

## Revision 2

# The Olivine-Spinel- $a_{\text{SiO}_2}^{\text{melt}}$ (OSaS) Oxybarometer: A New Method for Evaluating Magmatic Oxygen Fugacity in Olivine-Phyric Basalts

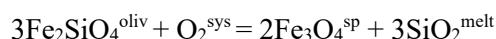
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### Abstract

The compositions of cotectic olivine-spinel pairs in mafic magmas provide information on the oxygen fugacity of their host liquid, which can be accessed with a thermodynamic analysis of the olivine-spinel-liquid peritectic reaction:



The extraction of redox information from cotectic olivine-spinel pairs requires a well-defined silica activity value ( $a_{\text{SiO}_2}^{\text{melt}}$ ) for the melt of interest, as well as a method to calculate  $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$  and  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$  from chemical analyses of olivine and spinel, respectively. In this work, we develop a new olivine-spinel- $a_{\text{SiO}_2}^{\text{melt}}$  (OSaS) oxygen barometer that utilizes MELTS to obtain values of  $a_{\text{SiO}_2}^{\text{melt}}$ , which are used with values  $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$  and  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$  determined from established solution models for olivine and spinel. We find that two implementations of the spinel-liquid peritectic equilibria can successfully generate magmatic oxygen fugacity values, (1) using a combination of mineral activity models from the literature (classical-OSaS) and  $a_{\text{SiO}_2}^{\text{melt}}$  determined from MELTS, and (2) directly from chemical potentials obtained from MELTS, where a correction is added to the MELTS-derived chemical potentials for the magnetite component of the spinel (MELTS-OSaS). The two implementations of the OSaS were tested by using each model to recover the experimentally reported  $f\text{O}_2$  values for a dataset consisting of 50 olivine-spinel-glass assemblages derived from 14 published experimental studies. This dataset was filtered to remove potential disequilibrium phase assemblages, experiments with failed redox buffers, and poor-quality EMP analyses. Data quality metrics for the dataset filtration included Fe-Mg partitioning between olivine and melt, Fe-Mg partitioning between olivine-spinel, and an examination of whether  $a_{\text{SiO}_2}^{\text{melt}}$  values were consistent with the reported phase assemblages. The classical-OSaS implementations reproduced the  $f\text{O}_2$  values reported from the experimental dataset with a standard error estimate (SEE) of  $\pm 0.39$ , root mean standard error (RMSE) of  $\pm 0.40$  and average deviation of  $\pm 0.31$ . In testing the MELTS-OSaS model, we identified that the solution model for magnetite underpredicted the values of  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$ ; therefore, we used the 50 experiments to assign a

35 correction to the MELTS-predicted chemical potentials of magnetite. We tested the MELTS-OSaS model  
36 with the magnetite correction on a dataset of 18 additional buffered experiments, filtered for redox  
37 equilibrium and not included in the original experimental dataset. We find that the MELTS-OSaS model,  
38 which includes the correction for the magnetite chemical potential, reproduces  $fO_2$  values for the 18  
39 experiments with an SEE of  $\pm 0.20$ , root mean standard error (RMSE) of  $\pm 0.23$  and average deviation of  
40  $\pm 0.18$ . The OSaS oxybarometer can return magmatic  $fO_2$  values with a standard error of  $\pm 0.20$  to 0.39 log  
41 units, depending on the model selected, provided that the olivine-spinel cotectic temperature is known to  
42 an accuracy of  $\pm 25^\circ\text{C}$ , the  $\text{H}_2\text{O}$  content of the melt can be estimated within  $\pm 1.5\text{wt}\%$ , and that the  
43 crystallization pressure of the olivine-spinel pair is  $< 500$  MPa. We also propose that the OSaS models can  
44 be applied to experimental run products to determine or confirm oxygen fugacity values. We additionally  
45 suggest that the careful application of the OSaS oxybarometer can provide a reliable and robust alternative  
46 for performing redox studies on samples that do not contain sufficient glassy material to support the  
47 application of spectroscopic techniques (i.e., XANES and Mössbauer).

48

## 49 **1. Introduction**

50 Oxygen fugacity ( $fO_2$ ) exerts critical influence on a wide range of petrologic and geochemical  
51 processes. In the broadest sense, oxygen fugacity plays a deterministic role in dictating the distribution of  
52 polyvalent elements (e.g., Fe, S, V, Mo, Cr) among various geochemical reservoirs - core, mantle, and crust  
53 - within the Earth (Arculus, 1979; Frost & McCammon, 2008). The bulk composition and speciation of  
54 magmatic fluids, which are ultimately emitted as fumarolic gasses (Gaillard & Scaillet, 2014; Moussallam  
55 et al., 2016; Ortenzi et al., 2020), are also directly controlled by magmatic oxygen fugacity; as such the  
56 prevailing  $fO_2$  of planetary scale magma oceans exerts significant influence over the development and  
57 evolution of early planetary atmospheres (Deng et al., 2020; Hirschmann, 2012; Sossi et al., 2020). The  
58 influence of oxygen fugacity even extends to rheological properties of mantle peridotites, where it controls  
59 the point defect density in olivine and therefore its effective viscosity and seismic properties (Bai et al.,  
60 1991; Cline et al., 2018). Understanding the prevailing oxidation state of basaltic magmas underpins our  
61 ability to interpret and predict liquid-crystal phase equilibria along their liquid lines of descent, as well as  
62 the speciation and degassing behaviors of their dissolved C-H-S-O volatile components (Gaillard &  
63 Scaillet, 2014). Perhaps even more importantly, the  $fO_2$  record preserved in primitive basaltic magmas is  
64 an accessible, albeit indirect, archive of redox heterogeneity among various geochemical reservoirs within  
65 the Earth's upper mantle. Comparisons of the  $fO_2$  values estimated for basalts with those of their peridotite  
66 sources (Birner et al., 2018; Carmichael, 1991; Cottrell et al., 2020; Stolper et al., 2020) show broad  
67 agreement, suggesting that basalts are indeed faithful recorders of the  $fO_2$  of their mantle sources. Thus,  $fO_2$

68 measurements from basalts may provide insights into spatial and temporal changes in the oxidation state of  
69 the mantle driven by the deep Earth oxygen cycle.

70 Magmatic redox conditions are typically assessed by either spectroscopic measurements or  
71 thermodynamic phase equilibrium approaches. If glassy materials are available (e.g., matrix glass or melt  
72 inclusions), Fe K-edge XANES (X-ray Absorption Near Edge Spectroscopy) (Berry et al., 2003; Cottrell  
73 & Kelley, 2011; O'Neill et al., 2018; Zhang et al., 2018)) or Mössbauer Spectroscopy measurements are  
74 commonly employed to quantify  $\text{Fe}^{3+}/\Sigma\text{Fe}$  ratios in glasses (O'Neill et al., 2018; Zhang, 2019). Measured  
75  $\text{Fe}^{3+}/\Sigma\text{Fe}$  ratios are subsequently converted into oxygen fugacities using an established model that relates  
76  $f\text{O}_2$  to intensive variables such as temperature, pressure, and liquid composition (Jayasuriya et al., 2004;  
77 Kress & Carmichael, 1991; O'Neill et al., 2018; Borisov et al. 2018). Although basalt is one of the most  
78 abundant terrestrial, martian, and asteroidal materials, there are surprisingly few methods for appraising the  
79 magmatic oxygen fugacity of primitive samples lacking the glassy material required for the application of  
80 spectroscopic techniques.

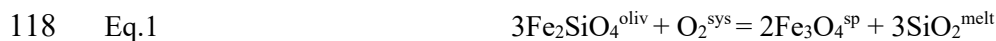
81 Phase equilibrium-based approaches, such as the magnetite-ilmenite geothermometer and  
82 oxybarometer (Buddington & Lindsley, 1964; Ghiorso & Evans, 2008) or the olivine-orthopyroxene-spinel  
83 oxybarometer (Bryndzia and Wood 1990; Ballhaus et al., 1991), can in some instances be applied to  
84 samples not amenable to spectroscopic methods of study. Though phase equilibrium-based oxybarometers  
85 can partially fill the technique gap for holocrystalline samples, we stress that the existing methods are not  
86 without drawbacks and limitations. For example, the reliability of redox calculations from magnetite-  
87 ilmenite pairs is often compromised in mafic samples, as these phases are highly prone to kinetic  
88 disequilibrium during crystallization, insidious low temperature re-equilibration, and post-crystallization  
89 oxy-exsolution (Hou et al., 2020, and refs within). Furthermore, magnetite-ilmenite pairs commonly appear  
90 relatively late in the crystallization sequence of basaltic magmas, therefore they may reveal little about the  
91 oxidation state of more primitive liquids. The olivine-spinel-orthopyroxene equilibrium that was originally  
92 developed as an oxybarometer for spinel peridotites by Ballhaus et al. (1991) can also be adapted for use  
93 in basalts. However, many silica-undersaturated rocks (e.g., alkaline basalts and picrites) either do not  
94 become saturated with orthopyroxene late in the crystallization sequence or fail to crystallize orthopyroxene  
95 entirely, as in the case of critically silica undersaturated compositions (Carmichael et al., 1970). The dearth  
96 of mafic compositions that generate phase assemblages with usable orthopyroxene phenocrysts limits the  
97 application of the Ballhaus et al. (1991) oxygen barometer to bulk compositions that have silica activities  
98 sufficient to support orthopyroxene crystallization.

99 The development of new, user-friendly oxybarometers for compositionally diverse basalts is a  
100 critical step if magmatic redox studies are to be expanded to a wider range of samples and tectonic settings.  
101 We stress that basalts from tectonic settings (i.e., continental rifts) that generate relatively few rapidly

102 quenched, glassy samples remain chronically understudied. In this work, we leverage thermodynamic  
103 calculations from the MELTS thermodynamic model collection (Ghiorso & Gualda, 2015; Ghiorso & Sack,  
104 1995; Gualda et al., 2012) as implemented by the ThermoEngine Python Package (Thermoengine, 2022),  
105 hereafter referred to as MELTS, to develop two novel implementations of an oxybarometer that exploit the  
106 olivine-spinel-melt equilibria. A python code containing the model with both implementations and  
107 benchmark files are provided as part of the supplemental material (Appendix A1).

## 109 2. The Olivine-Spinel- $a_{\text{SiO}_2}^{\text{melt}}$ (OSaS) Equilibrium

110 Phase equilibrium experiments and the presence of ubiquitous octahedral Cr-spinel inclusions in  
111 Mg-rich olivine phenocrysts provide strong evidence that olivine and Cr-rich spinel are the first two phases  
112 that appear on the liquidus of primitive basaltic magmas (Médard & Grove, 2008; Roeder et al., 2006). As  
113 such, cotectic olivine-spinel pairs are uniquely suited to provide insights into the prevailing magmatic  
114 oxygen fugacity of primitive basaltic liquids. Using a reaction reminiscent of the olivine-spinel-  
115 orthopyroxene equilibrium developed by Ballhaus et al. (1991), the compositions of olivine and Fe<sup>3+</sup>-  
116 bearing spinel can be formally connected to magmatic  $f\text{O}_2$  through the peritectic reaction:



119  
120 This reaction can be reformulated in thermodynamic notation to express oxygen fugacity as a function of  
121 the activity of the fayalite component of olivine ( $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$ ), the activity of the magnetite component of the  
122 spinel ( $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$ ), and the activity of SiO<sub>2</sub> in the melt ( $a_{\text{SiO}_2}^{\text{melt}}$ ):

123  
124 Eq. 2 
$$\log_{10}f\text{O}_2 = \frac{-\Delta_r G^\circ_{\text{T,P}}}{\ln(10)RT} + 3\log a_{\text{SiO}_2}^{\text{melt}} + 2\log a_{\text{Fe}_3\text{O}_4}^{\text{sp}} - 3\log a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$$

125  
126 Provided that the crystallization temperature for an olivine-spinel pair is known, the application of Eq. 2 to  
127 evaluate magmatic  $f\text{O}_2$  simply requires one to obtain values for  $\Delta_r G^\circ_{\text{(T,P)}}$ ,  $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$ ,  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$ , and  $a_{\text{SiO}_2}^{\text{melt}}$ . The  
128 calculation of  $\Delta_r G^\circ_{\text{(T,P)}}$ ,  $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$ , and  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$  is a relatively straightforward exercise, as standard state  
129 thermodynamic data (e.g.,  $\Delta_f H_{\text{Tr}}$ ,  $S^\circ_{\text{Tr}}$ , heat capacity functions, and molar volumes for the phases of interest)  
130 as well as solution models for the crystalline phases of interest are readily available. Obtaining  $a_{\text{SiO}_2}^{\text{melt}}$  values  
131 for basaltic melts that are compatible with Eq. 2 is a more difficult prospect, as the potential methods for  
132 obtaining this value are either insufficiently accurate or remain untested with respect to their efficacy when  
133 applied to  $f\text{O}_2$  calculations.

134

## 135 2.1 The Trouble with Calculating $a_{\text{SiO}_2}^{\text{melt}}$ in from Mineral-Melt Equilibria

136 One approach for obtaining the  $a_{\text{SiO}_2}^{\text{melt}}$  values for silicate magmas employs mineral-melt equilibria,  
137 such as the olivine-orthopyroxene-melt peritectic reaction. Though this approach presents the simplest  
138 solution for calculating  $a_{\text{SiO}_2}^{\text{melt}}$ , we note that equilibrium orthopyroxene-olivine pairs are relatively rare in  
139 primitive tholeiites that crystallize at shallow crustal pressures. Furthermore, orthopyroxene is entirely  
140 absent in critically silica-undersaturated alkali basalts and basanites (Carmichael et al., 1970). It is possible  
141 to reformulate the olivine-orthopyroxene-melt equilibrium in which the activity of the clinoenstatite  
142 component (augite) is substituted for the activity of enstatite in orthopyroxene. The peritectic reaction  
143 between olivine, the clinoenstatite component of high-Ca pyroxene (augite) and the melt offers an  
144 alternative approach for obtaining  $a_{\text{SiO}_2}^{\text{melt}}$  for basaltic phase assemblages that lack orthopyroxene. In magmas  
145 co-saturated with olivine and clinopyroxene the  $a_{\text{SiO}_2}^{\text{melt}}$  can be defined with the equilibrium:



148  
149 which can be re-arranged as:

150  
151 Eq. 4 
$$\log a_{\text{SiO}_2}^{\text{melt}} = \frac{-\Delta_r G^\circ_{\text{T,P}}}{\ln(10)RT} + 2\log a_{\text{MgSiO}_3}^{\text{cpx or opx}} - \log a_{\text{Mg}_2\text{SiO}_4}^{\text{oliv}}$$

152  
153 The  $\Delta_r G^\circ_{\text{(T,P)}}$  that appears in Eq. 4 is calculated from the standard state thermodynamic properties of  
154 clinoenstatite, rather than orthoenstatite. On the surface, this approach offers an appealing solution to the  
155  $a_{\text{SiO}_2}^{\text{melt}}$  problem, however there are several notable issues which diminish the effectiveness of this approach.  
156 The first issue is that cotectic olivine-spinel pairs may not be in equilibrium with augite phenocrysts in the  
157 assemblage, as clinopyroxene often appears relatively late in the crystallization sequence for melts  
158 experiencing low crystallization pressures (e.g., Sisson and Grove, 1993). The second issue is that the  
159 efficacy of this method largely depends on how well the selected clinopyroxene solution model performs  
160 for the composition of interest. For example, Bucholz and Keleman (2019) explored this approach and  
161 applied it to a suite of deep-crustal, ultramafic basaltic cumulates to determine  $a_{\text{SiO}_2}^{\text{melt}}$ . They demonstrate  
162 that  $a_{\text{SiO}_2}^{\text{melt}}$  values calculated in this manner critically depend on the pyroxene solution model's ability to  
163 generate accurate  $a_{\text{MgSiO}_3}^{\text{cpx}}$  values. The results of Bucholz and Keleman (2019) underscore the difficulty  
164 of using  $a_{\text{MgSiO}_3}^{\text{cpx}}$  values predicted for high Ca-enriched clinopyroxene. The  $a_{\text{MgSiO}_3}^{\text{cpx}}$  for Ca-enriched  
165 clinopyroxenes are insufficiently accurate for performing redox calculations, as the  $a_{\text{SiO}_2}^{\text{melt}}$  values for these

166 compositions are consistently underpredicted, which in turn, systematically skews the resultant  $f_{\text{O}_2}$  towards  
167 values that are too reduced.

168 Nikolaev et al. (2016) also attempted to exploit the olivine-spinel-melt equilibria to formulate an  
169 empirical oxybarometer for magmatic phase assemblages containing cotectic olivine-spinel pairs. In this  
170 approach the authors adopted a formulation which does not explicitly account for silica activity, where  
171 oxygen fugacity was cast as an empirical function of olivine composition, spinel composition, and  
172 temperature. Though this model successfully returns  $f_{\text{O}_2}$  values for many compositions, we stress that that  
173 the value assumed by  $a_{\text{SiO}_2}^{\text{melt}}$  in many cases exerts significant leverage on the resultant  $f_{\text{O}_2}$ . As such, empirical  
174 models lacking terms accounting for the impact of  $a_{\text{SiO}_2}^{\text{melt}}$  (which we note is not only a function of liquid  
175 composition, but also a function of pressure and dissolved water content) cannot serve as a universal model  
176 for all magmatic systems, and may produce systematically biased results for systems that have  $a_{\text{SiO}_2}^{\text{melt}}$   
177 dissimilar to the coarse “average”  $a_{\text{SiO}_2}^{\text{melt}}$  inherent to the calibration dataset.

178

### 179 3. Using MELTS to Obtain $a_{\text{SiO}_2}^{\text{melt}}$ for the OSaS Oxybarometer

180 In the absence of a silica activity buffering phase assemblage, MELTS may be utilized to obtain  
181 the silica activity for the liquid of interest through calculations of the chemical potential of silica ( $\mu_{\text{SiO}_2}^{\text{melt}}$ )  
182 for multi-component silicate melts. The  $\mu_{\text{SiO}_2}^{\text{melt}}$  values calculated from the MELTS algorithm can be  
183 converted into activity values using the expression:

184

$$185 \text{ Eq. 5} \quad \mu_{\text{SiO}_2}^{\text{melt}} - \mu_{\text{SiO}_2}^{\circ} = RT(\ln a_{\text{SiO}_2}^{\text{melt}})$$

186

187 where  $\mu_{\text{SiO}_2}^{\text{melt}}$  is the chemical potential of the  $\text{SiO}_2$  component of the melt obtained from MELTS and  $\mu_{\text{SiO}_2}^{\circ}$   
188 represents the standard state chemical potential to which the  $a_{\text{SiO}_2}^{\text{melt}}$  value is being referenced. The value of  
189  $\mu_{\text{SiO}_2}^{\circ}$  can refer to either the chemical potential of pure liquid  $\text{SiO}_2$  or the chemical potential of one of  
190 several crystalline  $\text{SiO}_2$  polymorphs. All calculations of  $\mu_{\text{SiO}_2}^{\text{melt}}$  performed in this work utilized the Rhyolite  
191 MELTS models of Ghiorso and Gualda (2015); the  $\mu_{\text{SiO}_2}^{\text{melt}}$  values were subsequently converted into obtaining  
192  $a_{\text{SiO}_2}^{\text{melt}}$  values for the liquid of interest.

193 Using MELTS, one can readily obtain  $a_{\text{SiO}_2}^{\text{melt}}$  for a basaltic melt composition of interest and  
194 subsequently insert that value along with appropriate values of  $a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$  and  $a_{\text{Fe}_3\text{O}_4}^{\text{sp}}$  into Eq.2 to calculate  $f_{\text{O}_2}$ .  
195 This approach is appealing for its familiar form (Eq. 2) and relative simplicity; for this reason, we hereafter  
196 refer to this approach as the “classical-OSaS oxybarometer.” In this version of the OSaS oxybarometer, we  
197 have opted to calculate  $\Delta_r G^{\circ}_{(T,P)}$  for the OSaS equilibrium with the internally consistent thermodynamic

198 dataset of Berman (1988), as it is inherently compatible with thermodynamic data generated from MELTS.  
199 The  $\Delta_r G^\circ_{(T,P)}$  values for Eq.1 were calculated using the standard state properties of crystalline SiO<sub>2</sub>, rather  
200 than pure silica liquid, therefore the  $a_{\text{SiO}_2}^{\text{melt}}$  values obtained from MELTS reference a high temperature  
201 polymorph of quartz as the standard state. We also note that it is possible to calculate  $\Delta_r G^\circ_{(T,P)}$  values for  
202 the OSaS oxybarometer using the Holland and Powell (2011) thermodynamic database. The  $\Delta_r G^\circ_{(T,P)}$  values  
203 calculated from the Berman (1988) and the Holland and Powell (2011) datasets differ by less than 1.5 kJ  
204 mol<sup>-1</sup> (from 1100°C to 1300°C). The subtle differences in the  $\Delta_r G^\circ_{(T,P)}$  obtained from the two databases  
205 translates to a difference in oxygen fugacity values of < 0.075 log units for the end-member quartz-fayalite-  
206 magnetite buffer reaction. This comparison suggests that implementing  $\Delta_r G^\circ_{(T,P)}$  calculated from either the  
207 Berman (1988) or the Holland and Powell (2011) databases in the OSaS should return nearly identical  $f_{\text{O}_2}$   
208 values.

209 We use the olivine solution model of O'Neill et al. (2003) to calculate fayalite activities, as the  
210 interaction parameter from this model is consistent with the calorimetrically determined mixing parameters  
211 of Dachs and Gieger (2007). Using the symmetric regular solution model of O'Neill et al. (2003), fayalite  
212 activity is calculated, using Eqs. 6 & 7:

213  
214 Eq. 6 
$$RT \ln \gamma_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}} = X_{\text{Mg}_2\text{SiO}_4}^2 W_{\text{Fe-Mg}}^{\text{oliv}}$$

215  
216  
217 Eq. 7 
$$a_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}} = [X_{\text{Fe}_2\text{SiO}_4} \gamma_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}]^2$$

218  
219 Where R is the universal gas constant, T is the temperature in K, and  $W_{\text{Fe-Mg}}^{\text{oliv}}$  is the binary interaction  
220 parameter that assumes a value of 2.3 kJ mol<sup>-1</sup>. The activity of the magnetite component of the spinel was  
221 calculated using the solution model of Nell and Wood (1990) which was given in an empirical form by  
222 Wood (1991) as:

223  
224 Eq. 8 
$$\log a_{\text{Fe}_3\text{O}_4}^{\text{sp}} = \left( \frac{(\text{Fe}^{2+})(\text{Fe}^{3+})}{4} \right)^2 + \frac{1}{T} [406(\text{Al})^2 + 653(\text{Mg})(\text{Al}) + 299(\text{Cr})^2 + 199(\text{Cr})(\text{Al}) + 463(\text{Mg})(\text{Cr})]$$

225  
226 where the element in parenthesis refers to the number of cations present per spinel formula unit normalized  
227 to four oxygen anions. Ferric and ferrous ratios and cation site occupancy calculations follow the procedure  
228 of the SPINCALC spreadsheet (found at <http://www.gabbrosoft.org>); the SPINCALC charge balance and  
229 normalization procedure is implemented into the python code and applied to the classical OSaS.

230 In addition to the classical-OSaS method described above, the MELTS algorithm can also be  
231 applied to the olivine-spinel- $a_{\text{SiO}_2}^{\text{melt}}$  equilibrium in a slightly different, though more fundamental way. Rather

232 than using MELTS to obtain  $a_{\text{SiO}_2}^{\text{melt}}$  values for use in Eq. 2, MELTS can alternatively be used in a second  
233 implementation of Eq. 2 to directly calculate the chemical potentials of the fayalite endmember in the  
234 olivine solution of interest, the magnetite endmember of spinel solution of interest, and  $\text{SiO}_2$  in the melt of  
235 interest. This approach has the advantage of using the internally consistent solution models and  
236 thermodynamic dataset intrinsic to the MELTS software. Chemical potentials calculated from MELTS can  
237 be arranged to define  $f_{\text{O}_2}$  as follows:

238

239 Eq. 9 
$$\mu_{\text{O}_2}^{\text{sys}} = 3\mu_{\text{SiO}_2}^{\text{melt}} + 2\mu_{\text{Fe}_3\text{O}_4}^{\text{sp}} - 3\mu_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$$

240

241 where the chemical potential  $\mu_{\text{O}_2}^{\text{sys}}$  obtained from Eq.5 can be converted into oxygen fugacity, using the  
242 standard state thermodynamic data for  $\text{O}_2$  reported in the JANAF tables (Chase, 1998), as in Eq. 10:

243

244 Eq. 10 
$$\mu_{\text{O}_2}^{\text{sys}} - \mu_{\text{O}_2}^{\circ} = RT \ln f_{\text{O}_2}$$

245

246 The “MELTS-only” version oxybarometer described above (hereafter referred to as the MELTS-OSaS  
247 oxybarometer) has the advantage of using solution models and a thermodynamic data set that are internally  
248 consistent. As such, the solution models for olivine and spinel endemic to this approach are different than  
249 the models implemented in the previous form of the classical-OSaS oxybarometer. MELTS calculations  
250 employ the Sack and Ghiorso (1989) olivine solution model for the calculation of  $\mu_{\text{Fe}_2\text{SiO}_4}^{\text{oliv}}$  and the Sack  
251 and Ghiorso (1991) spinel solution model for the calculation of  $\mu_{\text{Fe}_3\text{O}_4}^{\text{sp}}$ .

252

#### 253 **4. Evaluating the OSaS Oxybarometers: Calculating the Oxygen Fugacity Recorded by Olivine-** 254 **Spinel-Glass Sets in Redox Controlled Phase Equilibrium Experiments**

255 Although the two versions of the OSaS oxybarometer described above should in principle generate  
256 accurate magmatic oxygen fugacity data for equilibrium olivine-spinel pairs, we stress that both approaches  
257 still require a rigorous test before being applied to ‘real world’ magmatic redox studies. The primary  
258 objective of this work is to develop a working oxybarometer that can be applied to cotectic olivine-spinel  
259 ( $\pm$ glass) assemblages in holocrystalline basalts that lack phase assemblages amenable to other established  
260 oxybarometers. To assess the efficacy of each of the approaches, we apply each method to a suite of redox  
261 buffered phase equilibrium experiments drawn from the literature. We used the Library for Experimental  
262 Phase Relations (LEPR) (Hirschmann et al., 2008) and conducted a literature search to identify an initial  
263 set of validation experiments which (1) contained olivine-spinel-liquid phase assemblages and (2) were  
264 conducted at controlled  $f_{\text{O}_2}$ . In total, we identified 223 experiments from 33 experimental studies. The bulk



265 compositions of the starting materials used in these experiments range in composition from alkaline to  
266 subalkaline and from mafic to intermediate.

#### 267 4.1 Filtering Experimental Dataset

268 From this initial dataset we omit experiments with spinel analyses that contain >0.7 wt% SiO<sub>2</sub> to  
269 reduce any interference of groundmass glass contamination for calculation of spinel component activities.  
270 We also filtered the for experiments that contained olivine-melt pairs with  $K_d^{\text{oliv-melt}}_{\text{Fe-Mg}}$  values consistent with  
271 the attainment of equilibrium. For melt compositions low in total alkali content, we only selected  
272 experiments in which  $K_d^{\text{ol-melt}}_{\text{Fe-Mg}}$  values vary between 0.30±0.08 (Fig. 1A). Lower  $K_d^{\text{ol-melt}}_{\text{Fe-Mg}}$  values were  
273 accepted for melts that contained higher concentrations of alkalis (Fig. 1A), as it has been shown that  
274 increasing alkali content and decreasing silica activity effectively depress  $K_d^{\text{oliv-melt}}_{\text{Fe-Mg}}$  values (Toplis, 2005).  
275 We intentionally employ a wide filter for the olivine  $K_d^{\text{oliv-melt}}_{\text{Fe-Mg}}$  values, as our goal is to test the oxygen  
276 barometers across a spectrum of liquid compositions with variable silica activities.

277 We also evaluated experiments for the attainment of equilibrium between spinel and olivine.  
278 Depending on the choice of experimental starting material, it is possible for experiments to inherit relict  
279 spinel crystals that are out of equilibrium with the olivine and liquid present in the experiment.  
280 Disequilibrium or un-melted spinel crystals may remain in experimental phase assemblages because of  
281 sluggish re-equilibration kinetics or short experimental run times, which may be required to maintain a  
282 viable redox buffer assemblage. We use an empirical approach to filter out experiments that contain  
283 disequilibrium spinel. The distribution of Fe<sup>2+</sup> and Mg between olivine and spinel can be described with the  
284 exchange equilibrium:

285

286 Eq. 11 
$$X_{\text{Mg}}^{\text{ol}} + X_{\text{Fe}^{2+}}^{\text{sp}} = X_{\text{Fe}^{2+}}^{\text{ol}} + X_{\text{Mg}}^{\text{sp}}$$

287

288 Unlike olivine, a single canonical Fe-Mg exchange coefficient cannot be ascribed to olivine-spinel pairs.  
289 We found that within the experimental dataset, the Fe<sup>2+</sup>-Mg exchange coefficient depends primarily on the  
290 Al-content of the spinel (Fig. 1B). We also examined the dataset for a potential relationship between  
291  $K_d^{\text{ol-sp}}_{\text{Fe}^{2+}\text{-Mg}}$  and Cr content of the spinel, however, we found no significant correlation. The calculated  
292  $K_d^{\text{ol-sp}}_{\text{Fe}^{2+}\text{-Mg}}$  values increase with increasing Al content (Fig. 1B) for the dataset and fall on a linear trend  
293 described by:

294

295 Eq. 12 
$$K_D^{\text{ol-sp}}_{\text{Fe}^{2+}\text{-Mg}} = 0.249X_{\text{Al}} + 0.034$$

296

297 Where  $X_{Al}$  is the number of Al cations per spinel formula unit (normalized to four oxygen anions). The  
298 observed relationship between  $K_d^{ol-sp}_{Fe^{2+}-Mg}$  and the identity of the dominate cation occupying the octahedral  
299 site ( $Al^{3+}$ ,  $Cr^{3+}$ , or  $Fe^{3+}$ ) in the spinel is consistent with the reciprocal solution behavior exhibited by spinel  
300 (Wood and Nicholls 1978), as well as the results of previous studies of olivine-spinel partitioning (Evans  
301 and Frost, 1975). The linear trend described by Eq. 12 may be thought of as an apparent equilibrium trend,  
302 and as such is a useful tool for evaluating whether a given olivine-spinel pair represents an equilibrium  
303 assemblage. Using this criterion, we discarded eleven experiments that contained olivine-spinel pairs that  
304 plotted off the apparent equilibrium  $K_D$  trend ( $\pm 0.1$ ). We show the linear fit of the initial and filtered dataset  
305 in Fig. 1B to highlight the minimal change imparted to the fit after removing disequilibrium spinels.

306 Accurate control of oxygen fugacity is a fundamentally challenging problem in experimental petrology  
307 (Grove, 1981). Reported oxygen fugacity values from 1-bar gas mixing experiments are typically accurate,  
308 as they can be directly assessed with yttrium- or calcium-stabilized zirconia oxygen sensors. However,  
309 higher pressure experiments that rely on double capsule techniques that employ solid mineral redox buffer  
310 assemblages may either fail to achieve redox equilibrium or fail to maintain redox equilibrium over the  
311 duration of the experiment. It is difficult to assess the quality of literature-reported  $fO_2$  values or their  
312 affiliated uncertainties (if reported), however, we have attempted to identify experiments from the dataset  
313 that likely failed to attain or maintain redox equilibrium using a simple test based on calculated values of  
314  $a_{SiO_2}^{melt}$ . In this “reasonableness” test, we initially assume that each experiment was buffered at the reported  
315  $fO_2$ , and then we solve for the  $a_{SiO_2}^{melt}$  using a rearranged form of Eq. 2 (Fig. 1C). We find that  $a_{SiO_2}^{melt}$  values  
316 generated for many experiments plot in petrologically unreasonable regions of temperature- $a_{SiO_2}^{melt}$  space.  
317 We identified experiments where  $\log_{10} a_{SiO_2}^{melt} < 0.25$  or  $\log_{10} a_{SiO_2}^{melt} > 0.75$  as being suspicious, as the phase  
318 assemblages in these experiments are inconsistent with such extreme silica activity values. For example,  
319 experiments that return  $\log_{10} a_{SiO_2}^{melt}$  values  $> 0.75$  ( $-\log_{10} a_{SiO_2}^{melt} = -0.15$ ) should contain orthopyroxene as a  
320 liquidus phase instead of olivine (Fig. 1C) and other samples that plot above  $\log_{10} a_{SiO_2}^{melt} = 1$  should be  
321 saturated with a crystalline  $SiO_2$  polymorph which is inherently incompatible with the presence of olivine  
322 phenocrysts. Likewise, experiments that have  $\log_{10} a_{SiO_2}^{melt}$  values  $< 0.25$  ( $-\log_{10} a_{SiO_2}^{melt} = -0.60$ ) plot below  
323 perovskite-sphene silica buffer curve in the stability field of feldspathoid group minerals. Rare terrestrial  
324 rocks such as olivine melilites and extraterrestrial basalts (such as angrite meteorites) may have  
325  $\log_{10} a_{SiO_2}^{melt} < 0.25$ , however, the bulk compositions of the experiments considered for the calibration dataset  
326 bear no resemblance to these exotic compositions. The silica activity test allows us to directly assesses  
327 consistency of  $a_{SiO_2}^{melt}$  values constrained by thermodynamic analysis of *independent* peritectic reactions. The  
328 presence or absence of orthopyroxene, quartz, or nepheline in the experimental phase assemblages

329 effectively constrains the range of permissible silica activity values vis a vis the pertinent  $a_{\text{SiO}_2}^{\text{melt}}$  buffer  
330 reactions. In other words, this test is effectively a comparison of  $a_{\text{SiO}_2}^{\text{melt}}$  values calculated with the OSaS  
331 reaction to  $a_{\text{SiO}_2}^{\text{melt}}$  constraints from other mineral-melt reactions that define silica activity. We emphasize that  
332 experiments are not excluded on their  $a_{\text{SiO}_2}^{\text{melt}}$  value alone. Rather, this test excludes experiments that have  
333  $a_{\text{SiO}_2}^{\text{melt}}$  values that are inconsistent with reported phase assemblage of the experimental charge in question.  
334 For example, an experimental melt that does not contain quartz cannot have an  $\log_{10} a_{\text{SiO}_2}^{\text{melt}} > 1.0$ . The  
335 extreme high and low  $a_{\text{SiO}_2}^{\text{melt}}$  values obtained for the experimental melts may be attributed to several factors,  
336 including: (1) inaccurate spinel analyses, (2) unrecognized compositional zoning in olivine, or (3) a failed  
337 redox buffer assemblage. We omit these experiments from our calibration dataset, as some component of  
338 the olivine-spinel- $a_{\text{SiO}_2}^{\text{melt}}$ - $f\text{O}_2$  system reflects disequilibrium, where the mineral assemblage reported in the  
339 run products is inconsistent with the mineral assemblage predicted by the calculated values of  $a_{\text{SiO}_2}^{\text{melt}}$ . After  
340 culling the experimental dataset using the olivine-spinel  $\text{Fe}^{2+}$ -Mg exchange coefficient test and the  $a_{\text{SiO}_2}^{\text{melt}}$   
341 “reasonableness” test, our final dataset consists of 50 experiments on natural liquids.

342 In total, 19 experiments failed the olivine and liquid  $\text{Fe-Mg}K_D$  test; of those 19 experiments two  
343 experiments also failed the test of olivine-spinel equilibrium, and 11 also failed the  $a_{\text{SiO}_2}^{\text{melt}}$  test. Eleven  
344 experiments failed the test of olivine-spinel equilibrium, where two of the 11 experiments also failed the  
345 olivine and liquid  $\text{Fe-Mg}K_D$  test and one of the 11 experiments failed the  $a_{\text{SiO}_2}^{\text{melt}}$  test. Finally, 91 experiments  
346 failed the  $a_{\text{SiO}_2}^{\text{melt}}$  test, meaning that their calculated values of  $a_{\text{SiO}_2}^{\text{melt}}$  suggest that the experiments should be  
347 saturated in feldspathoids, orthopyroxene or quartz, but neither of these phases are reported in the run  
348 products. A single experiment failed all three tests. We note that all olivine-spinel pairs in our culled dataset  
349 are also consistent (within  $\pm 0.1$ ) with the olivine-spinel equilibrium proposed by Li et al. (1995), which  
350 accounts for variations in temperature. The final data set includes liquid compositions that range from  
351 basanite to andesite (Fig. 2) (Supplemental Data Table S1).

## 352 4.2 Evaluating the Performance of the Classical OSaS Oxybarometer

353 We used the activities of olivine and spinel, and the  $a_{\text{SiO}_2}^{\text{melt}}$  values relative to tridymite (using Eq. 5)  
354 for the experimental glasses and the  $\Delta_r G^\circ$  values based on the Berman (1988) database to solve for  $f\text{O}_2$   
355 based on Eq. 2. We find that this approach generates  $f\text{O}_2$  values for the experiments in the initial validation  
356 dataset with an RMSE of  $\pm 0.40$  log units, a standard error estimate of  $\pm 0.39$  log units and an average  
357 residual (the average of the absolute values of the residual for each experiment) of  $\pm 0.31$  log units (Fig.  
358 3A). We find a few weak patterns in the residuals of the OSaS oxybarometer (Fig. 4), however, all the  
359 residual slopes appear to be negligible within the average residual of the model. The greatest trend is  
360 associated with  $\text{H}_2\text{O}$  content, which cannot be deconvolved from pressure in experiments in the test dataset.

361 For melts from experiments conducted at high water contents and high pressures, the model systematically  
362 underestimates the reported  $fO_2$  values (Fig. 4C). We also find there is a weak correlation between the  $fO_2$   
363 residual and both melt and olivine compositions, such that the model systematically underestimates  $fO_2$  for  
364 silica-rich liquids and forsterite-rich olivine (e.g., Fo<sub>90</sub>; Fig. 4D), however, we stress that these correlations  
365 are weak and are smaller in magnitude than the average residual of the model. We suggest that the classical  
366 OSaS model should not be applied to olivine-spinel-glass assemblages with melts that contain more than  
367 10 wt.% H<sub>2</sub>O.

368

### 369 4.3 Evaluating the Performance of the MELTS-OSaS Oxybarometer

370 We used the MELTS algorithm to calculate the chemical potentials of spinel, olivine, and SiO<sub>2</sub> in  
371 the melt using compositions, temperatures, and pressures reported for the experiments included in the culled  
372 evaluation dataset. The resultant chemical potentials were inserted into Eq. 9 to obtain  $\mu_{O_2}$ , which we then  
373 converted into an  $fO_2$  using Eq. 10. The MELTS-OSaS approach reproduces  $fO_2$  values of the initial  
374 validation dataset with an average residual of +0.76 log units. The MELTS-OSaS approach systematically  
375 underpredicts the  $fO_2$  of experiments with equilibrium spinel compositions that are enriched in chromium  
376 and aluminum (Fig. 5).

377 This result suggests that we have identified an equilibrium for which the internally consistent  
378 MELTS model does not reproduce the experimental data with an acceptable margin of error. At the most  
379 fundamental level, the mismatch between the experimental and predicted  $fO_2$  values is reflected by a deficit  
380 chemical potential calculated for the reaction of interest (Eq. 9). There are two potential sources of this  
381 deficit (1) the standard state  $\mu^\circ$  values used for any of the end-member phases or (2) the chemical potential  
382 associated with the excess mixing properties derived from the solution model of choice (we also stress that  
383 these two possibilities are not mutually exclusive). Given the internal consistency of the Berman  
384 thermodynamic dataset that underpins the MELTS OSaS and the fact that it faithfully reproduces  
385 experimentally determined equilibrium  $fO_2$  values of the fayalite-magnetite-quartz buffer, there is no  
386 evidence implicating the standard state properties as the source of the observed error. Therefore, it is likely  
387 that the source of the error is related to the mixing properties defined by either the olivine or spinel solution  
388 model.

#### 389 4.3.1 Source of the energy deficit in the MELTS OSaS equilibrium: olivine or spinel?

390 The observed MELTS OSaS chemical potential deficit can potentially be attributed to deficiencies  
391 values of  $\mu_{Fe_3O_4}^{sp}$  or  $\mu_{Fe_2SiO_4}^{oliv}$  predicted by the spinel and olivine solution models, respectively. We evaluate  
392 which phase is the source of the energy deficit by comparing the residuals from the MELTS OSaS model  
393 (known-predicted values of  $\log fO_2$ ) as a function of the compositions of olivine and spinel (Fig. 6). We  
394 find that the residuals from the MELTS OSaS show the strongest correlations with the composition of the

395 spinel, in particular the Cr-content and Cr# (residuals vs. Cr# yield  $R^2 = 0.45$ ,  $p\text{-value} = 9.8 \times 10^{-8}$ ; Fig. 6A),  
396 where the lowest residuals coincide with spinel compositions with low concentrations of Cr. Furthermore,  
397 we find that the average residual for the nine experiments that have spinel compositions with  $\text{Cr}\# < 0.01$  is  
398  $+0.24$  log units which suggests that the MELTS OSaS model performs well for spinel compositions that  
399 are effectively binary  $\text{MgAl}_2\text{O}_4\text{-Fe}_3\text{O}_4$  or  $\text{Fe}_2\text{TiO}_4\text{-Fe}_3\text{O}_4$  mixtures. In contrast, residuals show a much  
400 weaker correlation with olivine composition (residuals vs. mol% fayalite yields  $R^2 = 0.15$ , which is reduced  
401 to 0.07 if a single, fayalite-rich olivine at the far right-hand side of the fit is discarded; Fig. 6B). We also  
402 note that when the Sack and Ghiorso (1989) solution model is used in the internally consistent MELTS  
403 architecture, it has been demonstrated that it successfully reproduces a preponderance of the experimental  
404 phase equilibrium data on which it was evaluated. The broad success of the Sack and Ghiorso (1989) olivine  
405 solution model within the MELTS architecture is a strong argument that the observed chemical potential  
406 deficit is not, in fact, related to a mishandling of the olivine solution properties.

407 The observed correlations between spinel composition and residuals suggest Cr parameterization  
408 of Sack and Ghiorso (1991b) - which was meant to extend to the original Sack and Ghiorso (1991a) model  
409 for Fe-Mg-titanomagnetite-aluminate spinel to Cr-bearing compositions - underpredicts magnetite activity  
410 for spinel compositions that contain a chromite component. We emphasize that composition space for spinel  
411 is large and that the solution properties of spinel are exceedingly complicated. The configurational entropy  
412 of normal-inverse spinel solutions is impacted by temperature-dependent ordering on the cation sublattice;  
413 therefore, spinel solution models contain provisions to predict configurational entropy for a given  
414 composition. Magnetite activity values are influenced solution model implicit parameters that account for  
415 compositionally driven variations in cation distributions (i.e., the inversion parameter and its temperature  
416 dependence). Kurepin (2005) re-evaluated degree of inversion and cation mixing across the chromite-  
417 magnetite binary with new lattice parameter data and found that the Sack and Ghiorso (1991b) Cr extension  
418 overestimates the inversion parameter for Cr bearing compositions. The Kurepin (2005) work suggests that  
419 that the inversion parameter is nearly zero for spinel that contain dilute magnetite concentrations (i.e.,  $< 25$   
420 mol. %  $\text{Fe}_3\text{O}_4$ ). If this is correct, then the overestimation of the inversion parameter results in configurational  
421 entropy estimates that are too high, which would translate to  $a_{\text{Fe}_3\text{O}_4}^{\text{SP}}$  values that are too low. The use of low  
422  $a_{\text{Fe}_3\text{O}_4}^{\text{SP}}$  in OSaS equilibrium will, by extension generate  $f\text{O}_2$  values that are also too low, which is consistent  
423 with the observed behavior of the residuals for experiments that contain Cr spinel.

424

#### 425 *4.3.2 Correction to $\mu\text{Fe}_3\text{O}_4$ values*

426 We developed an empirical correction that can be applied to the  $\mu\text{Fe}_3\text{O}_4$  values generated by  
427 MELTS. This correction effectively increases the MELTS-derived  $\mu\text{Fe}_3\text{O}_4$  values to bring them into

428 equilibrium with the reported  $fO_2$  values for the experiments in the initial validation dataset. The equilibrium  
429 values for  $\mu_{Fe_3O_4}$  (i.e.,  $\mu_{Fe_3O_4}^{spinel-eq}$  in Eq. 13 below) can be obtained by rearranging Eq. 9 such that:

430

431 Eq.13 
$$\mu_{Fe_3O_4}^{spinel-eq} = -(3\mu_{SiO_2}^{melt} - 3\mu_{Fe_2SiO_4}^{olivine} - \mu_{O_2})/2$$

432

433 We conducted a multivariate linear regression to relate the difference in the equilibrium  $\mu_{Fe_3O_4}^{spinel}$  values  
434 ( $\mu_{Fe_3O_4}^{spinel-eq}$ ) and MELTS  $\mu_{Fe_3O_4}^{spinel}$  values to the composition of the spinel (as mole fractions of oxide  
435 components). We systematically removed inconsequential compositional terms from the regression until  
436 we reached a combination of statistically significant terms and a low standard error on the regression fit.  
437 We find that the intercept, the initial, uncorrected value of  $\mu_{Fe_3O_4}$  from MELTS, and a subset of oxide  
438 “components” ( $X_{Cr_2O_3}$ ,  $X_{MgO}$ ,  $X_{FeOT}$ ) are all significant terms (p-values  $\leq 0.02$ ) (Table 1; Fig. 7A) and the  
439 model fit reproduces the idealized  $\mu_{Fe_3O_4}$  values with a standard error estimate of  $\pm 4.816$  kJ, which is  
440 equivalent to an uncertainty of  $\pm 0.17$  log units of  $fO_2$ . Seven significant figures are required for each of the  
441 regression coefficients, as using less than the seven significant figures (i.e., rounding) will result in  $\mu_{Fe_3O_4}$   
442 that are insufficiently precise for calculating accurate  $fO_2$  values. It is also important to note that the  
443 corrected equilibrium  $\mu_{Fe_3O_4}$  values obtained through this regression cannot be reincorporated into the  
444 MELTS algorithm, as they are no longer internally consistent with supporting model parameters. Using the  
445 newly derived regression equation (Table 1) to calculate  $\mu_{Fe_3O_4}$  from MELTS outputs, we find that the  
446 MELTS OSaS can successfully reproduce the  $fO_2$  values for the experimental dataset with a SEE of  $\pm 0.35$   
447 log units. Additionally, we find no significant patterns in the residuals as a function of spinel composition  
448 (Fig. 7B).

449 To understand the error of the MELTS-OSaS oxygen barometer, we must apply it to experiments  
450 that were not used to calibrate the correction to  $\mu_{Fe_3O_4}$ . We identified an additional 18 experiments that  
451 were not either (1) not found during our initial, imperfect, search of the LEPR database and literature or (2)  
452 were published after the initial testing and calibration of the MELTS-OSaS oxybarometer (Supplemental  
453 Table S2). This additional test dataset includes the experiments of Gaetani et al. (1994), Melekova et al.  
454 (2017), Takagi et al. (2005), Krawczynski et al. (2012) and Zhang et al. (2023). We have applied the  
455 MELTS-OSaS oxybarometer to predict the  $fO_2$  values of these experiments and found that the MELTS-  
456 OSaS with a corrected  $\mu_{Fe_3O_4}$  returns  $fO_2$  values for most of these experiments with of  $\pm 0.23$  log units, a  
457 standard error estimate of  $\pm 0.20$  log units and an average residual (the average of the absolute values of the  
458 residual for each experiment) of  $\pm 0.18$  log units (Fig. 7C).

459 We additionally tested this model on experiments on picritic melts with  $>10$  wt.% MgO from  
460 Matzen et al. (2011) and Zhang et al. (2023) (which pass all filters but were not included in either of the  
461 preceding experimental datasets; Supplemental Table S3). We found that both the MELTS-OSaS and the

462 classical-OSaS models overestimate the  $fO_2$  of picritic liquids by an average of +0.29 log units and by +0.42  
463 log units, respectively (Supplemental Fig. S1). We observe that this effect is confined to liquid compositions  
464 containing >10.0 wt. % MgO. This effect suggests that MELTS systematically overpredicts  $a_{SiO_2}^{melt}$  values  
465 for liquid compositions enriched in normative olivine, therefore, we caution users to be cognizant of the  
466 small, albeit systematic,  $fO_2$  bias imparted to MgO-rich liquids.

467 We find a few weak patterns in the residuals for the validation dataset (Fig. 8A-D), but the  
468 magnitudes of the correlation slopes are negligible within the average residual of the model and lower in  
469 magnitude than those of the classical OSaS oxybarometer for a given parameter. The model has some  
470 pattern in residual with increasing  $SiO_2$  concentration (Fig. 8A) and  $H_2O$  content (Fig. 8C) of the coexisting  
471 melt, both of which impact the activity of silica parameter used in the model. Like the classical OSaS  
472 oxybarometer, the residuals associated with the MELTs OSaS oxybarometer indicate that the model  
473 satisfactorily reproduces the evaluation dataset. The model's performance is significantly degraded for  
474 olivine-spinel-glass assemblages that grew from extremely  $H_2O$  rich melts (e.g., > 10 wt.%). Therefore, as  
475 with the classical OSaS oxybarometer, we strongly caution against applying the MELTS OSaS model to  
476 water-rich systems, as it may produce inaccurate results.

477 In general, the  $fO_2$  values generated from the two models are in good agreement when considering  
478 the error estimates of both models (Fig. 9). The mean difference in  $fO_2$  predicted by the two models for the  
479 18 experiments used to test the MELTS-OSaS barometer is -0.12 log units and the average absolute value  
480 of the difference in the  $fO_2$  predicted by the two models is 0.2 log units.

481

## 482 **5. Uncertainties and Limitations of the Classical and MELTS OSaS Oxybarometers**

483 The advantage to testing the classical-OSaS and MELTS-OSaS oxybarometers on experiments is  
484 that they are conducted at known temperatures, pressures, and water contents. As the goal of this work is  
485 to provide a method for estimating  $fO_2$  in natural samples, we have also attempted to evaluate how well the  
486 model performs when intensive and compositional variables are not well known. Temperature exerts a  
487 principal control  $\Delta_rG^\circ$  values that appear in Eq. 2, as well as (though to a lesser extent) the mineral and melt  
488 activities calculated from the solution models. Both OSaS formulations are mildly dependent on pressure  
489 and the dissolved  $H_2O$  content of the liquid of interest. Like temperature, pressure also directly impacts  $\Delta_rG$   
490 for the reaction of interest, as well as the  $a_{SiO_2}^{melt}$  value calculated from MELTS. The dissolved water content  
491 of the melt exerts considerable influence on the  $a_{SiO_2}^{melt}$  (Carmichael 1970), where increasing water content  
492 depresses the silica activity of the melt, which in turn decreases the calculated oxygen fugacity values. We  
493 also note that  $CO_2$  has a minor effect on  $a_{SiO_2}^{melt}$ , however, the magnitude of this effect is insignificant  
494 compared to  $H_2O$ . Varying  $CO_2$  content from 0 to 2000 ppm changes the  $a_{SiO_2}^{melt}$  value by 0.003.

495           Uncertainties in the composition of the equilibrium liquid coexisting with olivine and spinel may  
496 impact the calculated  $a_{\text{SiO}_2}^{\text{melt}}$  value, however, we stress that uncertainties in the  $a_{\text{SiO}_2}^{\text{melt}}$  obtained for tholeiites  
497 and olivine tholeiites ( $a_{\text{SiO}_2}^{\text{melt}}$  ranging from 0.45 to 0.65) exert minimal leverage on the  $f\text{O}_2$  values returned  
498 by the model. To illustrate this point, we have performed a sensitivity analysis that shows uncertainties in  
499 the  $a_{\text{SiO}_2}^{\text{melt}}$  of  $\pm 0.05$  (a reasonable assumption for the effects uncertainties in the input liquid composition)  
500 generate a response in the returned  $f\text{O}_2$  value of approximately  $\pm 0.10$  log units (Fig. 9), which is  
501 significantly smaller than the error estimate of either model. This analysis highlights an important feature  
502 intrinsic to the OSaS approach - namely that a reasonable approximation of the input liquid composition  
503 may be sufficient for applying the models to  $f\text{O}_2$  calculations of basaltic lavas. In other words, small errors  
504 in the input liquid composition are not translated into significant errors in the calculated  $f\text{O}_2$  values for  
505 tholeiites and olivine tholeiites. For liquids with high  $a_{\text{SiO}_2}^{\text{melt}}$  values, silica activity is effectively a variable  
506 of second order importance. On the other hand, for liquid compositions that have low  $a_{\text{SiO}_2}^{\text{melt}}$  values that  
507 characterize basanites and feldspathoidal basalts, it is clear that  $a_{\text{SiO}_2}^{\text{melt}}$  exerts significant leverage on the  
508 resultant  $f\text{O}_2$  values (Fig. 10). Therefore, caution should be exercised in applying the OSaS to silica-  
509 undersaturated magmas with poorly constrained melt compositions. Though the OSaS models were  
510 successfully applied experiments performed on basanites and alkali-rich compositions, we suggest that the  
511 models are best applied to magmas with  $a_{\text{SiO}_2}^{\text{melt}} > 0.35$  to minimize errors related to intrinsic uncertainties  
512 associated with the silica activity values.

513           We explored the impact of uncertainties in pressure, temperature, and dissolved water content on  
514 the  $f\text{O}_2$  values calculated from the OSaS formulations by performing a sensitivity test using the olivine-  
515 spinel-glass assemblage from an experiment reported in Grove et al. (2003) (their experiment 85-41c#7).  
516 The olivine-spinel and liquid compositions were supplied to the oxybarometers and the assumed values for  
517 temperature, pressure, and water content were systematically varied. We find that, for the classical-OSaS  
518 oxygen barometer, if temperature is known within  $\pm 25^\circ\text{C}$  (at a constant pressure of 200 MPa), the  
519 uncertainty in  $f\text{O}_2$  is approximately  $\pm 0.3$  log units (Fig. 11). Increasing the water content of the melt at  
520 constant pressure (200 MPa) and temperature, from 1.0 wt. % to 5.0 wt%, generates a decrease in the  
521 calculated  $f\text{O}_2$  of  $\sim 0.40$  log units (Fig. 11A). At a constant temperature of  $1050^\circ\text{C}$  and dissolved  $\text{H}_2\text{O}$  content  
522 of 4 wt. %, the effect of increasing pressure from 100 to 500 MPa generates an increase in the model  
523 calculated  $f\text{O}_2$  value of less than 0.3 log units. We find similar uncertainties with respect to the effects of  
524 temperature, dissolved  $\text{H}_2\text{O}$  content, and pressure when repeating the same test for the MELTS-OSaS  
525 oxybarometer (Fig. 11C&D). Provided that one can estimate the crystallization temperature of olivine-  
526 spinel pairs to a precision of  $\pm 25^\circ\text{C}$  and the dissolved water content of the melt to  $\pm 1.5$  wt%, both OSaS  
527 models should return accurate  $f\text{O}_2$  values.



528

## 529 **6. Application of the OSaS to Natural Samples**

530 While the OSaS barometers yield accurate  $fO_2$  values for the experimental validation datasets, we  
531 have also applied the models to a suite of natural samples, where considerably less is known about the  
532 temperature-pressure- $H_2O$  conditions at the time of crystal growth. This application effectively serves as a  
533 “field” test that is intended to help establish whether the models generate reasonable estimates of  $fO_2$  for  
534 natural samples. We have attempted to apply the OSaS models to olivine-spinel-melt pairs from natural  
535 samples that have established values of  $fO_2$ , preferably through a method of determining  $fO_2$  other than a  
536 strictly thermodynamic approach (i.e., an evaluation of  $Fe^{3+}/\Sigma Fe$  from XANES or Mossbauer  
537 Spectroscopy). Though many spectroscopic works on  $Fe^{3+}/\Sigma Fe$  in glasses in melt inclusions often supply  
538 the composition of the host olivine, we cannot identify a study that also reports spinel compositions.  
539 Therefore, we target olivine- and spinel-bearing mafic rocks that have an existing  $fO_2$  estimates derived  
540 from  $Fe^{3+}/\Sigma Fe$  from XANES or Mossbauer Spectroscopy, which are from locations that also have a variety  
541 of samples with detailed petrologic descriptions and analyses of olivine, spinel, and glass.

542 It has long been recognized that the oxidations states recorded by basalt glasses from the midocean  
543 ridge (MORBs) provide a record of the oxidation state of their mantle source (Arculus, 1979; Christie et  
544 al., 1986; Haggerty, 1978). As such, there has been significant effort exerted in determining the  $Fe^{3+}/\Sigma Fe$   
545 of MOR glasses (Bézos & Humler, 2005; Christie et al., 1986; Cottrell & Kelley, 2011; O’Neill et al., 2018;  
546 Zhang et al., 2018), which can be converted to an oxygen fugacity using models from the literature  
547 (Jayasuriya et al., 2004; Kress & Carmichael, 1991; O’Neill et al., 2018). In general, the  $Fe^{3+}/\Sigma Fe$  measured  
548 for MORBs indicate that these basalts record an oxygen fugacity within approximately  $\pm 0.20$  log units of  
549 the fayalite-magnetite-quartz buffer (e.g.,  $\Delta FMQ + 0.10 \pm 0.18$ , Cottrell & Kelley, 2011;  $\Delta FMQ - 0.17 \pm 0.15$ ,  
550 Zhang et al. 2018;  $\Delta FMQ + 0.19 \pm 0.35$ , O’Neill et al., 2018) (Fig. 12). We examined literature associated  
551 with the Deep-Sea Drilling Project (DSDP) and identified studies that report compositions of olivine, spinel  
552 and matrix glasses from any midocean ridge. We found olivine, spinel and matrix glasses from the Costa  
553 Rican Ridge Zone (leg 70 sample 504B, Group J) (Natland et al., 1983) and from the Lau Basin (Hawkins  
554 & Melchior, 1985), which is a complex back arc basin situated between a subduction zone on its eastern  
555 side and back arc ridges on its western margin (Baker et al., 2019) (Supplemental Data Table S4). We note  
556 that within these studies, some metadata are reported for mineral analyses, such as location on the grain  
557 (i.e., core or rim) or if spinels were included in olivine, but reporting of these observations is not consistent  
558 from study to study. For the Lau Basin samples, Hawkins and Melchior (1985) and Kamenetsky et al.  
559 (1997) report temperatures for the rocks from their study using olivine-melt equilibrium and olivine-  
560 chromite equilibrium, and we adopt those temperatures [average from Hawkins and Melchior (1985) =  
561  $1190^\circ C$ ] for our application here, along with pressures of 0.1 MPa and  $H_2O$  contents of 0 wt.%. We find

562 that the classical and MELTS-OSaS barometers yield  $\log f_{\text{O}_2}$  values of  $-8.33 (\pm 0.1)$  and  $-8.42 (\pm 0.07)$ , which  
563 correspond to values of  $\Delta\text{QFM}+0.09$  and  $-0.02$ , respectively, for the Lau Basin Basalts. For the Costa Rican  
564 Ridge samples, Natland et al. (1983) report several olivine and spinel compositions for a given rock  
565 composition. We show the average oxygen fugacity ( $\pm 1\sigma$ ) for each sample based on all possible pairings  
566 of olivine and spinel for a given liquid composition, where we assume a temperature of  $1200^\circ\text{C}$ , a pressure  
567 of  $0.1\text{ MPa}$ , and  $\text{H}_2\text{O}$  content of  $0\text{ wt. \%}$  in our calculations (Supplemental Data Table S2). We find that the  
568 classical-OSaS and MELTS-OSaS barometers yield  $\log f_{\text{O}_2}$  values of  $-8.41 (\pm 0.24)$  and  $-8.47 (\pm 0.23)$ , which  
569 correspond to  $\Delta\text{FMQ}-0.11$  and  $-0.16$ , respectively, for the Costa Rican Ridge Basalts (Fig. 12). Overall, the  
570 oxygen fugacity values generated from the OSaS for these samples agree with the established redox range  
571 for MORBs from derived from other methods.

572 It is also widely accepted that volcanic rocks erupting from subduction zone settings are  
573 systematically more oxidized than midocean ridges (Carmichael, 1991; Cottrell et al., 2020), thus we aim  
574 to identify arc segments for which there is an estimate of magmatic oxygen fugacity using some  
575 spectroscopic method. Brounce et al. (2014) reports oxygen fugacity values derived from Fe K-edge  
576 XANES analyses for primitive volcanic glasses from Mariana trough and arc (Fig. 12). Brounce et al.  
577 (2014) found that elevated  $\text{Fe}^{3+}/\Sigma\text{Fe}$  ratios and low MgO contents of whole rock and glass compositions  
578 from the Mariana samples suggested that olivine fractionation had occurred prior to eruption. Therefore,  
579 Brounce et al. (2014) corrected the measured  $\text{Fe}^{3+}/\Sigma\text{Fe}$  to reflect the fractionation of olivine from the liquid  
580 using the model of Lee et al. (2009). We show  $\Delta\text{FMQ}$  values that correspond to the initial  $\text{Fe}^{3+}/\Sigma\text{Fe}$   
581 determined by spectroscopy and the  $\Delta\text{FMQ}$  values that correspond to  $\text{Fe}^{3+}/\Sigma\text{Fe}$  corrected for olivine  
582 fractionation. We applied the OSaS models to olivine-spinel-glass data from samples from the Mariana  
583 trough and arc from the literature (Bloomer & Hawkins, 1987; Hawkins & Melchior, 1985). Five samples  
584 from the Marianas trough have reported temperatures that range from  $1084\text{--}1197^\circ\text{C}$ , water contents of  $\sim 2$   
585 wt% to which we ascribe pressures of  $100\text{ MPa}$ . We find that the classical-OSaS and MELTS-OSaS  
586 oxybarometers yield redox estimates from  $\Delta\text{FMQ} +0.3$  to  $+1.3$  and  $+0.1$  to  $+1.5$ , respectively, for the  
587 samples from the Mariana Trough. One sample from the Mariana Arc (Bloomer & Hawkins, 1987) has a  
588 reported temperature of  $1200^\circ\text{C}$  and  $\text{H}_2\text{O}$  contents of  $\sim 2\text{ wt\%H}_2\text{O}$ , which we adopt for our tests  
589 (Supplemental Data Table S4). We assign pressure of olivine crystallization based on the  $\text{H}_2\text{O}$  contents  
590 reported for these samples ( $100\text{ MPa}$ ). The classical and MELTS-OSaS oxybarometers yield redox  
591 estimates from  $\Delta\text{FMQ} +1.9$  and  $+1.5$ , respectively, for the sample from the Mariana arc. The OSaS-  
592 determined redox conditions for the Mariana trough samples span a range that partially overlaps with the  
593 oxygen fugacities determined by Brounce et al. (2014), after olivine addition. The redox conditions for  
594 samples from the Mariana arc determined by OSaS barometer overlap well with those determined by  
595 Brounce et al. (2014).

596 OSaS-model  $fO_2$  estimates for basalts from the Mariana trough exceed the values determined by  
597 Brounce et al. (2014). We suspect this difference arises due to treatments of the different dataset; we do not  
598 correct the samples in our application for any olivine fractionation. The addition of olivine back into the  
599 Mariana trough samples to reconstruct primary liquid compositions will cause the oxygen fugacities in Fig.  
600 11 to decrease, towards those of Brounce et al. (2014). We find that the samples from the Mariana trough  
601 that yield the highest estimated values of  $fO_2$  also have the lowest MgO contents, suggesting that the olivine-  
602 spinel pairs could record evolving  $fO_2$  due to fractionation or melt-vapor separation. We emphasize that  
603 numerous redox processes (e.g., degassing, crystallization) occur in magmatic plumbing systems and that  
604 the compositions of olivine-spinel pairs may provide a valuable record of these processes. The similarities  
605 between the  $fO_2$  estimates from both the Classical and MELTS implementations of the barometers and those  
606 from spectroscopic studies lend considerable confidence to  $fO_2$  estimates produced by both  
607 implementations of the OSaS models. A caveat to both comparisons is that neither application involves  
608 precisely the same sample, however, we note that the  $fO_2$  values returned for each tectonic setting are  
609 consistent with the accepted values or those reported in the literature.

610

## 611 **7. Implications**

612 One potential application of these models is to evaluate the attainment of redox equilibrium that  
613 employ solid state buffer assemblages (e.g., the double capsule technique in piston cylinder experiments)  
614 in phase equilibrium and crystallization experiments performed on basaltic compositions. The new models  
615 offer an accessible method (i.e., one that only requires access to an electron microprobe) for experimental  
616 petrologists to ascertain if redox equilibrium was indeed achieved and maintained throughout the duration  
617 of an experiment.

618 More importantly, we envision that the OSaS models can potentially facilitate an expansion of  
619 magmatic redox studies to samples not amenable to XANES or Mossbauer measurements. Existing  
620 magmatic redox studies have been limited to a small number of samples from settings that produce copious  
621 quantities of glassy material, however tectonic settings (such as continental rifts) simply do not generate  
622 many glassy samples, and thus remain chronically understudied. Furthermore, the OSaS models provide an  
623 accessible alternative for researchers who need to generate magmatic redox data but lack access to  
624 synchrotron or Mossbauer facilities. We also stress that the OSaS models can serve a key role in cross  
625 checking  $fO_2$  values from olivine hosted melt inclusions or rapidly quenched samples derived from  
626 spectroscopic measurements against those with recorded cotectic olivine spinel pairs.

627 The application of the OSaS models to natural samples requires that potential users (1) identify  
628 equilibrium olivine-spinel pairs in the samples of interest, (2) estimate the cotectic temperature for the  
629 olivine-spinel pair, (3) obtain an estimate of the liquid in equilibrium with the olivine-spinel pairs, along

630 with the H<sub>2</sub>O content, and (4) have some constraint on equilibration pressure. Below we offer a few criteria  
631 and suggested methods to aid potential users in completing the aforementioned tasks. We recognize that  
632 this list of suggestions is not exhaustive and there are other potential methods approaches to assess  
633 equilibrium among the phases of interest, to obtain estimates for liquidus temperatures, and to estimate the  
634 water content of the melt. Potential OSaS users are under no obligation to employ our suggestions and are  
635 encouraged to adapt the tool to their purposes as they see fit, however, we stress that it is incumbent on  
636 potential users to exercise sound petrologic judgement when applying the OSaS models.

637 The identification of disequilibrium olivine-spinel pairs can be accomplished by comparing the  
638  $K_d^{\text{ol-sp}}_{\text{Fe}^{2+}\text{-Mg}}$  for the pair of interest with the values predicted by Eq. 12 and/or through the equilibrium  
639 evaluation of Li et al. (1995). Though this simple approach does not ensure that a given pair represents an  
640 equilibrium assemblage, it does serve as a rough filter to eliminate olivine-spinel pairs that are clearly out  
641 of equilibrium and will generate inaccurate  $f\text{O}_2$  values. We stress that olivine and Cr-spinel are often the  
642 first two liquidus phases in basalts that contain > 6.0 wt. % MgO. In such magmas, spinel is often present  
643 in the form of euhedral to subhedral inclusions in the cores of olivine phenocrysts (Roedder et al. 2006).  
644 These textures represent cotectic pairs that can be readily identified. We suggest that the OSaS models be  
645 applied to samples that experienced rapid cooling after eruption (e.g., surficial lava flows) to minimize  
646 potential subsolidus re-equilibration between olivine and spinel.

647 Of these tasks, obtaining accurate estimates for the olivine-spinel cotectic temperature is the least  
648 straightforward. There are several geothermometers that can be used to help estimate olivine-spinel cotectic  
649 temperatures (e.g., the olivine liquid geothermometers of Putrika, 2005; Herzberg and O'Hara, 2002),  
650 however we suggest that the Al in olivine geothermometer (Coogan et al., 2014; Wan et al., 2008) is well  
651 suited to estimate the crystallization temperature for an olivine-spinel pair of interest. The Al in olivine  
652 geothermometer is ideally suited for this task as it exploits the temperature dependence of the Al partition  
653 coefficient between olivine and spinel and can generate information about the cotectic temperature for the  
654 pair. We note that this approach does require careful consideration of EMP detection limits and analytical  
655 uncertainties for measured Al concentration of olivine. Thermometers based on Mg-Ni partitioning in  
656 olivine (e.g., Pu et al., 2017) may also prove useful for the OSaS, as this method can also provide estimates  
657 of pre-eruptive H<sub>2</sub>O contents, though we note that laser ablation inductively coupled mass-spectrometry  
658 (LA-ICPMS) may be required for successful application of this thermometer. We also suggest that if whole  
659 rock compositions are known, the “reasonableness” of the olivine-spinel temperature estimates can be cross  
660 checked against the MELTS-predicted liquidus temperature for the olivine composition of interest.

661 To determine the appropriate liquid composition in equilibrium with olivine spinel pairs for  
662 samples that lack glassy groundmass, we suggest that whole rock compositions could be used directly,  
663 depending if sample crystallinity is low or if it could be demonstrated that an olivine-spinel pair is in

664 equilibrium with the whole rock composition. Alternatively, the whole rock composition, mineral  
665 compositions, and mineral modes in a rock could be used to calculate a predicted interstitial liquid. In  
666 evaluating the combination of any liquid-crystal pair, some equilibrium test, such as the  $^{Fe-Mg}K_D$  values  
667 between olivine and melt, can be employed to assess the reasonableness of a selected melt composition.  
668 We do emphasize that one of the features of the OSaS model is that the uncertainties in the  $a_{SiO_2}^{melt}$  obtained  
669 for tholeiites and olivine tholeiites ( $a_{SiO_2}^{melt}$  ranging from 0.45 to 0.65), and therefore, the selected liquid  
670 composition, exert minimal leverage on the  $fO_2$  values returned by the model (Fig. 10). We provide a guide  
671 in Appendix 2 for arriving at estimates of melt compositions in equilibrium with phenocrysts, using whole  
672 rock compositions, mineral compositions, and modes for a Snake River Plane basalt.

673 For hydrous magmas, the implementation of the OSaS models depends on one being able to  
674 estimate the water content of the melt. In the absence melt inclusion data, we suggest that users estimate  
675 water content with plagioclase-liquid hygrometry (e.g., Putirka, 2008; Waters and Lange, 2015), or through  
676 microbeam studies of melt inclusions where possible. Pressure should be considered when applying the  
677 OSaS to non-experimental samples. Careful microbeam studies of dissolved volatiles (e.g.,  $CO_2$ ) in olivine-  
678 hosted melt inclusions may also provide constraints on the minimum pressure for olivine crystallization. In  
679 many cases it is difficult, if not impossible, to estimate the pressure at which olivine-spinel pairs grew from  
680 the liquid, however, we stress that pressure has only a minor effect on the OSaS-determined  $fO_2$  values for  
681 pressures < 500 MPa. As such, we strongly recommend that the OSaS should primarily to samples in which  
682 the olivine-spinel pairs generated by episodes of shallow crustal crystallization.

683 Finally, in the supplement, we provide all datasets, a python code with instructions to users, both  
684 the classical-OSaS and MELTS-OSaS models that can be uploaded to and used on the Thermoengine  
685 website, a benchmark input file that can be modified with a user's data and uploaded along with the python  
686 script, as well as benchmark summary output files for the different models. We encourage readers to utilize  
687 the instructions to users, as the code is designed to output all variables described in this work.

688

689

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695 manuscript.

696

697 Figure Captions:

698

699 Figure 1: (A) The olivine-liquid  $^{Fe-Mg}K_D$  values for olivine melt pairs from experiments are shown as a  
700 function of the total alkali content of the liquid, where the  $^{Fe-Mg}K_D$  values are calculated using the  $Fe^{2+}$   
701 contents in the glasses determined based on the reported temperature, pressures, oxygen fugacities, glass  
702 compositions and the empirically calibrated equation of Kress & Carmichael (1991). The  $^{Fe-Mg}K_D$  value of  
703 0.3 is shown as a solid black line and grey dashed lines correspond to the  $^{Fe-Mg}K_D$  of  $0.3 \pm 0.08$ . Anomalously  
704 high and low  $K_D$  values and those from experiments that failed additional tests (light colored symbols that  
705 fall above or below the dashed grey lines) were flagged as potentially representing poor analyses or  
706 disequilibrium. (B) The olivine-spinel  $^{Fe-Mg}K_D$  values calculated for the experimental dataset are shown as  
707 a function of the Al content of the spinel. Values that plot significantly ( $> \pm 0.1$ ) off the linear trend were  
708 discarded from the calibration. (C) A plot of the  $\log a_{SiO_2}^{melt}$  calculated using Eq. 2 rearranged to solve for  
709  $a_{SiO_2}^{melt}$  using the  $\Delta_r G^\circ$ ,  $a_{Fe_3O_4}^{sp}$ , the  $a_{Fe_2SiO_4}^{oliv}$  and the reported values of  $fO_2$ . Experiments that plot in the quartz  
710 stability field or plot in the feldspathoid stability field and lack those minerals in their reported run products  
711 were excluded from the calibration data set.

712

713 Figure 2: Experiments that passed all exclusionary criteria (e.g., Fig. 1) are shown as a function of their  
714  $SiO_2$  contents and total alkali contents to illustrate the compositional of the dataset. (Auwera & Longhi,  
715 1994; Barclay & Carmichael, 2004; Davis & Cottrell, 2018; Feig et al., 2010; Grove et al., 1997, 2003;  
716 Grove & Bryan, 1983; Grove & Juster, 1989; Kawamoto, 1996; Krawczynski et al., 2012; Médard & Grove,  
717 2008; Meen, 1987, 1990; Pichavant & Macdonald, 2007; Sack et al., 1987; Waters et al., 2021)

718

719 Figure 3: The reported  $fO_2$  values (i.e.,  $\log fO_2$  known) for the experimental dataset are shown with their  
720 calculated values of  $fO_2$  using the classical OSaS oxygen barometer. The symbols are color coded to  
721 represent the Cr content of the spinel composition used in the calculation. The classical OSaS model (using  
722 MELTS generated silica activity values referenced to tridymite and activity models from the literature)  
723 reproduces the experimental  $fO_2$  values with an average RMSE of  $\pm 0.40$  log units and an average residual  
724 of  $\pm 0.32$ . The  $fO_2$  values generated by the classical OSaS model do not covary with spinel composition.

725

726 Figure 4: In all panels, the residuals (known  $fO_2$ -modeled  $fO_2$ ) from the classical OSaS barometer are  
727 shown as a function of various input parameters: (A) wt. %  $SiO_2$ , where symbols are color coded to total  
728 alkali content, (B) experimental temperature, where symbols are color coded to experimental pressure  
729 (MPa), (C) dissolved water content of the melt, where symbols are color coded to experimental pressure  
730 (MPa), (D) Mg content of the experimental olivine, where symbols are color coded to the Cr#  
731 ( $X_{Cr}/(X_{Cr}+X_{Al})$ ) in spinel.

732

733 Figure 5: The reported  $fO_2$  values (i.e.,  $\log fO_2$  known) for the validation dataset are plotted against the  $fO_2$   
734 using the predicted MELTS-OSaS; this plot illustrates how the uncorrected version of MELTS-OSaS  
735 reproduces reported  $fO_2$  values for experiments that have spinel with low Cr concentrations and  
736 underpredicts  $fO_2$  values for experiments that have spinel with Cr content.

737

738 Figure 6: (A) The residuals from the MELTS OSaS are plotted against Cr# of the spinel; this plot shows a  
739 strong correlation between the Cr content of the spinel and the observed  $fO_2$  residual. (B) The residuals of  
740 the MELTS OSaS plotted against the mol. % fayalite in the olivine.

741

742 Figure 7: (A) The MELTS  $\mu Fe_3O_4$  values (black diamonds) and the corrected  $\mu Fe_3O_4$  values (grey circles)  
743 are shown, as a function of the equilibrium  $\mu Fe_3O_4$  values (i.e., the values of  $\mu Fe_3O_4$  required to successfully  
744 predict the experimental  $fO_2$  values). The  $\mu Fe_3O_4$  values directly output from MELTS fall below the 1:1  
745 line, indicating that they will under predict values of  $fO_2$ . The corrected  $\mu Fe_3O_4$  values match well with the  
746 1:1 line suggesting that they accurately reproduce the reported values of values of  $fO_2$ . (B) The reported  $fO_2$   
747 values (i.e.,  $\log fO_2$  known) for the experimental validation dataset are shown with their calculated values  
748 of  $fO_2$  using the calibrated MELTS OSaS with the corrected  $\mu Fe_3O_4$  values. (C) The reported  $fO_2$  values  
749 (i.e.,  $\log fO_2$  known) for 18 experiments from the studies of Krawczynski et al (2012), Gaetani et al. (1994),  
750 Takagi et al. (2005), Melekova et al. (2017), and Zhang et al. (2023) that were not a part of the initial  
751 validation/calibration dataset used to generate the  $\mu Fe_2O_3$  correction are plotted against the  $fO_2$  values  
752 predicted from the calibrated MELTS-OSaS model. MELTS-OSaS reproduces the 18 experimental  $fO_2$   
753 values with an average RMSE of  $\pm 0.23$  log units, a standard error estimate of  $\pm 0.20$ , and an average residual  
754 of  $\pm 0.18$ .

755

756 Figure 8: In all panels, the residuals (known  $fO_2$ -modeled  $fO_2$ ) from the MELTS OSaS model (with  $\mu Fe_3O_4$   
757 correction) are shown as a function of various input parameters: (A) wt.%  $SiO_2$ , where symbols are color  
758 coded to total alkali content, (B) experimental temperature, where symbols are color coded to experimental  
759 pressure (MPa), (C) dissolved water content of the melt, where symbols are color coded to experimental  
760 pressure (MPa), (D) Mg content of the experimental olivine, where symbols are color coded to the Cr#  
761 ( $X_{Cr}/(X_{Cr}+X_{Al})$ ) in spinel.

762

763 Figure 9: The  $fO_2$  values calculated for the experimental dataset from the classical OSaS model plotted  
764 against the values calculated from the MELTS-OSaS (with  $\mu Fe_3O_4$  correction). The plot shows a 1:1 line  
765 as well as the equation derived from a linear regression of the plotted data.

766

767 Figure 10: The curve in this figure shows how the OSaS predicted  $fO_2$  values vary as a function of  $a_{SiO_2}^{melt}$   
768 for a fictive olivine-spinel pair with fixed composition activity values and a fixed temperature of 1150°C.  
769 The symbols with the error bars on the curve illustrate the magnitude of the error in the predicted  $fO_2$  value  
770 assuming a that MELTS generated  $a_{SiO_2}^{melt}$  values have an intrinsic uncertainty of  $\pm 0.05$ . The  $a_{SiO_2}^{melt}$  and  $fO_2$   
771 values for the experimental validation dataset are superimposed on this plot to illustrate that most “basaltic”  
772 magma compositions (even alkali-rich basalts) characterized by  $a_{SiO_2}^{melt}$  values that correspond to low  
773 uncertainties in OSaS derived  $fO_2$  values.

774

775 Figure 11: (A) The effect of variable water content impacts the melts derived silica activity and the  
776 calculated  $fO_2$  values across a range of temperatures (at constant pressure of 200 MPa) for the classical-  
777 OSaS model. (B) The effect of pressure variation on calculated  $fO_2$  values as a function of temperature ( $\Delta_rG$   
778 values are calculated for each curve at the temperatures at which they appear on the plot) is shown for the  
779 classical-OSaS model. (C) The effect of variable water content on the MELTS-derived silica activity and  
780 the calculated  $fO_2$  values is shown for a range of temperatures (at constant pressure) using the MELTS-  
781 OSaS model. (D) The effect of pressure variation on the calculated values of  $fO_2$  is shown for the MELTS-  
782 OSaS model.

783

784 Figure 12 : The  $fO_2$  values (relative to the FMQ buffer) calculated from the OSaS models for the MORB  
785 samples from the Lau Basin (1, Hawkins & Melchior, 1985; 2, Kamenetsky et al., 1997), Costa Rican Ridge  
786 Zone (3, Natland et al., 1983), and basalts from the Mariana Trough (1, Hawkins & Melchior, 1985) and  
787 Arc (7, Bloomer & Hawkins, 1987) are shown with the  $fO_2$  values determined by XANES for midocean  
788 ridge basalt glasses (4, Zhang et al., 2018; 5, O’Neill et al., 2018) and basalt glasses from the Mariana  
789 Trough and Arc basalts (6, Brounce et al., 2014). Brounce et al. (2014) report the  $Fe^{3+}/\Sigma Fe$  ratios for glasses  
790 from the Mariana trough in their supplement; we convert these ratios to  $\Delta FMQ$  values using a temperature  
791 of 1150°C the model of Kress and Carmichael (1991). The OSaS-generated values broadly agree with the  
792 XANES-established oxygen fugacity values, where there is less agreement in the Mariana trough samples,  
793 but excellent agreement between analyses from MORB and general agreement with samples from the  
794 Mariana arc (see text).

795

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1085

<i>Table 1: Linear Regression Parameters for <math>\mu\text{Fe}_3\text{O}_4</math> Correction</i>				
	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>
Intercept	-88317.12	30632.35	-2.88	6.02E-03
MELTS $\mu\text{Fe}_3\text{O}_4$	0.9680702	0.02	56.66	1.73E-43
<i>X<sub>i</sub> Spinel</i>				
Cr <sub>2</sub> O <sub>3</sub>	66581.75	11814.68	5.64	1.08E-06
FeO <sup>T</sup>	53625.74	12355.58	4.34	7.96E-05
MgO	75747.29	20637.63	3.67	6.40E-04



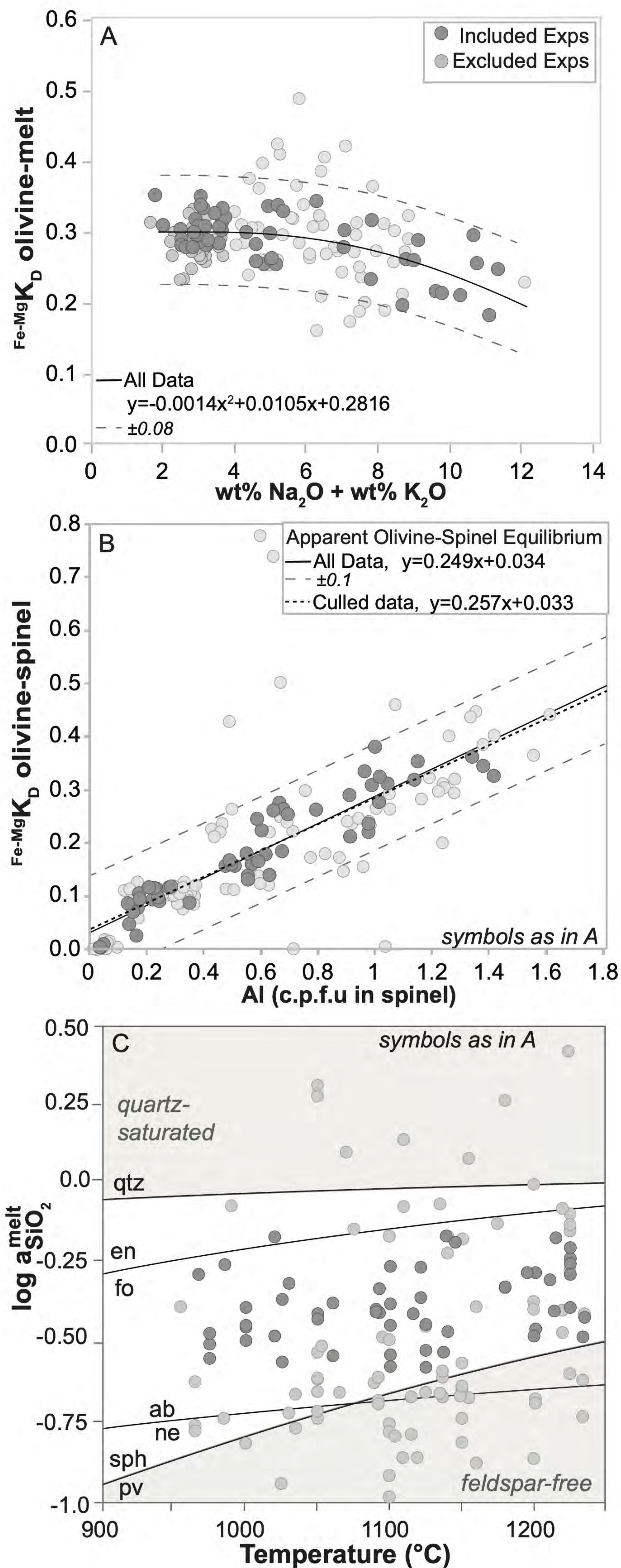


Figure 1



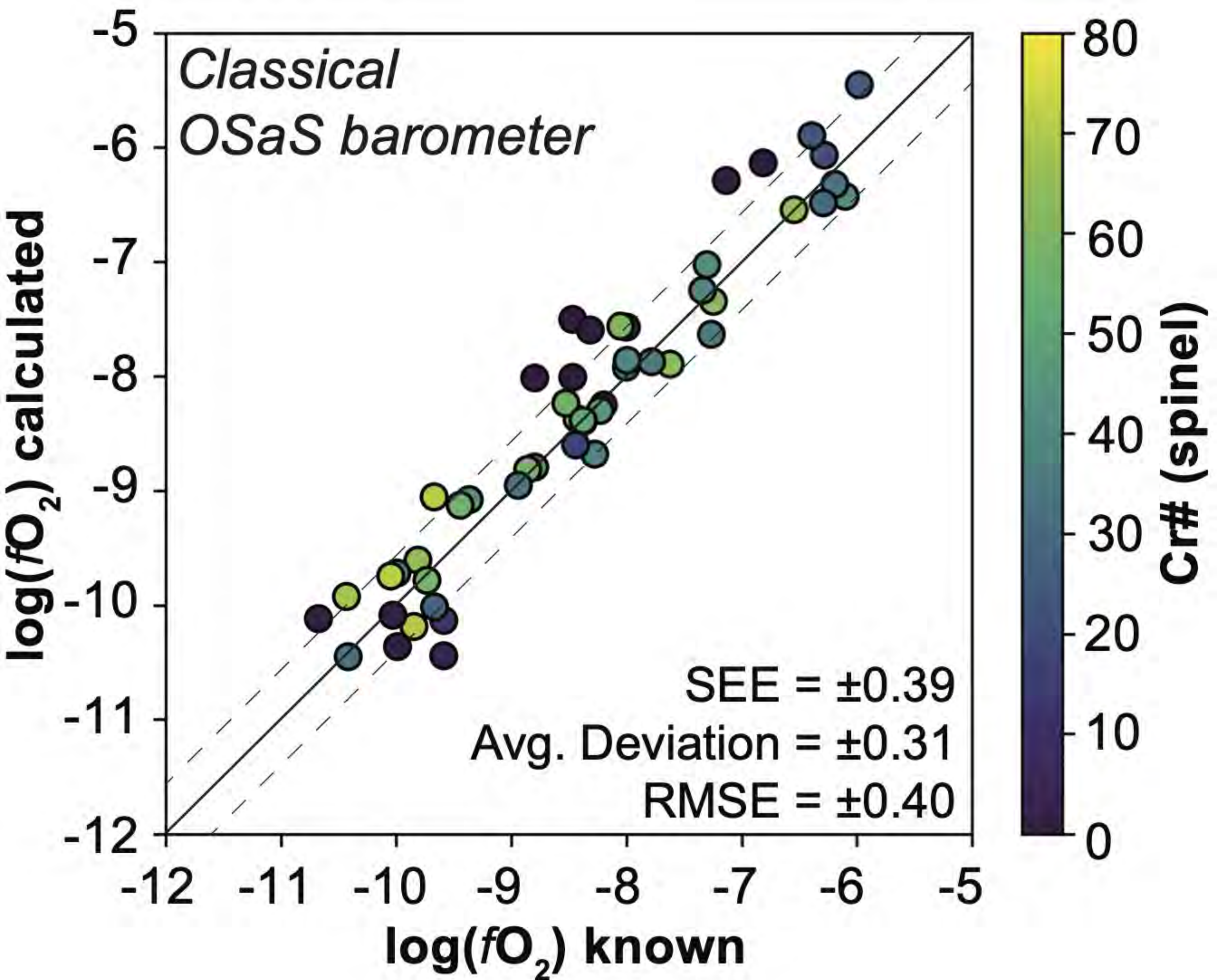


Figure 3

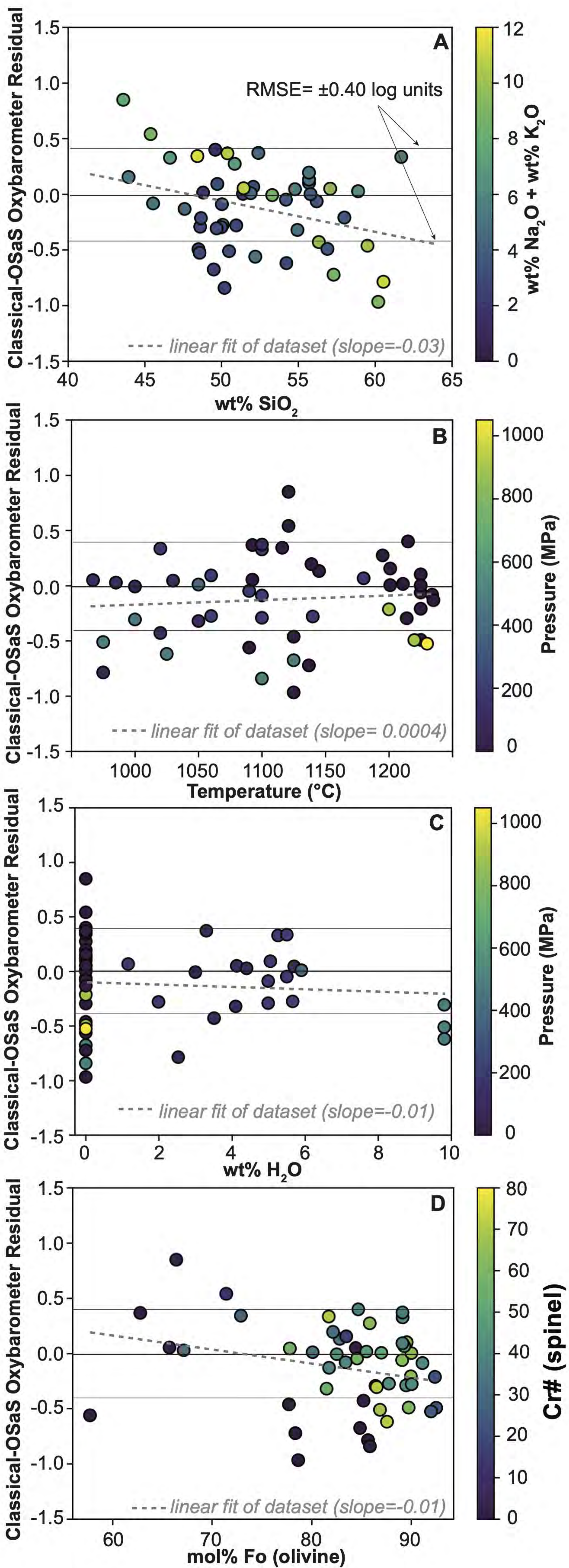
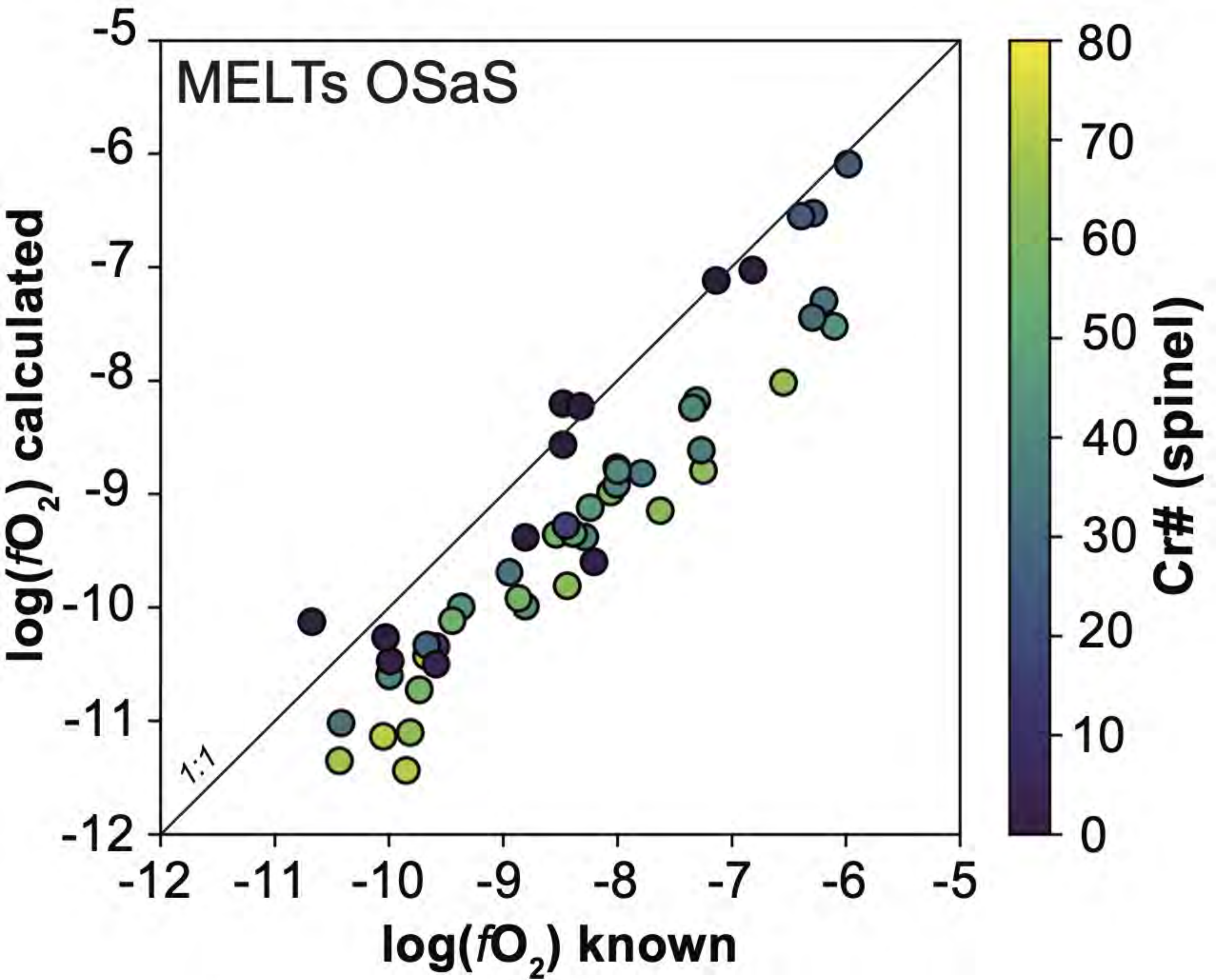


Figure 4



**Figure 5**

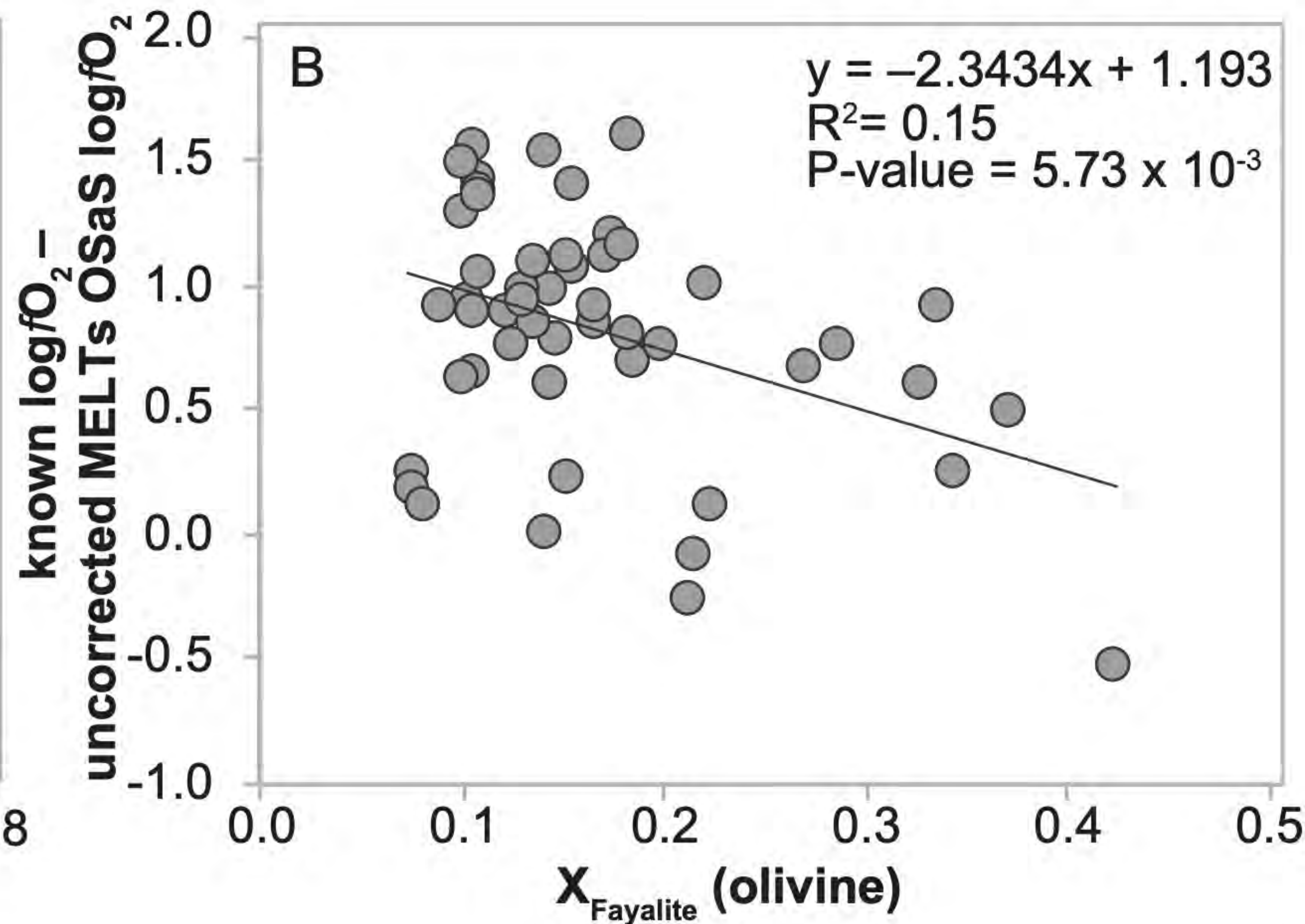
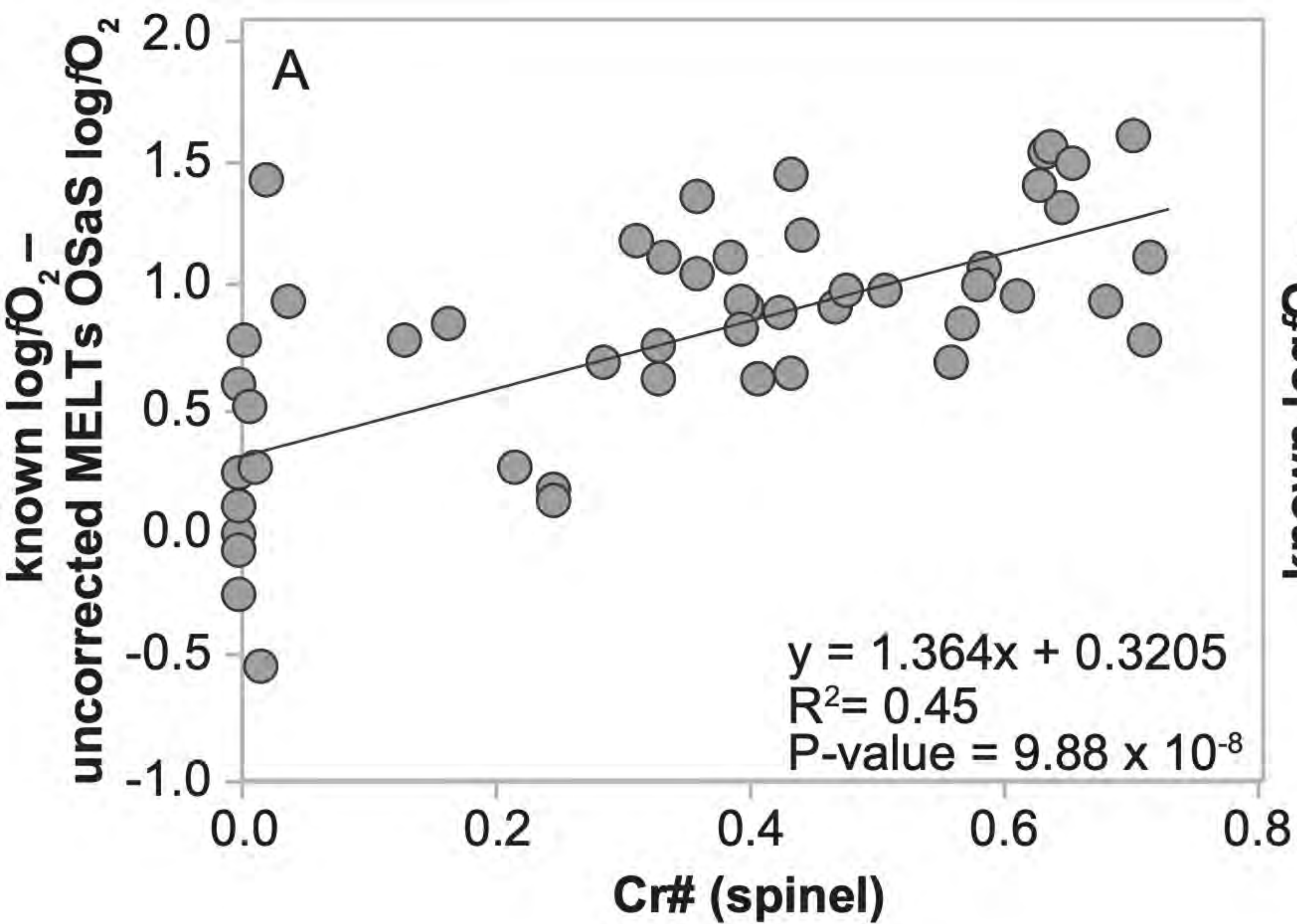


Figure 6

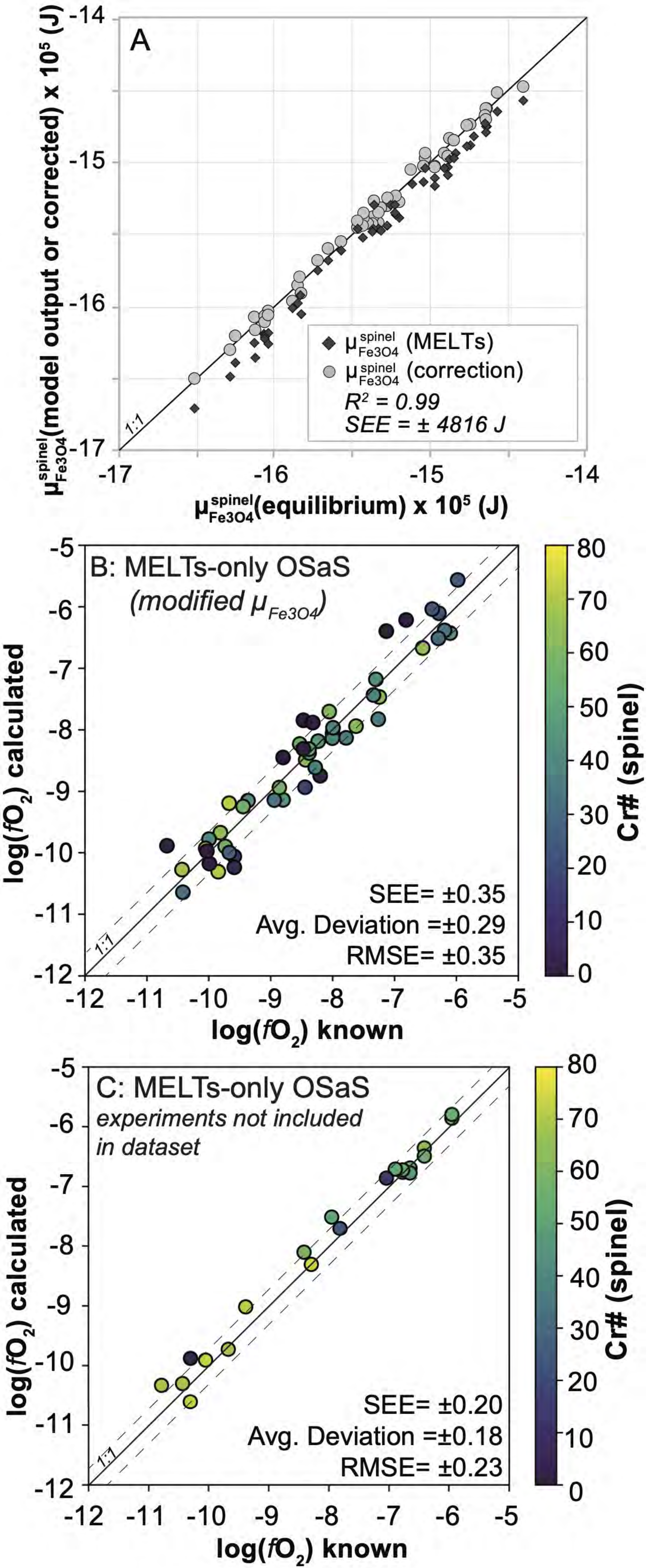


Figure 7

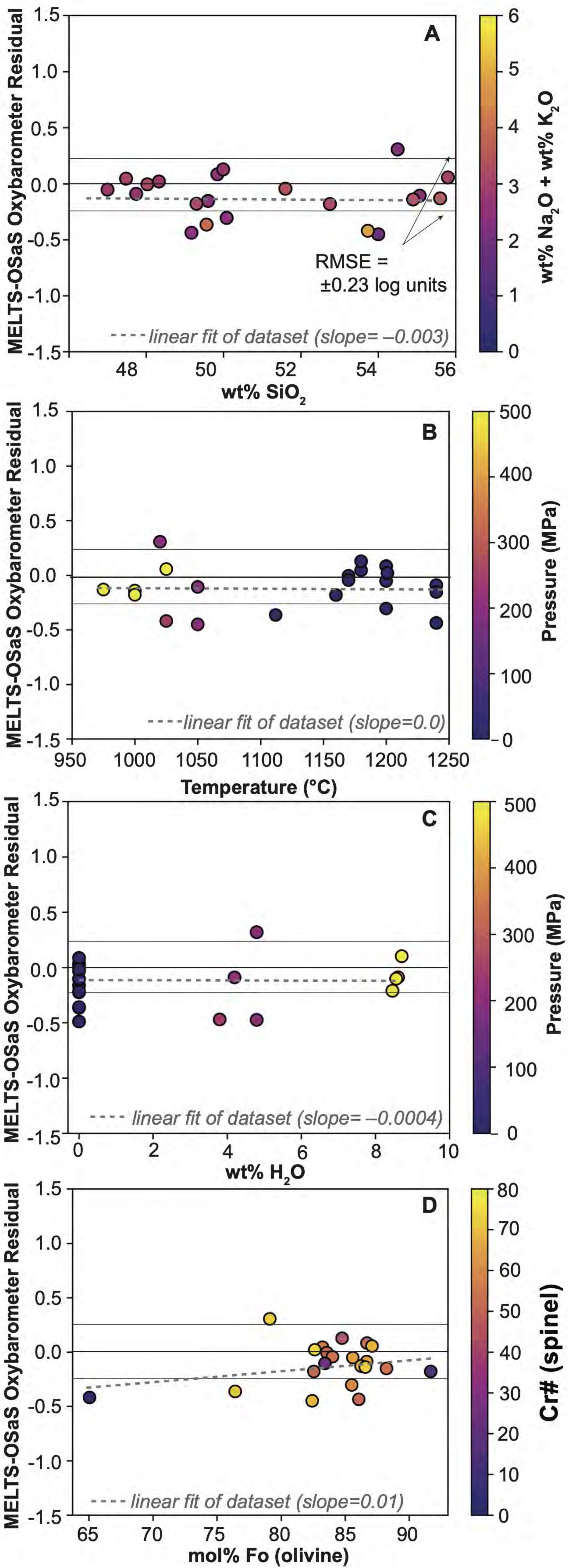


Figure 8



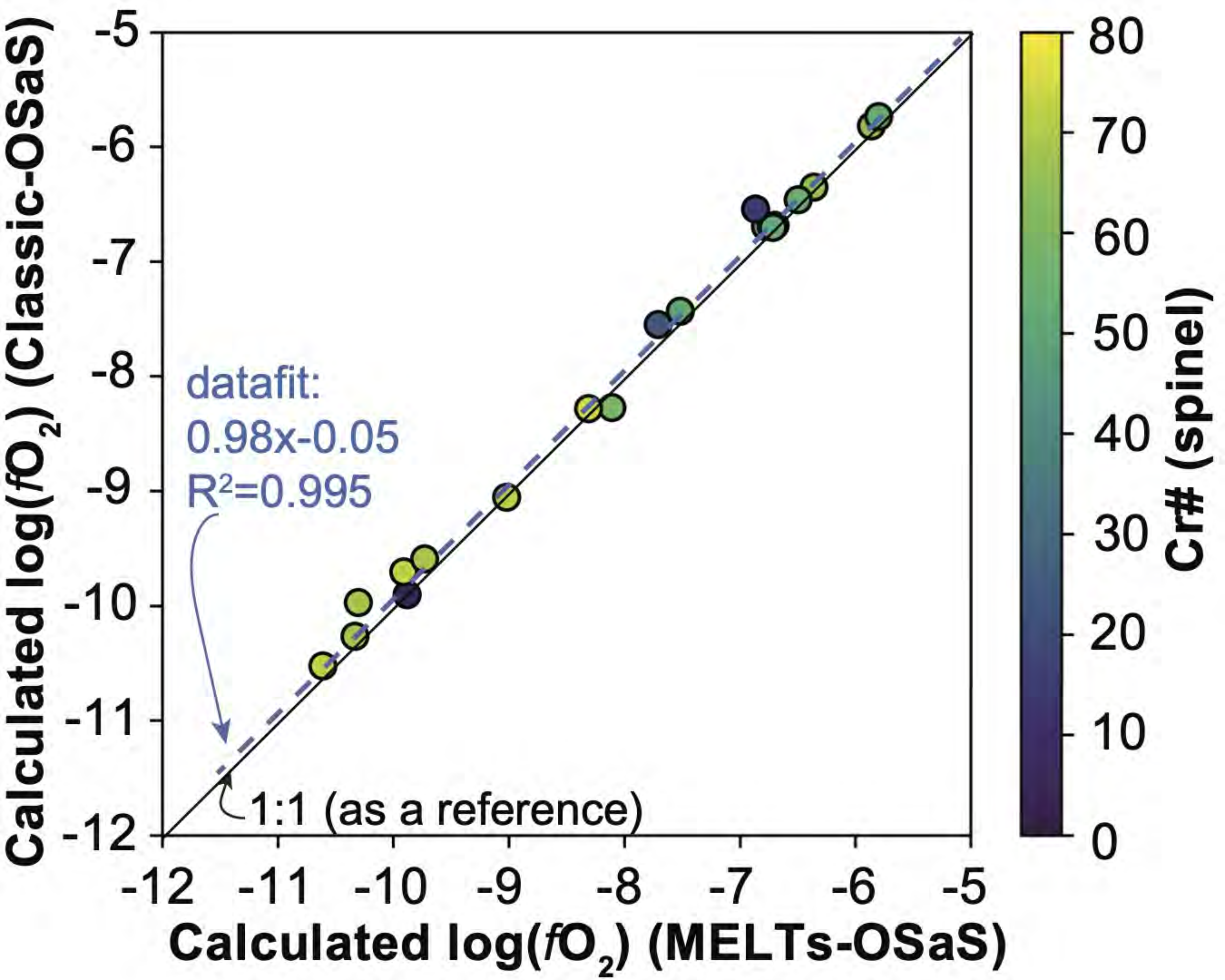


Figure 9

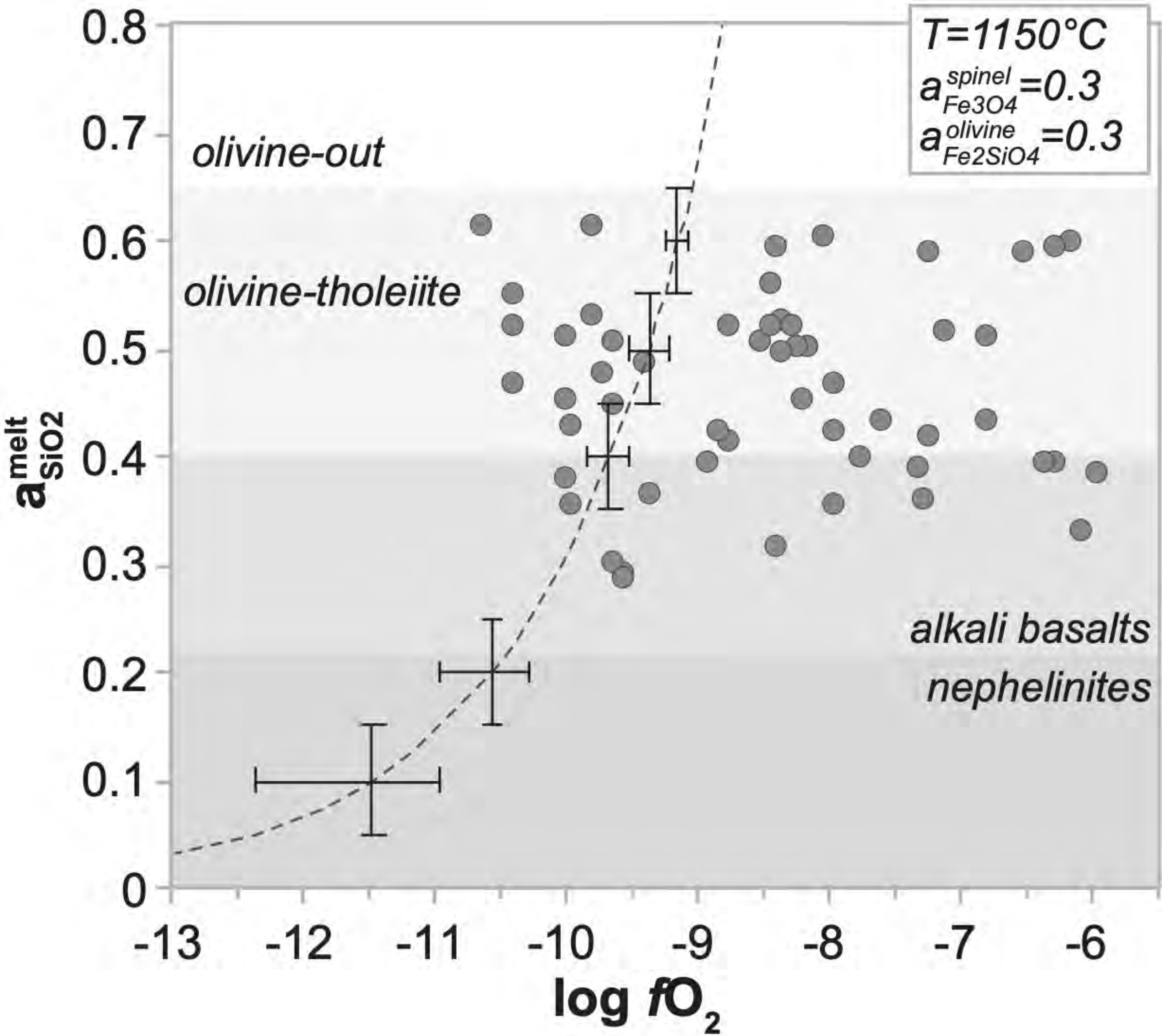


Figure 10

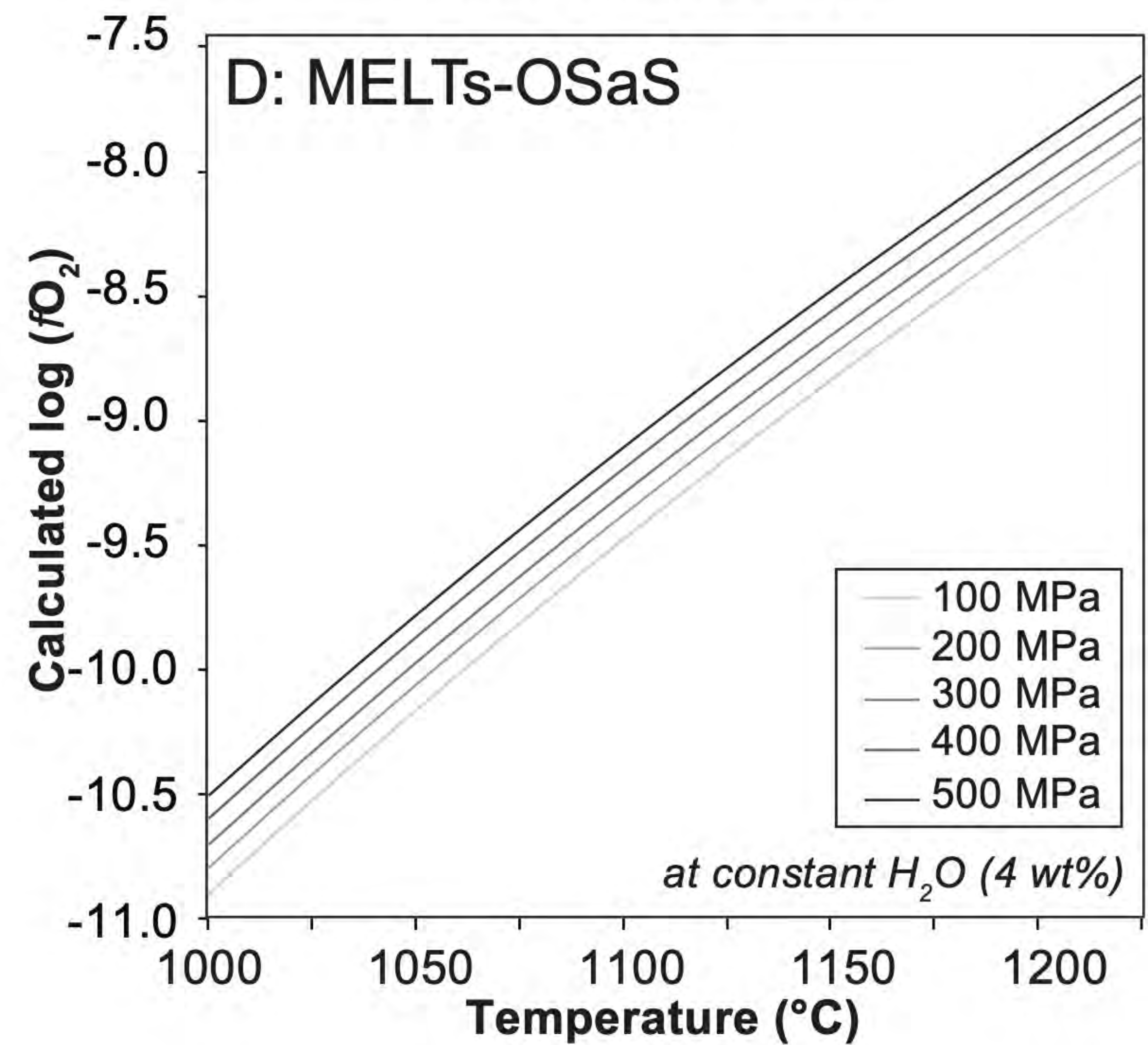
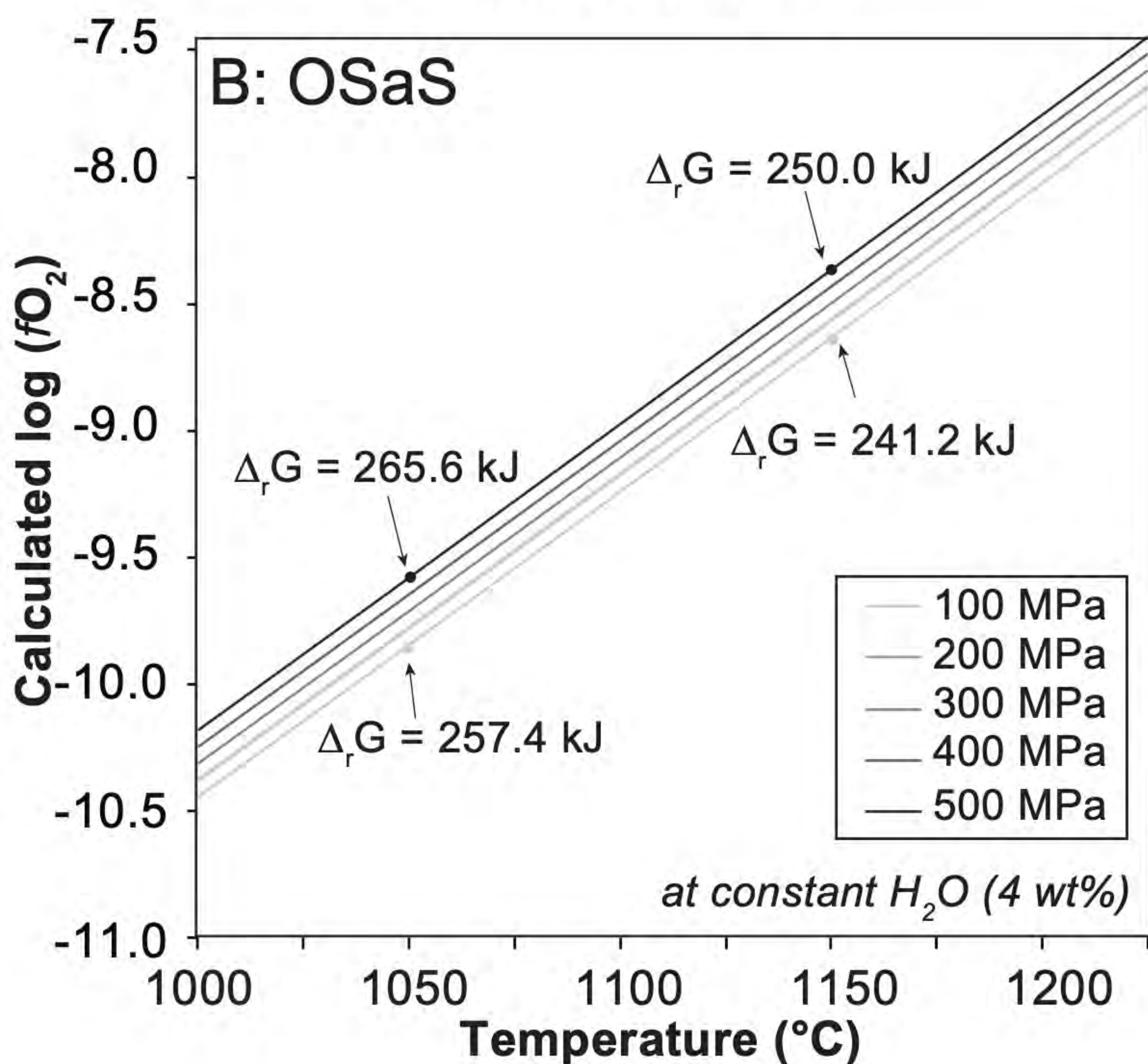
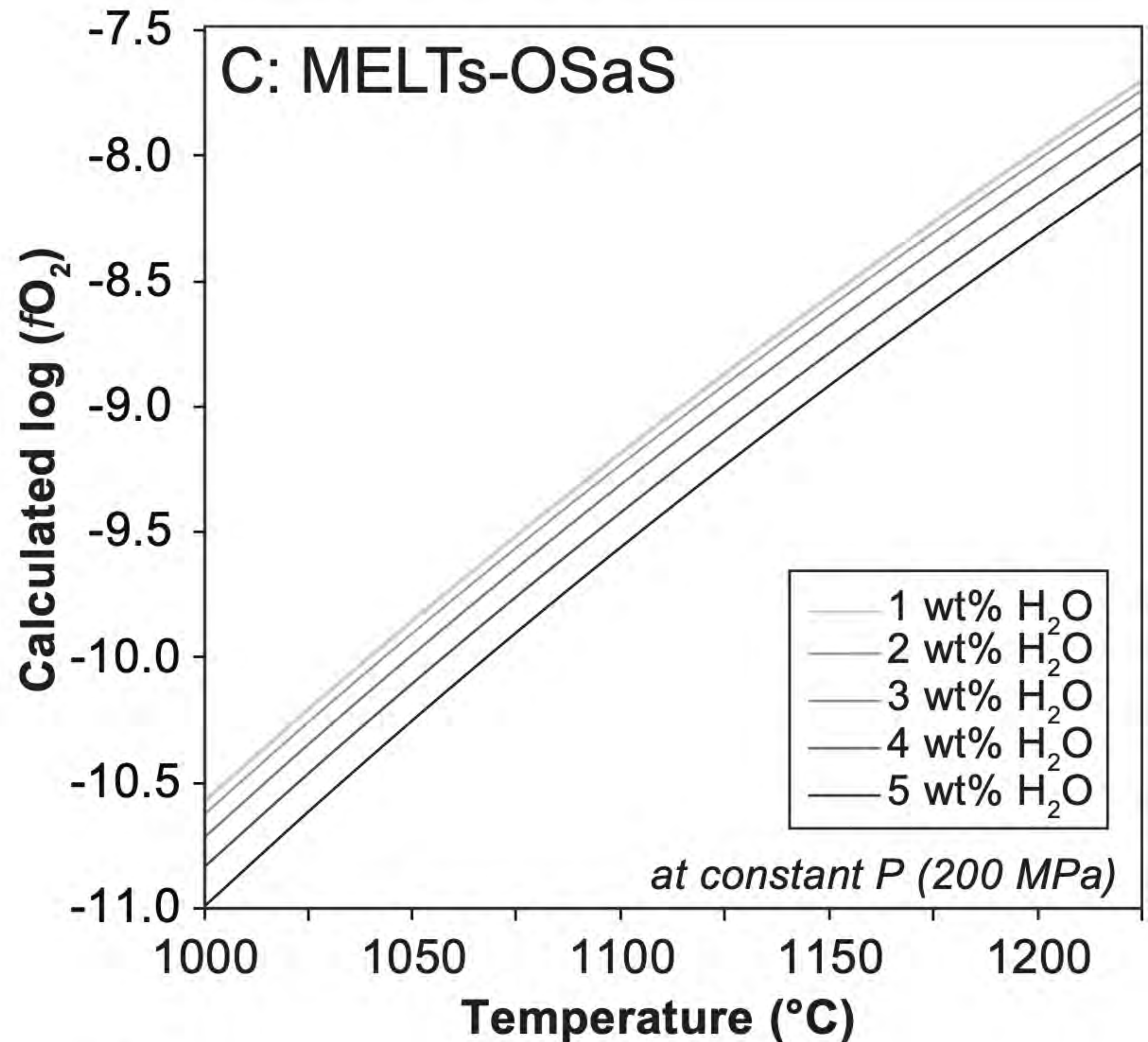
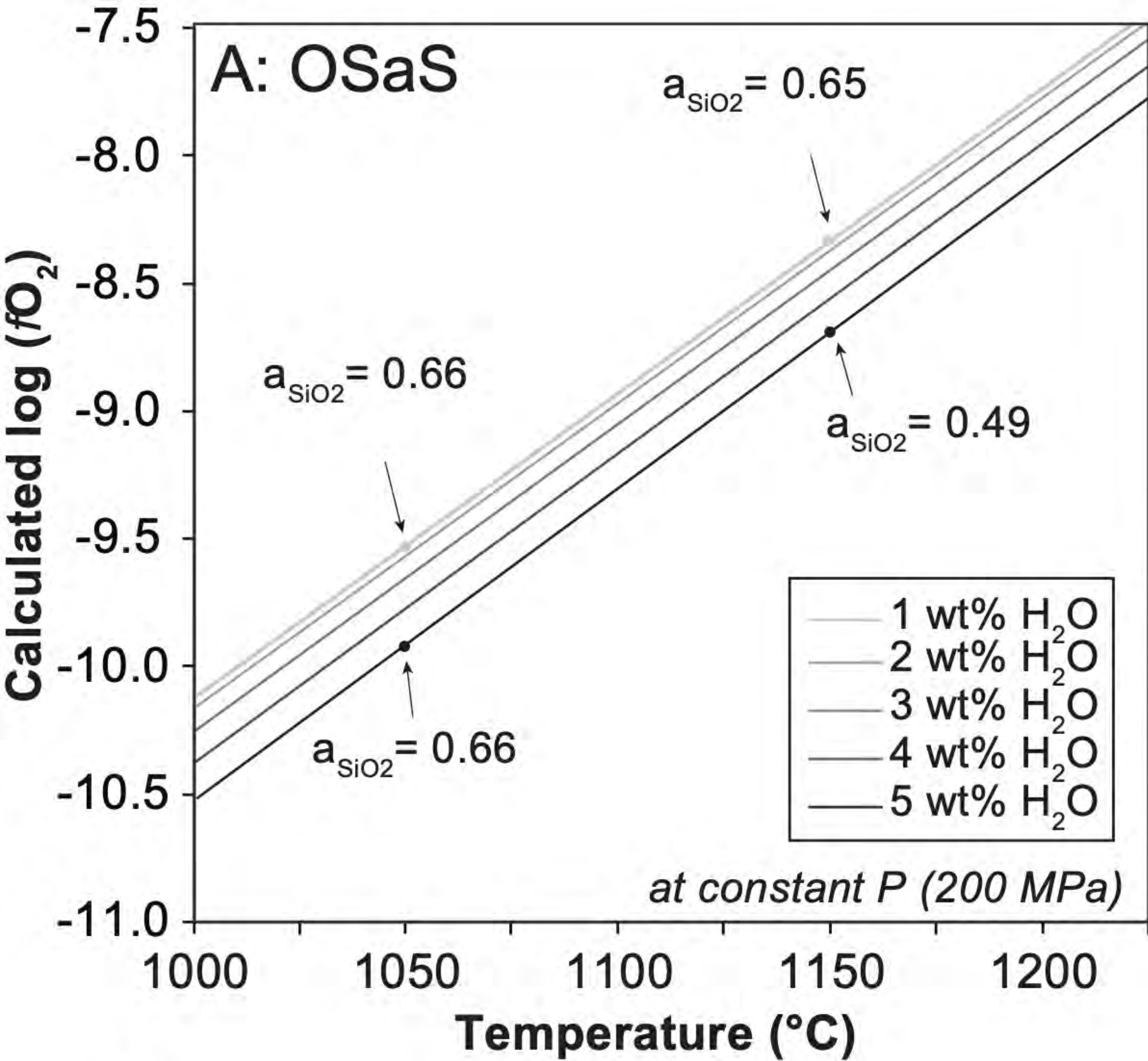
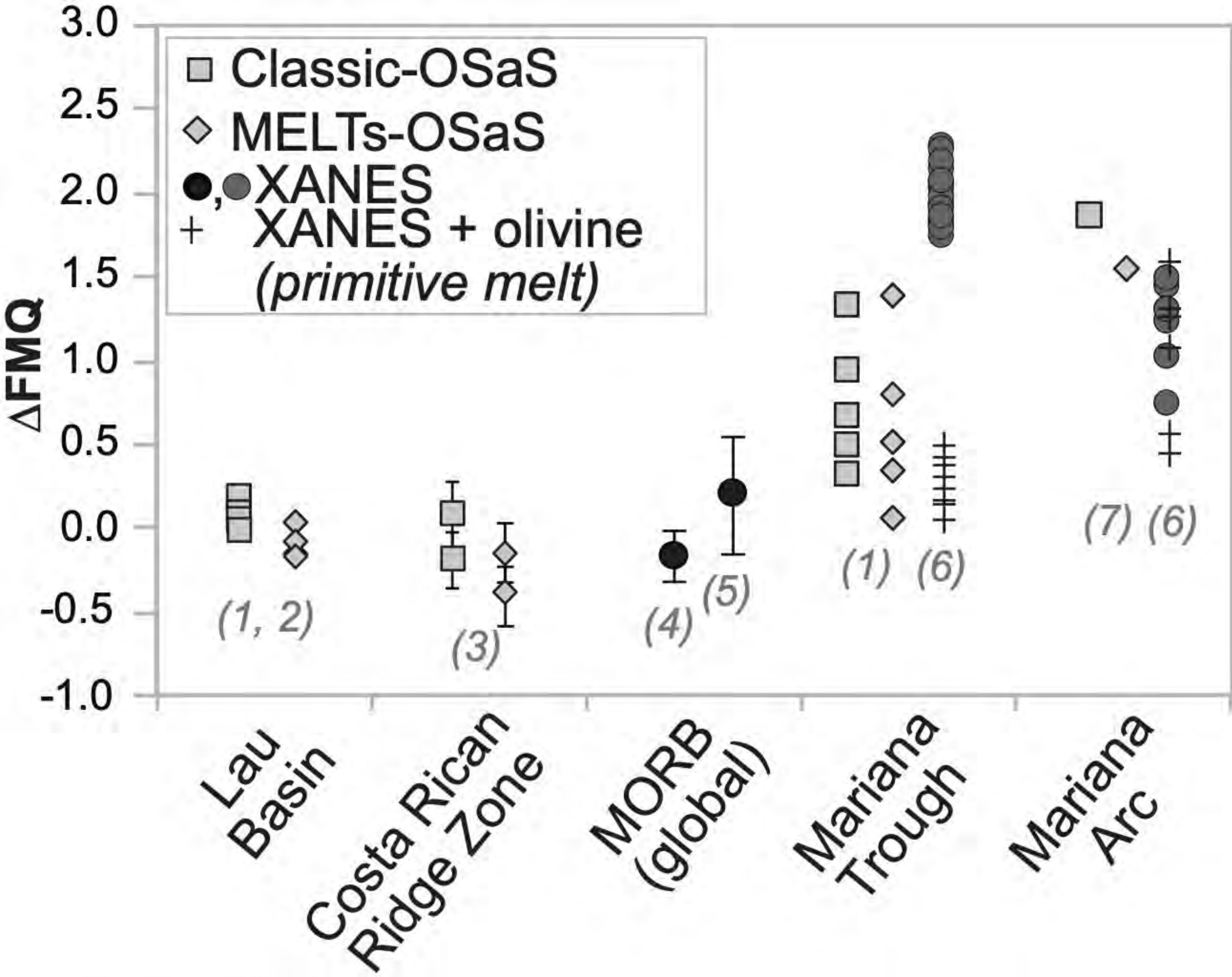


Figure 11



**Figure 12**