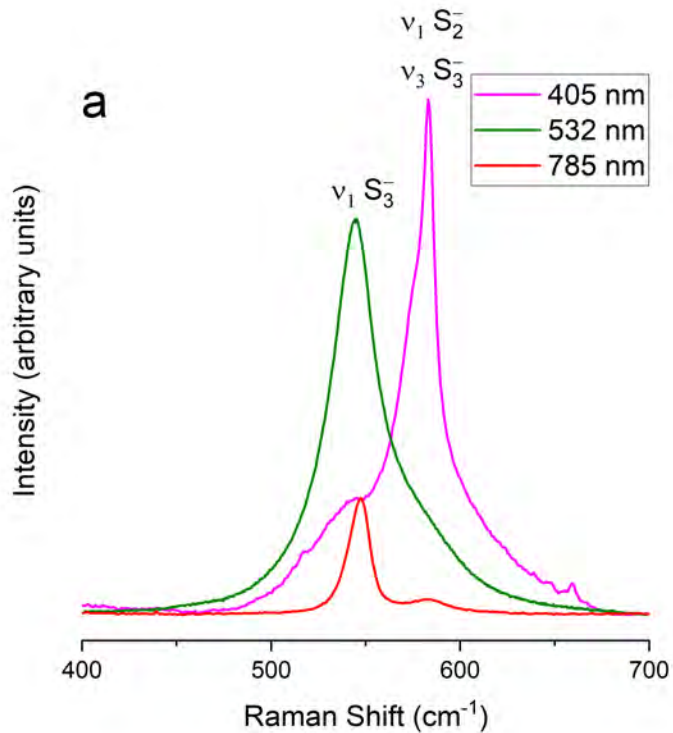


Figure 5

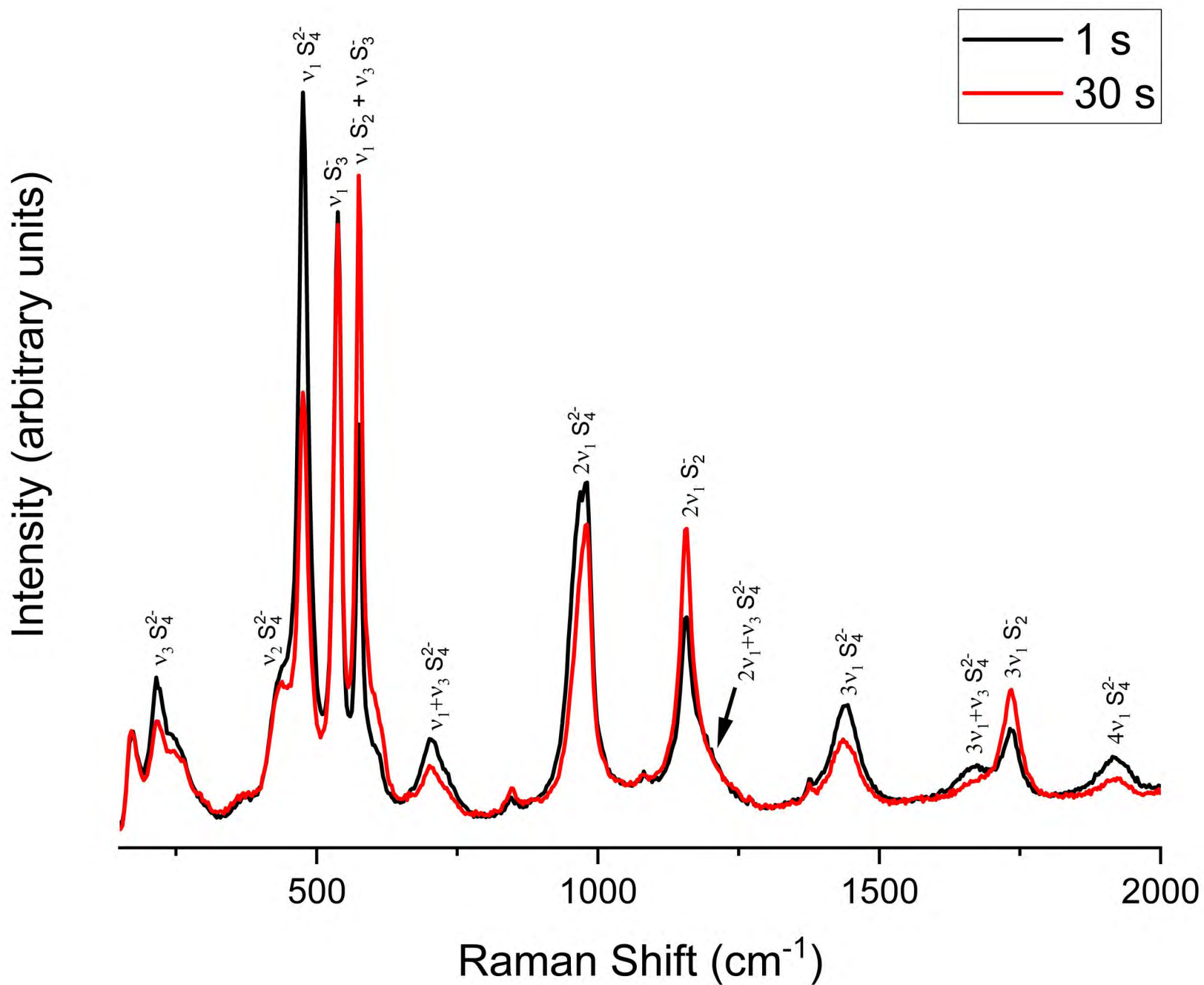


Figure 6

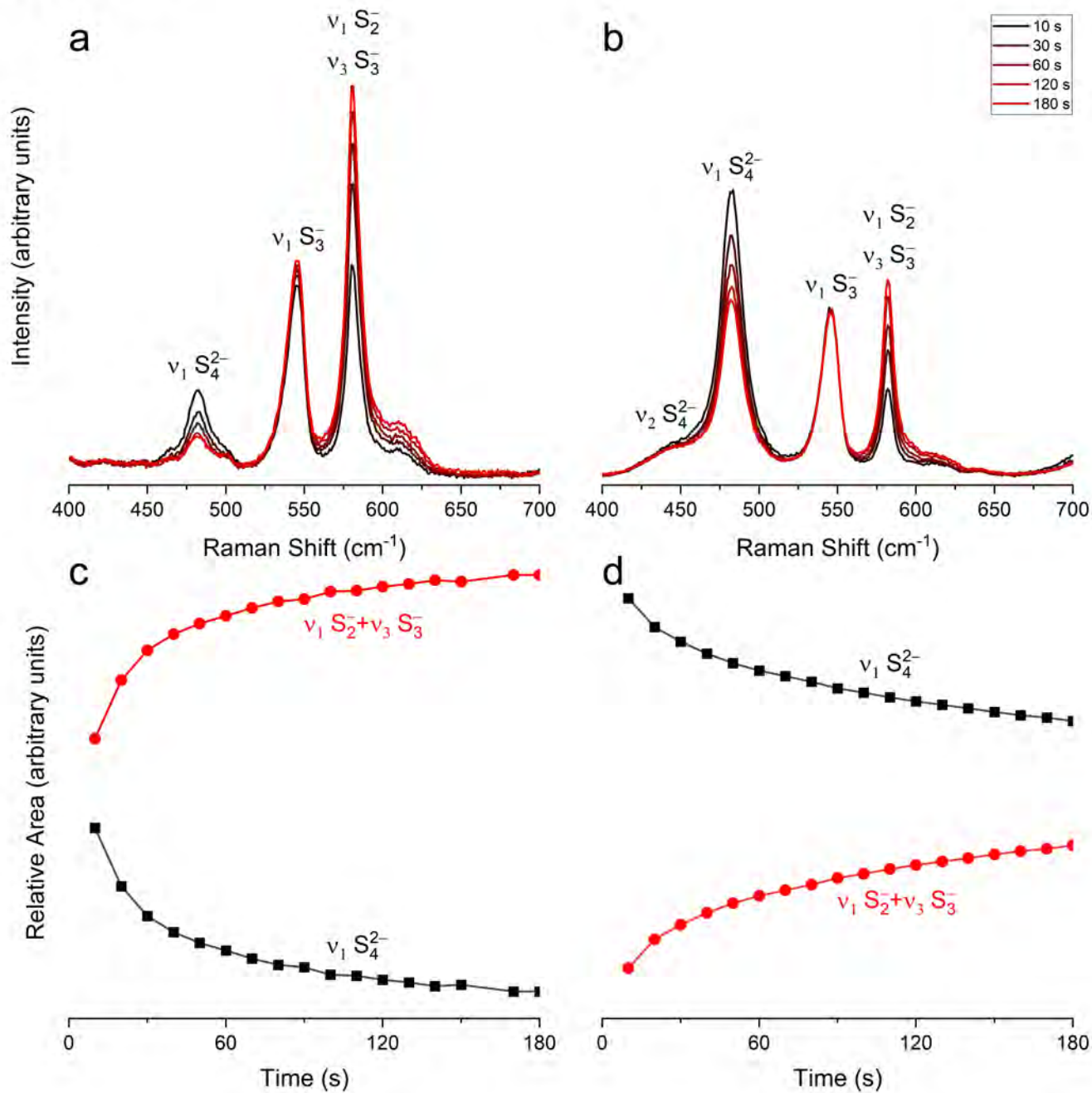
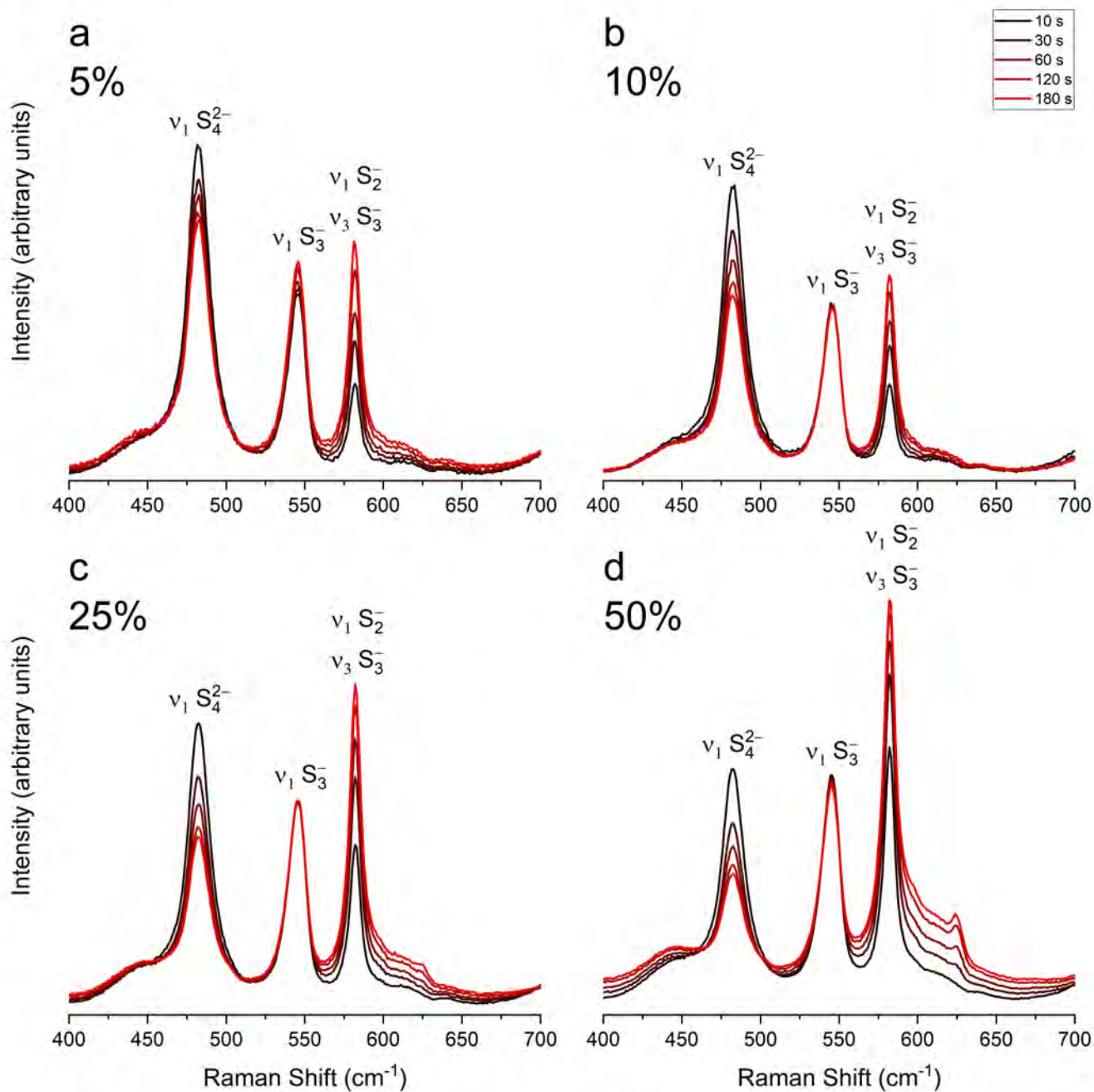


Figure 7



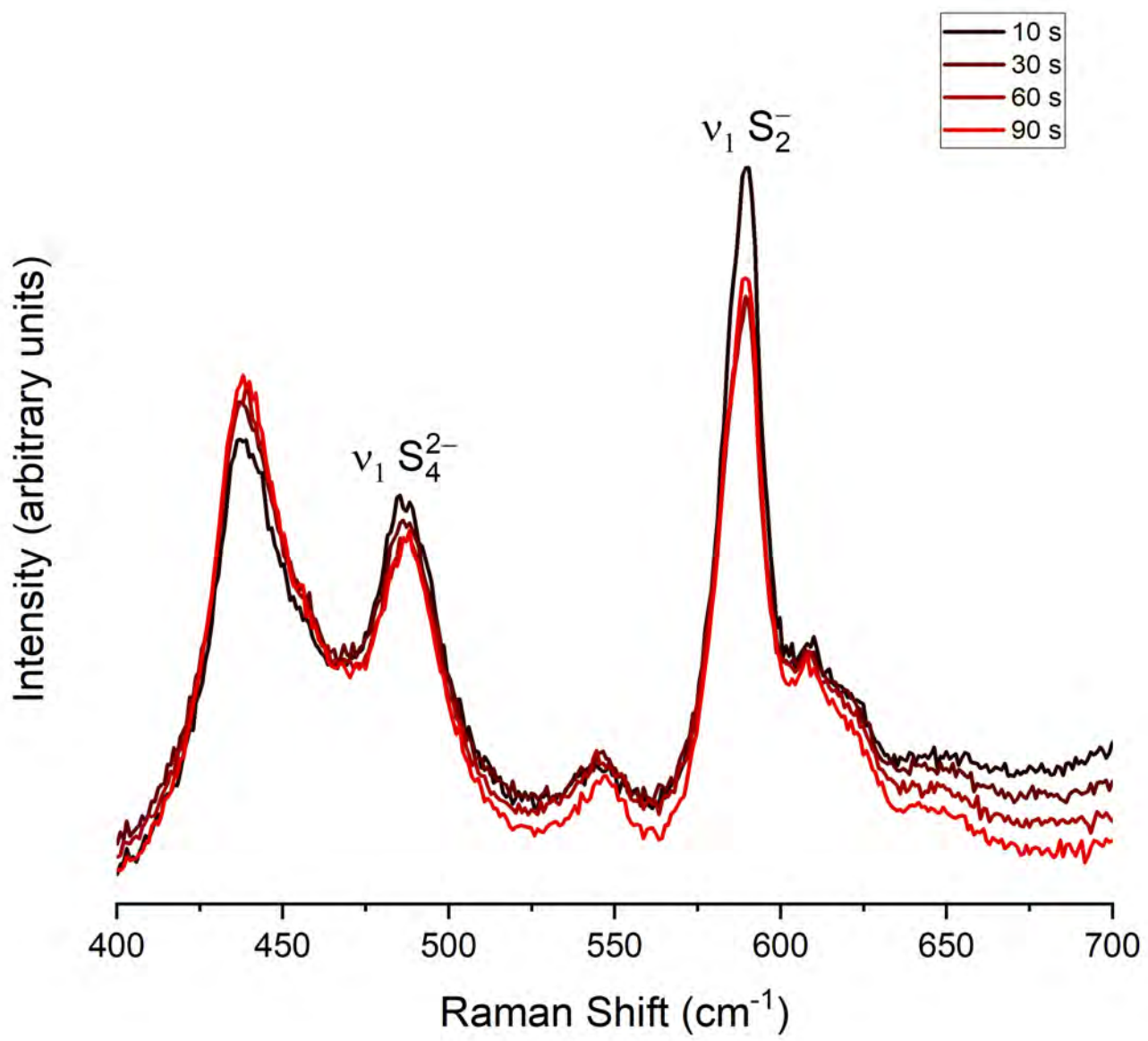


Figure 8

