

1 Calorimetry and structural analysis of uranyl sulfates with rare topologies

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9

10 **Abstract**

11 Uranyl sulfate minerals are the most rapidly expanding group of uranium minerals, with dozens
12 of species described in the past decade from the localities of White Canyon, USA and Jáchymov,
13 Czech Republic. Synthetic analogs of a suite of uranyl sulfate minerals were crystallized,
14 characterized, and the standard-state enthalpies of formation (ΔH_f°) were determined. Synthetic
15 lussierite is monoclinic, space group *Cc*, $a = 9.2896$, $b = 28.685$, $c = 9.6155$, $\beta = 93.504$.
16 Synthetic geschieberite is orthorhombic, space group *Pna2₁*, $a = 13.7408$, $b = 7.2713$, $c =$
17 11.5844 . The standard-state enthalpies of formation from the binary oxides for lussierite,
18 péligotite, shumwayite, geschieberite, and bluelizardite are -3214 ± 78 , -2026 ± 33 , -587 ± 22 , -
19 966.1 ± 10.9 , and -2084 ± 21 kJ/mol, respectively, while the standard-state enthalpies of
20 formation of each phase from its elements are -9743 ± 78 , -7220 ± 33 , -5255 ± 22 , -3916 ± 20 ,
21 and -7117 ± 21 kJ/mol, respectively. The ΔH_f° of péligotite was accurately estimated using the
22 ΔH_f° of lussierite, bluelizardite and literature values of the oxide components of each phase. This
23 implies that estimates can be made accurately of the ΔH_f° of uranyl sulfates of minerals without

24 synthetic analogs.

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26 **Keywords:**

27 High temperature drop solution calorimetry; uranyl sulfate minerals; hydrogen atom positions

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30 **Introduction**

31 Uranium is of considerable societal importance: it is the primary fuel of nuclear energy,
32 essential for production of many medical isotopes, central to international security concerns
33 regarding nuclear weapons and non-proliferation, and an environmental contaminant where
34 uranium mining and nuclear fuel cycle activities occurred. Uranyl sulfates, which contain U in its
35 hexavalent oxidation state as the UO_2^{2+} uranyl ion, are an important and rapidly growing group
36 of secondary minerals found where hydration-oxidation processes alter primary uranium
37 minerals and sulfides, typically in abandoned mines (Finch and Murakami, 1999; Plášil et al.,
38 2014). Acid-mine drainage conditions promote the transport of UO_2^{2+} and SO_4^{2-} aqueous ions
39 through the country rock, resulting in efflorescent crusts of secondary minerals on mine walls
40 (Kampf et al., 2019). Until 2009, less than 20 uranyl sulfate minerals had been described, of
41 which zippeite ($\text{K}_3(\text{H}_2\text{O})_{3.3}[(\text{UO}_2)_4(\text{SO}_4)_2\text{O}_3(\text{OH})]$) is the most commonly encountered. Over the
42 past dozen years studies of mining districts including White Canyon, Utah, USA, and Jáchymov,
43 Czech Republic, have tripled the number of described uranyl sulfate mineral species (IMA,
44 2023).

45 The structures of uranyl sulfate minerals generally consist of anionic structural units
46 containing uranyl and sulfate polyhedra and an interstitial complex of low-valence cations and
47 H_2O (Burns et al., 1997). Uranyl oxyanion structural units in uranyl minerals have been
48 organized into a hierarchy based on dimensionality (Burns et al., 1996; Krivovichev and Plášil,
49 2013), in which sheets predominate (Burns et al., 1996). The structural units of uranyl sulfate
50 minerals are topologically and dimensionally diverse, including finite clusters, chains, and sheets
51 of polyhedra (Gurzhiy and Plášil, 2019). Sulfate groups bond to uranyl ions in both monodentate

52 and bidentate fashions, which further enhances structural diversity through the multiple modes of
 53 connection between the polyhedra (Krivovichev and Plášil, 2013; Gurzhiy and Plášil, 2019). No
 54 thermodynamic data exists to help understand the formation of the unique uranyl sulfates found
 55 in White Canyon, Utah.

56 High-temperature oxide melt solution calorimetry has been extensively applied for
 57 determination of the enthalpy of formation (ΔH_f°) of uranyl compounds (Navrotsky, 2014)
 58 including uranyl silicates (boltwoodite, uranophane (Shvareva et al., 2011); soddyite (Gorman-
 59 Lewis et al., 2007)), uranyl carbonates (rutherfordine, grimselite, andersonite (Kubatko et al.,
 60 2005)), uranyl vanadates (carnotite, curienite, francevillite (Spano et al., 2017)), uranyl sulfates
 61 (zippeite (Sharifironizi et al., 2016); natrozippeite, cobaltzippeite, zinczippeite (Sharifironizi and
 62 Burns, 2018)), and some U^{IV} minerals (coffinite (Guo et al., 2015); brannerite (Simoncic and
 63 Navrotsky, 2007); behounekite (Zhang et al., 2019)). These studies revealed relationships
 64 between the enthalpy of formation and the Smith acidity of the interstitial cation (Sharifironizi
 65 and Burns, 2018), the normalized charge deficiency per anion (Spano et al., 2017), and the

Table 1. The concentration and quantity of each reagent used in the phase synthesis.

Name	Formula	H ₂ O (ml)	UO ₃ (g)	18.4 M H ₂ SO ₄ (mL)	Aliquot evaporated (mL)	5.0 M NaOH (mL)	Final Stock pH
Lussierite	Na ₁₀ [(UO ₂)(SO ₄) ₄](SO ₄) ₂ ·3 H ₂ O	20.0	2.6	2.2	3	‡	2.6
Péligotite	Na ₆ [(UO ₂)(SO ₄) ₄]·4H ₂ O	40.0	5.7	4.5	2	1.15*	2.5
Shumwayite	[(UO ₂)(SO ₄)(H ₂ O) ₂] ₂ ·H ₂ O	20.0	1.4	0.3	2	None	1.7
Bluelizardite	Na ₇ [(UO ₂)(SO ₄) ₄]Cl·2H ₂ O	20.0	5.1	8.6	3	26.4†	1.8
Name	Formula	H ₂ O (ml)	(UO ₂)(NO ₃) ₂ ·6H ₂ O (g)	18.4 M H ₂ SO ₄ (mL)	K ₂ SO ₄ (g)		
Geschieberite	K ₂ [(UO ₂)(SO ₄) ₂ (H ₂ O)]·H ₂ O	5.0	2.5	0.14	0.44		

*NaOH added to aliquot vial rather than the stock solution.

†5 M solution was added to the uranyl sulfate stock, followed by 2.5 mL of 12 M HCl to adjust the pH.

‡The solution was titrated with NaOH to a specific pH and the volume was not recorded.

66 number of oxygen atoms per U (Navrotsky et al., 2013).

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68 Here we report synthesis of the analogs of five of the new uranyl sulfate minerals from
69 Red Canyon and Jáchymov and determination of their enthalpies of formation. We had initially
70 planned to measure the aqueous solubility of these minerals, but we qualitatively observed that
71 these phases are highly soluble and accurate measurements were precluded by the large amount
72 of material those measurements would require. This is part of our on-going efforts to develop
73 thermodynamic data for uranyl minerals in order to better understand their occurrences and
74 transformations.

75

76 **Methods**

77 **Synthesis of uranyl sulfate phases.** Lab-prepared UO_3 was synthesized by placing
78 $(\text{UO}_2)(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ (International Bio-analytical Industries) into an alumina crucible, covering
79 the crucible with a watch glass and heating the sample to $600\text{ }^\circ\text{C}$ on a hot plate in a hood until the
80 uranyl nitrate had melted and then formed a red-orange solid. The material was verified as
81 slightly hydrated UO_3 via powder X-ray diffraction (PDF-00-053-0877) and was stored in a
82 sealed container under vacuum until used as a reagent.

83

84 Crystalline uranyl sulfate phases were synthesized from aqueous uranyl sulfate stock
85 solutions containing various amounts of ultrapure Milli-Q H_2O , UO_3 and concentrated H_2SO_4
86 (BDH). Different amounts of 5 M NaOH (ACS) were added to supply sodium ions and to adjust
87 the pH. Details of the synthesis experiments are summarized in Table 1. The pH of each solution
88 was measured using a Fisher Scientific AB150 pH/mV probe calibrated with three NIST
89 standards (BDH). To synthesize the analog of blue lizardite, $\text{Na}_7[(\text{UO}_2)(\text{SO}_4)_4]\text{Cl} \cdot 2\text{H}_2\text{O}$, 5 M
90 NaOH was added to a uranyl sulfate solution until a precipitate formed. The precipitate was then

91 dissolved by adding concentrated HCl (BDH). The solutions that yielded synthetic analogs of
92 lussierite, shumwayite and bluelizardite were evaporated in Isotemp ovens at 60, 70 and 70 °C,
93 respectively, until crystals formed at the bottom of the vials and a small amount of the stock
94 solution remained. The solution that yielded the synthetic analog of péligotite was dried to
95 completion at 70 °C. After addition of K₂SO₄ (Fisher Chemical), geschieberite crystals
96 precipitated from the stock solution at room temperature over a few hours and were harvested
97 quickly from the mother liquor to prevent contamination by the formation of secondary
98 potassium sulfate salts. Crystals from all syntheses were harvested and rinsed with ethanol and a
99 few drops of hot ultrapure water on filter paper in a Buchner funnel to remove any impurities or
100 residual stock solution, if present. A vacuum was applied during rinsing to prevent excessive
101 dissolution of the uranyl sulfate crystals. After cleaning, all crystals were dried completely over
102 the vacuum, then recovered for further analysis.

Table 2. Crystallographic parameters of synthetic phases examined in this study.

	Lussierite	Péligotite	Shumwayite	Geschieberite	Bluelizardite
Space Group	<i>Cc</i>	<i>P-1</i>	<i>P2₁/c</i>	<i>Pna2₁</i>	<i>C2/c</i>
<i>a</i> (Å)	9.2896	9.7935	6.730	13.7408	21.162
<i>b</i> (Å)	28.685	9.9419	12.479	7.2713	5.3462
<i>c</i> (Å)	9.6155	10.615	16.881	11.5844	34.719
α (°)	90	88.659	90	90	90
β (°)	93.504	74.013	90.931	90	104.902
γ (°)	90	89.188	90	90	90
Vol (Å³)	2557.4	993.26	1417.5	1157.43	3795.9

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104 **Single Crystal X-ray Diffraction.** Selected crystals from each product were immersed
105 in mineral oil and attached to cryoloops. Single-crystal X-ray diffraction (SC-XRD) data were
106 collected using a Bruker Apex II Quazar diffractometer with a micro-source sealed tube using
107 monochromated Mo *K* α X-radiation. Data integration was done with the APEX III software and

108 SADABS was used to apply absorption corrections (Sheldrick, 2008). All structures were solved
109 and refined with the SHELXTL software package (Sheldrick, 2015a, b). The synthetic phases in
110 this study diffracted well enough that the positions of all hydrogen atoms were determined.
111 Hydrogen atoms were added to all structures at crystallographically appropriate positions based
112 on residual electron densities. Crystallographic information files (CIF) were generated and were
113 used to simulate powder diffractograms (Macrae et al., 2020). Crystallographic information is
114 summarized in Table 2.

115

116 **Powder X-ray Diffraction.** Dried crystals of each phase were ground into a fine powder
117 using an agate mortar and pestle. Small amounts of powder were placed on a glass slide for
118 collection of diffraction data using a Bruker D8 Advance Davinci powder X-ray diffractometer
119 (PXRD). Data were collected using monochromatic Cu $K\alpha$ radiation over the 2θ range of 5 to
120 55° . Powder patterns of each uranyl sulfate phase were simulated using the Mercury software
121 package (Macrae et al., 2020) using the structural parameters of the synthetic phases obtained
122 during the SC-XRD analysis. Comparison of simulated and measured diffractograms of the bulk
123 powders confirmed phase identity and purity.

124

125 **Inductively Coupled Plasma Optical Emission Spectroscopy.** For verification of the
126 cation content of the phases under study, 10 mg of each powdered phase were dissolved in 5%
127 v/v nitric acid that was analyzed in an Avio 200 PerkinElmer inductively coupled plasma optical
128 emission spectrometer (ICP-OES). Each phase was analyzed in triplicate with five calibration
129 standards, with Y used as an internal standard. The resulting compositions are in good agreement

130 with the ideal chemical formulas from the literature and increase our confidence that the
131 synthetic phases are identical to the natural minerals.

132

133 **Thermogravimetric Analysis.** Thermogravimetric analysis (TGA) was performed using
134 ~12 mg of each powdered phase in alumina crucibles, with an empty crucible as a blank, inside a
135 Mettler Toledo Thermogravimetric Analyzer heated to 700 °C. Bluelizardite was heated to 800
136 °C, although the Cl was completely liberated by ~725 °C. The moles of water of each phase, and
137 Cl in the case of bluelizardite, were calculated from the mass loss of the sample as measured by
138 the TGA.

139

140 **Calorimetry.** A Setaram AlexSYS 1000 model Calvet high temperature calorimeter was
141 used to measure the heat of dissolution of each crystalline phase. Each powdered phase was
142 pressed into ~5 mg pellets and dropped into molten solvent at 700 °C. Sodium molybdate
143 ($3\text{Na}_2\text{O}\cdot 4\text{MoO}_3$) was employed as the solvent as it is an effective solvent for uranyl phases,
144 including uranyl sulfates (Navrotsky, 1997, 2014; Sharifironizi et al., 2016; Sharifironizi and
145 Burns, 2018). Prior to calorimetric studies, pellets of each phase were dropped into molten
146 sodium molybdate in alumina pans in a furnace at 700 °C to visually confirm complete
147 dissolution of the pellet. In the calorimeter, oxygen gas was bubbled through the solvent to
148 maintain oxidizing conditions and to stir the solvent to encourage dissolution of the pellets.
149 Oxygen flushing gas was used to sweep away gas and water vapor from the crucible. The heat of
150 dissolution of each phase was recorded and used in thermal chemical cycles to calculate the
151 enthalpies of formation of each compound from elements and binary oxides. The thermal
152 chemical cycles and number of drops for each phase are listed in Table 3.

153 For blue lizardite, the distribution of Cl between the solvent and gas upon dissolution at
154 700 °C was determined (Lilova et al., 2020). The ΔH_{ds} of NaCl was measured by dropping 5 mg
155 pellets of ground reagent-grade NaCl (Fisher Chemical) into solvent in the calorimeter and
156 recording the heat of dissolution. Powdered NaCl was heated in a TGA and no mass loss was
157 observed at or below 700 °C, indicating the reagent had not absorbed ambient water. To verify
158 that Cl remained in the solvent during dissolution, alumina crucibles were prepared with 1 g of
159 freshly prepared sodium molybdate solvent in a furnace at 700 °C. Fifty mg of NaCl was added
160 (30.3 mg Cl) to four crucibles. After quenching the total mass loss was 3.7 ± 1.7 mg, which was
161 comparable to the mass lost in a blank crucible loaded with only sodium molybdate solvent.
162 Analysis of the quenched solvent with SEM-EDS indicated the presence of Cl (Table S5).

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165 **Results and Discussion**

166 The refined crystal structures of the five uranyl sulfate phases under study are in good
167 accord with the published structures of the natural phases (Table 2) (Plášil et al., 2014; Plášil et
168 al., 2015; Kampf et al., 2017a; Kampf et al., 2017b; Kampf et al., 2019). Powder X-ray
169 diffraction data confirmed the identity and purity of each phase (Fig. S1-S5). Chemical analysis
170 yielded molar ratios of M:U:S (M = Na, K or no cation) within error of the ideal mineral
171 formulas (Table S1). Thermogravimetric analysis provided the molar amounts of water and Cl of
172 the synthetic uranyl sulfates and these are in agreement with the idealized mineral formulas

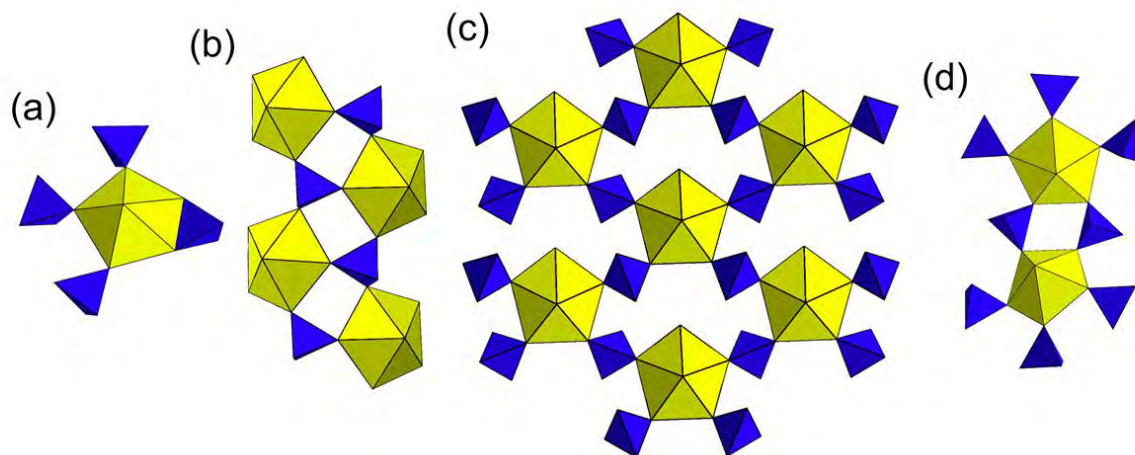
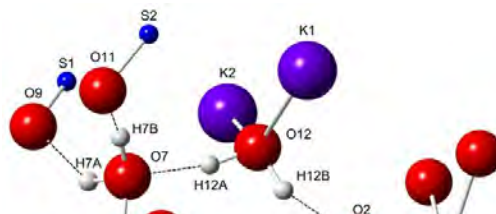


Fig. 1. The uranyl sulfate structural units for (a) péligotite and lussierite, (b) shumwayite, (c) geschieberite and (d) bluelizardite.

174

175 The structural units of the five compounds under study are shown in Fig. 1. The earlier
176 crystal structure determinations for natural samples of geschieberite and lussierite did not include
177 the positions of H atoms. The X-ray data for the synthetic crystals readily yielded the positions
178 of all H atoms. In the case of geschieberite, Plášil et al. proposed H bonds donated by the H₂O
179 group bonded in the equatorial plane of the uranyl ion and accepted by non-bridging O atoms of
180 sulfate tetrahedra located in the same sheet as the uranyl polyhedron. There are two H₂O groups
181 in the structure: the one bonded to the uranyl ion, and another located in the interlayer where it is
182 bonded to K. In the new structure, the H bonds of the H₂O group bonded to the uranyl do form
183 the predicted bonds to the sulfate groups (Fig. 2, O7). However, in the synthetic structure the
184 H₂O group bonded to the uranyl ion also accepts a H bond donated by the H₂O group located in
185 the interlayer (Fig. 2, O12). The other H bond emanating from the interlayer H₂O group is
186 accepted by a uranyl ion oxygen atom of an adjacent sheet, such that H bonds from this
187 interlayer H₂O group bridge sheets of uranyl and sulfate polyhedra (Fig. 2).

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197 The structure of lussierite contains three H₂O groups located in interstitial positions,
198 where each of them is bonded to two Na cations (Fig. 3). The structural unit consists of a uranyl
199 polyhedron sharing vertices with four sulfate tetrahedra, and there are two different sulfate
200 tetrahedra in the interstitial complex. The O27 oxygen donates two H bonds that are accepted by
201 two different interstitial oxygen atoms of sulfate groups. The O28 oxygen atom donates H bonds
202 that are accepted by oxygen atoms of two sulfate tetrahedra of different structural units. As for
203 the O27 oxygen, O29 oxygen donates two H bonds that are accepted by oxygen atoms of the two
204 distinct interstitial sulfate groups (Fig. 3).

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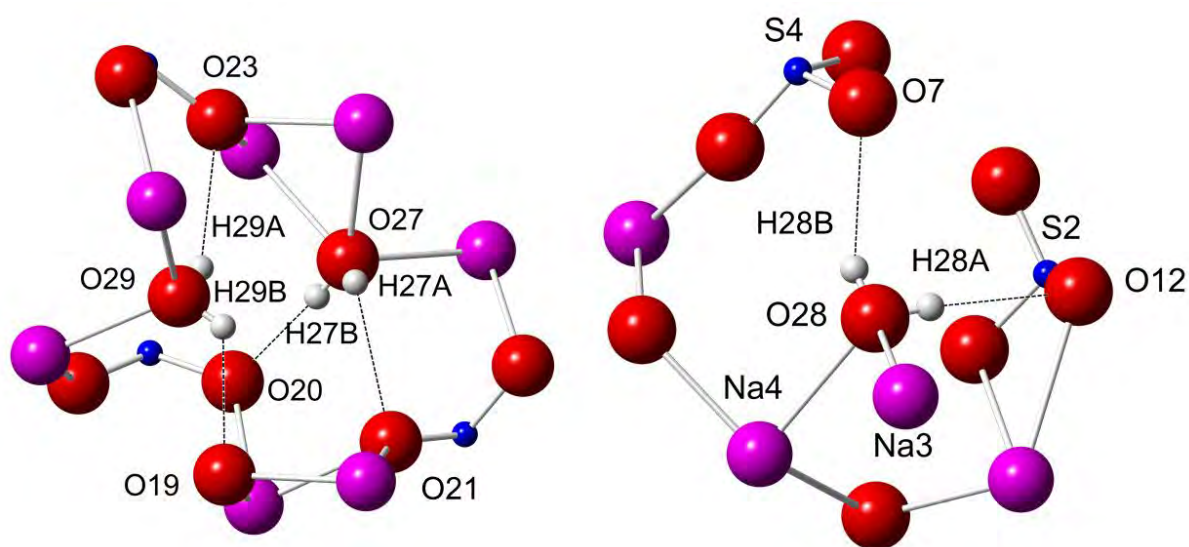


Fig. 3. The hydrogen bonding in lussierite. (Left) The O27 water molecule donates hydrogen bonds to two different interstitial oxygen atoms of sulfate units. (Left) The O29 water molecule also donates hydrogen bonds to oxygen atoms of two distinct, interstitial sulfate units. (Right) The O28 water molecule donates hydrogen bonds that connect to two distinct sulfate tetrahedra
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217 Thermodynamic cycles (Table 3) were used to calculate the standard-state enthalpy of
218 formation of each phase from the measured heats of dissolution. When sufficient sample was
219 available, additional measurements were done using a second AlexSYS calorimeter to verify
220 heat curve data. The standard-state enthalpies of formation from the binary oxides for lussierite,
221 péligotite, shumwayite, geschieberite, and bluelizardite are -3214 ± 78 , -2026 ± 33 , -587 ± 22 , -
222 966.1 ± 10.9 , and -2084 ± 21 kJ/mol, respectively. The standard-state enthalpies of formation of
223 each phase from its elements are -9743 ± 78 , -7220 ± 33 , -5255 ± 22 , -3916 ± 20 , and -7117 ± 21
224 kJ/mol, respectively.

225 Péligotite, lussierite and bluelizardite are structurally and chemically similar minerals,
226 which provides an opportunity to evaluate the internal consistency of the calorimetric results.
227 Each contains finite uranyl sulfate units linked through interstitial Na and H₂O, although
228 bluelizardite has Cl in the interstitial complex, and lussierite contains sulfate groups in the
229 interstitial complex. Literature values for ΔH_f° for H₂O, NaCl, and Na₂SO₄ are -285.5, -411.3,
230 and -1387.8 kJ/mol, respectively (Robie et al., 1978). The ΔH_f° for péligotite,
231 Na₆[(UO₂)(SO₄)₄](H₂O)₄, calculated from the thermochemical cycles is -7220 ± 33 kJ/mol. This
232 value can also be estimated starting with ΔH_f° (-9743 ± 78 kJ/mol) of lussierite,
233 Na₁₀[(UO₂)(SO₄)₄](SO₄)₂·3H₂O, by subtracting ΔH_f° for two moles of Na₂SO₄ and adding ΔH_f°
234 for one mole of H₂O, which yields -7253 ± 78 kJ/mol. Similarly, it can be estimated starting with

235 ΔH_f° (-7117 ± 21 kJ/mol) of blue lizardite, $\text{Na}_7[(\text{UO}_2)(\text{SO}_4)_4]\text{Cl}\cdot 2\text{H}_2\text{O}$, followed by subtracting
236 the ΔH_f° of one mole of NaCl and adding the ΔH_f° of two moles of H_2O , which yields $-7277 \pm$
237 21 kJ/mol.

238

239 **Implications**

240 Generally, SCXRD data for new minerals is collected on the X-ray diffractometer at
241 room temperature, ~ 20 °C. Excepting for phases unstable at room temperature, it is normally no
242 issue to determine the true structure of a mineral with modern diffractometers due to incremental
243 improvements in detector resolution and X-ray sources. However, heavy elements such as U
244 cause excessive X-ray scattering that can make accurately determining the thermal parameters of
245 light elements as heavy as even O quite difficult. Exact H atom positions are often impossible to
246 determine from natural uranium minerals and often the H-bond network must be estimated from
247 bond valence calculations. This is further complicated by hydrous minerals that have dehydrated
248 in the field prior to collection. Synthesis of uranyl mineral analogs in laboratory conditions
249 avoids the dehydration issue with natural samples. Further, using a cryostream will both stabilize
250 phases prone to dehydration and will reduce the X-ray scatter around U atoms such that H-atom
251 positions can be more readily found, as exemplified by the phases reported in this study.

252 The ΔH_f° value of péligotite calculated from thermochemical cycles in this study is in
253 close agreement with the ΔH_f° calculated from the starting ΔH_f° of similar minerals. This implies
254 that estimating the ΔH_f° values can be done for minerals that have yet to be synthesized in
255 laboratory conditions. For instance, ottohahnite, $\text{Na}_6(\text{UO}_2)_2(\text{SO}_4)_5(\text{H}_2\text{O})_7\cdot 1.5\text{H}_2\text{O}$, is structurally
256 similar to péligotite, lussierite and blue lizardite. Ottohahnite has no synthetic analog and its
257 enthalpy of formation is unknown, but using the ΔH_f° of péligotite and literature enthalpy values

258 an estimate can be made of the ΔH_f° of ottohahnite. The literature value of ΔH_f° for
259 $\text{UO}_2\text{SO}_4 \cdot 3\text{H}_2\text{O}$ is -2747.2 kJ/mol (Glushko, 1978; Karyakin et al., 2003). Starting with ΔH_f° of -
260 7220 ± 33 kJ/mol, then adding ΔH_f° for one mole of $\text{UO}_2\text{SO}_4 \cdot 3\text{H}_2\text{O}$ and ΔH_f° for 1.5 moles of
261 H_2O yields $-10,395.5 \pm 33$ kJ/mol for ottohahnite.

262 The rate of new mineral discoveries, particularly uranyl sulfates, is far outpacing the rate
263 at which analogs of minerals are being synthesized in laboratories. The newly described uranyl
264 sulfate minerals are diverse in structure and chemistry, indicating variations in local geochemical
265 conditions. However, aside from the minerals described in this study and a few others, most of
266 the uranyl sulfates have not been replicated in laboratory conditions and their thermodynamic
267 data is unknown. The lack of ΔH_f° data of these new minerals hampers a deeper understanding
268 of the formation processes behind these minerals. Previous efforts have been made to accurately
269 estimate the ΔH_f° values of uranyl minerals without experiment analysis or expensive DFT
270 simulations (Chen et al., 1999). The results of this study imply that accurate estimates can be
271 made of the ΔH_f° values of mineral phases by using ΔH_f° values from chemically and
272 structurally similar phases. This is not only accurate, but rapid and facile. This method will likely
273 be improved with more data points for study.

274 The standard state entropy of formation for zippeite is three orders of magnitude smaller
275 than the standard state enthalpy of formation (Sharifironizi and Burns, 2018; Sharifironizi et al.,
276 2016), indicating that the standard state enthalpy is the largest contributor to the standard state
277 free energy of the mineral. If that is the case for other uranyl sulfates, then estimating ΔH_f° of a
278 mineral using the method described here also allows for an accurate approximation of the ΔG_f° .
279 This is of potential value, as the high solubility of this suite of uranyl sulfates prevented
280 experimental determination of their solubility products. Geochemists that model uranium mineral

281 formation and uranium transport in acid mine conditions may therefore be interested in a means
282 of predicting the ΔG_f° of uranyl sulfate minerals that exist in defunct uranium mines, but have
283 yet to be replicated in a laboratory.

284 **Notes:**

285 The authors declare no competing interests.

286 **Acknowledgements**

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Table 3. Calorimetry thermal cycles for determination of enthalpy of formation (ΔH_f°). The number of calorimeter drops is indicated in parenthesis in the $\text{kJ}\cdot\text{mol}^{-1}$ column. Crystalline phase = xl; gas phase = g; solution = soln; liquid phase = l. The error was calculated as two standard deviations of the mean.

Reactions	Compound	Thermal Equation	$\text{kJ}\cdot\text{mol}^{-1}$	Reference
$\Delta H1$	ΔH_{ds} Lussierite	$\text{Na}_{10}[(\text{UO}_2)(\text{SO}_4)_4](\text{SO}_4)_2\cdot 3(\text{H}_2\text{O})_{(xl, 298\text{ K})} = 5\text{Na}_2\text{O}_{(soln, 973\text{ K})} + \text{UO}_3_{(soln, 973\text{ K})} + 6\text{SO}_3_{(soln, 973\text{ K})} + 3\text{H}_2\text{O}_{(g, 973\text{ K})}$	1120 ± 71 (5)	This study
$\Delta H2$	ΔH_{ds} Pélégotite	$\text{Na}_6[(\text{UO}_2)(\text{SO}_4)_4]\cdot 4\text{H}_2\text{O}_{(xl, 298\text{ K})} = 3\text{Na}_2\text{O}_{(soln, 973\text{ K})} + \text{UO}_3_{(soln, 973\text{ K})} + 4\text{SO}_3_{(soln, 973\text{ K})} + 4\text{H}_2\text{O}_{(g, 973\text{ K})}$	844 ± 25 (6)	This study
$\Delta H3$	ΔH_{ds} Shumwayite	$[(\text{UO}_2)(\text{SO}_4)(\text{H}_2\text{O})_2]_2\cdot \text{H}_2\text{O}_{(xl, 298\text{ K})} = 2\text{UO}_3_{(soln, 976\text{ K})} + 2\text{SO}_3_{(soln, 976\text{ K})} + 5\text{H}_2\text{O}_{(soln, 976\text{ K})}$	542 ± 14 (18)	This study
$\Delta H4$	ΔH_{ds} Geschieberite	$\text{K}_2[(\text{UO}_2)(\text{SO}_4)_2]\cdot 2(\text{H}_2\text{O})_{(xl, 298\text{ K})} = \text{K}_2\text{O}_{(soln, 973\text{ K})} + \text{UO}_3_{(soln, 973\text{ K})} + 2\text{SO}_3_{(soln, 973\text{ K})} + 2\text{H}_2\text{O}_{(g, 973\text{ K})}$	388 ± 6 (16)	This study
$\Delta H5$	ΔH_{ds} Bluelizardite	$\text{Na}_7[(\text{UO}_2)(\text{SO}_4)_4]\text{Cl}\cdot 2(\text{H}_2\text{O})_{(xl, 298\text{ K})} = 3\text{Na}_2\text{O}_{(soln, 973\text{ K})} + \text{UO}_3_{(soln, 973\text{ K})} + 4\text{SO}_3_{(soln, 973\text{ K})} + \text{NaCl}_{(soln, 973\text{ K})} + 2\text{H}_2\text{O}_{(g, 973\text{ K})}$	838.2 ± 1.9 (9)	This study
$\Delta H7$	ΔH_{ds} (UO_3)	$\text{UO}_3_{(xl, 298\text{ K})} = \text{UO}_3_{(soln, 973\text{ K})}$	9.5 ± 1.5	Helean et al. 2002
$\Delta H8$	ΔH_{ds} (SO_3)	$\text{SO}_3_{(g, 298\text{ K})} = \text{SO}_3_{(soln, 973\text{ K})}$	-203.7 ± 4.1	Navrotsky 2014
$\Delta H9$	ΔH_{ds} (Na_2O)	$\text{Na}_2\text{O}_{(xl, 298\text{ K})} = \text{Na}_2\text{O}_{(soln, 973\text{ K})}$	-217.6 ± 4.3	Tessier et al. 2000
$\Delta H10$	ΔH_{ds} (K_2O)	$\text{K}_2\text{O}_{(xl, 298\text{ K})} = \text{K}_2\text{O}_{(soln, 973\text{ K})}$	-318 ± 3	Tessier et al. 2000
$\Delta H11$	ΔH_{ds} (NaCl)	$\text{NaCl}_{(xl, 298\text{ K})} = \text{NaCl}_{(soln, 973\text{ K})}$	74.6 ± 1.1 (6)	This study
$\Delta H12$	ΔH_{hc} (H_2O)	$\text{H}_2\text{O}_{(l, 298\text{ K})} = \text{H}_2\text{O}_{(g, 973\text{ K})}$	69.01	Robie et al. 1978
$\Delta H13$	ΔH_f° (UO_3)	$\text{U}_{(xl, 298\text{ K})} + 1.5\text{O}_2_{(g, 298\text{ K})} = \text{UO}_3_{(xl, 298\text{ K})}$	-1223.8 ± 0.8	Robie et al. 1978
$\Delta H14$	ΔH_f° (SO_3)	$\text{S}_{(xl, 298\text{ K})} + 1.5\text{O}_2_{(g, 298\text{ K})} = \text{SO}_3_{(g, 298\text{ K})}$	-395.7 ± 0.7	Robie et al. 1978
$\Delta H15$	ΔH_f° (Na_2O)	$2\text{Na}_{(xl, 298\text{ K})} + 0.5\text{O}_2_{(g, 298\text{ K})} = \text{Na}_2\text{O}_{(xl, 298\text{ K})}$	-414.8 ± 0.3	Robie et al. 1978
$\Delta H16$	ΔH_f° (K_2O)	$2\text{K}_{(xl, 298\text{ K})} + 0.5\text{O}_2_{(g, 298\text{ K})} = \text{K}_2\text{O}_{(xl, 298\text{ K})}$	-363.2 ± 2.1	Robie et al. 1978
$\Delta H17$	ΔH_f° (NaCl)	$\text{Na}_{(xl, 298\text{ K})} + 0.5\text{Cl}_2_{(g, 298\text{ K})} = \text{NaCl}_{(xl, 298\text{ K})}$	-411.30 ± 0.10	Robie et al. 1978
$\Delta H18$	ΔH_f° (H_2O)	$\text{H}_2_{(g, 298\text{ K})} + 0.5\text{O}_2_{(g, 298\text{ K})} = \text{H}_2\text{O}_{(l, 298\text{ K})}$	-285.80 ± 0.10	Robie et al. 1978
$\Delta H19$	ΔH_{f-ox}° Lussierite	$5\text{Na}_2\text{O}_{(xl, 298\text{ K})} + \text{UO}_3_{(xl, 298\text{ K})} + 6\text{SO}_3_{(xl, 298\text{ K})} + 3\text{H}_2\text{O}_{(l, 298\text{ K})}$ $-\Delta H1 + 5\Delta H9 + 1\Delta H7 + 6\Delta H8 + 3\Delta H12$	-3214 ± 78	
$\Delta H20$	ΔH_f° Lussierite	$10\text{Na}_{(xl, 298\text{ K})} + \text{U}_{(xl, 298\text{ K})} + 6\text{S}_{(xl, 298\text{ K})} + 3\text{H}_2_{(g, 298\text{ K})} + 14.5\text{O}_2_{(g, 298\text{ K})}$ $-\Delta H1 + 5\Delta H9 + 1\Delta H7 + 6\Delta H8 + 3\Delta H12 + 5\Delta H15 + 1\Delta H13 + 6\Delta H14 + 3\Delta H18$	-9743 ± 78	
$\Delta H21$	ΔH_{f-ox}° Pélégotite	$3\text{Na}_2\text{O}_{(xl, 298\text{ K})} + \text{UO}_3_{(xl, 298\text{ K})} + 4\text{SO}_3_{(xl, 298\text{ K})} + 4\text{H}_2\text{O}_{(l, 298\text{ K})}$ $-\Delta H2 + 3\Delta H9 + 1\Delta H7 + 4\Delta H8 + 4\Delta H12$	-2026 ± 33	
$\Delta H22$	ΔH_f° Pélégotite	$6\text{Na}_{(xl, 298\text{ K})} + \text{U}_{(xl, 298\text{ K})} + 4\text{S}_{(xl, 298\text{ K})} + 4\text{H}_2_{(g, 298\text{ K})} + 11\text{O}_2_{(g, 298\text{ K})}$ $-\Delta H2 + 3\Delta H9 + 1\Delta H7 + 4\Delta H8 + 4\Delta H12 + 3\Delta H15 + 1\Delta H13 + 4\Delta H14 + 4\Delta H18$	-7220 ± 33	
$\Delta H23$	ΔH_{f-ox}° Shumwayite	$2\text{UO}_3_{(xl, 298\text{ K})} + 2\text{SO}_3_{(xl, 298\text{ K})} + 5\text{H}_2\text{O}_{(l, 298\text{ K})}$ $-\Delta H3 + 2\Delta H7 + 2\Delta H8 + 5\Delta H12$	-587 ± 22	
$\Delta H24$	ΔH_f° Shumwayite	$2\text{U}_{(xl, 298\text{ K})} + 2\text{S}_{(xl, 298\text{ K})} + 5\text{H}_2_{(g, 298\text{ K})} + 8.5\text{O}_2_{(g, 298\text{ K})}$ $-\Delta H3 + 2\Delta H7 + 2\Delta H8 + 5\Delta H12 + 2\Delta H13 + 2\Delta H14 + 5\Delta H18$	-5255 ± 22	

ΔH25	ΔH _{f-ox} ⁰ Geschieberite	1K ₂ O _(xl, 298 K) + UO _{3 (xl, 298 K)} + 2SO _{3 (xl, 298 K)} + 2H ₂ O _(l, 298 K)	-966 ± 11
		-ΔH4 + 1ΔH10 + 1ΔH7 + 2ΔH8 + 2ΔH12	
ΔH26	ΔH _f ⁰ Geschieberite	2K _(xl, 298 K) + U _(xl, 298 K) + 2S _(xl, 298 K) + 2H _{2 (g, 298 K)} + 12O _{2 (g, 298 K)}	-3916 ± 20
		-ΔH4 + 1ΔH10 + 1ΔH7 + 2ΔH8 + 2ΔH12 + 1ΔH16 + 1ΔH13 + 2ΔH14 + 2ΔH18	
ΔH27	ΔH _{f-ox} ⁰ Bluelizardite	3Na ₂ O _(xl, 298 K) + UO _{3 (xl, 298 K)} + 4SO _{3 (xl, 298 K)} + NaCl _(xl, 298 K) + 2H ₂ O _(l, 298 K)	-2084 ± 21
		-ΔH5 + 3ΔH9 + 1ΔH7 + 4ΔH8 + 1ΔH11 + 2ΔH12	
ΔH28	ΔH _f ⁰ Bluelizardite	7Na _(xl, 298 K) + U _(xl, 298 K) + 4S _(xl, 298 K) + 0.5Cl _{2 (g, 298 K)} + 2H _{2 (g, 298 K)} + 10O _{2 (g, 298 K)}	-7117 ± 21
		-ΔH5 + 3ΔH9 + 1ΔH7 + 4ΔH8 + 1ΔH11 + 2ΔH12 + 3ΔH15 + 1ΔH13 + 4ΔH14 + 1ΔH17 + 2ΔH18	

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