

### Revision 3

1 **Thermal equation of state of Li-rich schorl up to 15.5 GPa and 673**  
2 **K: Implications for lithium and boron transport in slab subduction**

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11 **ABSTRACT:** The thermal equation of state (EoS) of natural schorl has been  
12 established at high temperatures up to 673 K and high pressures up to 15.5 GPa using  
13 *in-situ* synchrotron X-ray diffraction combined with a diamond anvil cell. The  
14 pressure-volume (*P-V*) data were fitted to the third-order Birch-Murnaghan EoS with  
15  $V_0 = 1581.45 \pm 0.25 \text{ \AA}^3$ ,  $K_0 = 111.6 \pm 0.9 \text{ GPa}$  and  $K'_0 = 4.4 \pm 0.2$ ; additionally, when  
16  $K'_0$  was fixed at a value of 4,  $V_0 = 1581.04 \pm 0.20 \text{ \AA}^3$  and  $K_0 = 113.6 \pm 0.3 \text{ GPa}$ . The  $V_0$   
17 ( $1581.45 \pm 0.25 \text{ \AA}^3$ ) obtained by the third-order Birch-Murnaghan EoS agreed well  
18 with the measured  $V_0$  ( $1581.45 \pm 0.05 \text{ \AA}^3$ ) under ambient conditions; this result  
19 confirmed the high accuracy of the experimental data in this study. Furthermore, the  
20 axial compression data of the schorl at room temperature were also fitted to a  
21 “linearized” third-order Birch-Murnaghan EoS, and the obtained axial moduli for the  
22 *a*- and *c*-axes were  $K_a = 621 \pm 9 \text{ GPa}$  and  $K_c = 174 \pm 2 \text{ GPa}$ , respectively.  
23 Consequently, the axial compressibilities were  $\beta_a = 1.61 \times 10^{-3} \text{ GPa}^{-1}$  and  $\beta_c =$   
24  $5.75 \times 10^{-3} \text{ GPa}^{-1}$  with an anisotropic ratio of  $\beta_a:\beta_c = 0.28:1.00$ , indicating axial  
25 compression anisotropy. In addition, the compositional effect on the axial

26 compressibilities of tourmalines was also discussed. Fitting our  
27 pressure-volume-temperature ( $P$ - $V$ - $T$ ) data to the high-temperature third-order  
28 Birch-Murnaghan EoS provided the following thermal EoS parameters:  $V_0 = 1581.2 \pm$   
29  $0.2 \text{ \AA}^3$ ,  $K_0 = 110.5 \pm 0.6 \text{ GPa}$ ,  $K'_0 = 4.6 \pm 0.2$ ,  $(\partial K_T / \partial T)_P = -0.012 \pm 0.003 \text{ GPa K}^{-1}$  and  
30  $\alpha_{V0} = (2.4 \pm 0.2) \times 10^{-5} \text{ K}^{-1}$ . The obtained thermal EoS parameters in this study were  
31 also compared with those of previous studies on other tourmalines. The potential  
32 factors influencing the thermal EoS parameters of tourmalines were further discussed.  
33 **Keywords:** Schorl; Equation of state; High pressure and high temperature; X-ray  
34 diffraction; Diamond anvil cell

## 35 INTRODUCTION

36 Tourmaline is the most abundant and widespread borosilicate mineral on Earth. It  
37 forms over a wide range of temperature and pressure conditions, and typically occurs  
38 in a wide variety of granites, granitic pegmatites, sedimentary, metamorphic rocks,  
39 and even (ultra)high pressure metamorphic rocks (Slack 1996; Dutrow and Henry  
40 2011; van Hinsberg et al. 2011; Nabelek 2021; Ertl et al. 2022; Han et al. 2023;  
41 Vincent et al. 2023). Therefore, tourmaline is stable in environments that extend from  
42 the crust to ultrahigh pressure conditions prevailing in the upper mantle (Ota et al.  
43 2008; Dutrow and Henry 2011; van Hinsberg et al. 2011; Henry and Dutrow 2012)  
44 and can maintain equilibrium with a variety of geological fluids (Meyer et al. 2008;  
45 Konzett et al. 2012; Berryman et al. 2016). The diffusion rate of the main and trace  
46 elements in tourmaline is extremely low (van Hinsberg et al. 2011); thus, tourmaline  
47 may preserve textural, compositional, and isotopic features during growth and hence  
48 reveal considerable details regarding its crystallized environment (e.g., Maloney et al.  
49 2008; van Hinsberg et al. 2011; Berryman et al. 2017; Kotowski et al. 2020; Qiu et al.  
50 2021; Feng et al. 2022; Li et al. 2022; Guo et al. 2023). More importantly, as a  
51 dominant carrier of light elements (e.g., lithium and boron), tourmaline plays a vital  
52 role in the lithium and boron cycles in the deep Earth, especially in subduction zones  
53 (e.g., Nakano and Nakamura 2001; Bebout and Nakamura 2003; Ota et al. 2008; van  
54 Hinsberg et al. 2011; Liu and Jiang 2021; Srivastava and Singh 2022). Thus, studies

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55 of the thermal stability and equation of state (EoS) of tourmaline in the subduction  
56 slab can aid in the assessment of the lithium and boron cycle depth and explain the  
57 formation of lithium deposits.

58 Tourmaline is a kind of ring-silicate mineral, and its structure can be expressed as  
59  $XY_3Z_6T_6O_{18}(BO_3)_3V_3W$ , where  $X = Na^+, K^+, Ca^{2+}$ , vacancy;  $Y = Mg^{2+}, Fe^{2+}, Al^{3+}, Li^+$ ,  
60  $Fe^{3+}, Cr^{3+}, V^{3+}, Mn^{2+}$ ;  $Z = Al^{3+}, Fe^{3+}, Cr^{3+}, V^{3+}, Mg^{2+}, Fe^{2+}$ ;  $T = Si^{4+}, Al^{3+}, B^{3+}$ ;  $B =$   
61  $B^{3+}$ ;  $V = (OH)^-, O^{2-}$ ;  $W = (OH)^-, F^-, O^{2-}$  (Hawthorne and Henry 1999; Henry et al.  
62 2011). Tourmaline has a trigonal crystal system and belongs to the  $R3m$  space group  
63 (Fig. 1). Its structure consists of two alternating basic structural layers. One consists  
64 of sixfold rings of tetrahedra ( $T$  sites) with a threefold axis along the  $c$  direction. The  
65 other consists of octahedral clusters on top of the tetrahedral rings, with three inner  $Y$   
66 sites and six outer  $Z$  sites arranged concentrically. The  $X$  site occupies a  
67 nine-coordinate polyhedron above the center of the sixfold ring. B atoms form  
68  $[BO_3]^{3-}$  triangles linked to the  $Y$ - and  $Z$ -octahedra, almost perpendicular to the  $c$ -axis.

69 The chemical composition of tourmaline is diverse, and there are many isomorphic  
70 substituents in its structure (Hawthorne and Henry 1999; Bosi et al. 2022). The  
71 physical properties of tourmaline, such as the intrinsic dipole moment (Kim et al.  
72 2018) and bulk modulus (Berryman et al. 2019; Chen et al. 2022), depend on the type  
73 of cation at the  $X$ ,  $Y$ , and  $Z$  positions. Schorl (Fe-rich tourmaline) is the most common  
74 in the tourmaline supergroup, occurring in pegmatites and granites (e.g., Novák et al.  
75 2004; Filip et al. 2012; Chakraborty 2021; Zhao et al. 2022). In addition, schorl is also  
76 an important petrogenetic indicator due to its ubiquity and sensitivity to  $fO_2$   
77 conditions (e.g., Foit et al. 1989; Fuchs et al. 2002; Pieczka and Kraczká 2004).

78 To date, pressure-volume ( $P$ - $V$ ) EoS studies of tourmalines (e.g., uvite, dravite,  
79 schorl, maruyamaite, magnesio-foitite, olenite, and elbaite) have been widely carried  
80 out using synchrotron X-ray diffraction (XRD) combined with a diamond anvil cell  
81 (e.g., Li et al. 2004; Xu et al. 2016; O'Bannon III et al. 2018; Berryman et al. 2019;  
82 Likhacheva et al. 2019; Chen et al. 2022). For instance, Li et al. (2004) performed the  
83 first *in situ* high-pressure synchrotron energy-dispersive XRD experiments on a  
84 natural schorl up to 27.8 GPa using a methanol-ethanol-water mixture (16:3:1) as the

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85 pressure medium. They obtained a bulk modulus  $K_0 = 184(4)$  GPa with a fixed  
86 pressure derivative of  $K'_0 = 4$ . However, O'Bannon III et al. (2018) conducted  
87 synchrotron single-crystal XRD measurements on a natural dravite at high pressures  
88 up to ~24 GPa using neon as the pressure medium and obtained  $K_0 = 109.6(3.2)$  GPa  
89 and  $K'_0 = 4.6(8)$ . The  $K_0$  of dravite obtained by O'Bannon III et al. (2018) is  
90 significantly less than that of schorl obtained by Li et al. (2004). Later, Likhacheva et  
91 al. (2019) studied the compressibility of natural maruyamaite using synchrotron XRD  
92 up to 20 GPa with a helium pressure medium, and the obtained  $K_0 = 112(3)$  GPa was  
93 also clearly less than that of Li et al. (2004). In addition, Berryman et al. (2019)  
94 collected synchrotron single-crystal XRD patterns of five synthetic Mg-Al  
95 tourmalines (dravite, K-dravite, magnesio-foitite, oxy-uvite, and olenite) at  
96 high-pressures up to 60 GPa with a neon pressure medium, and the reported  $K_0$  ranged  
97 from 97(6) GPa to 116(6) GPa. Moreover, Chen et al. (2022) recently investigated the  
98 EoS of natural elbaite using *in situ* synchrotron XRD at high pressures up to 21.1 GPa  
99 with a neon pressure medium and concluded that the reasonable range of  $K_0$  for  
100 tourmalines was 106-128 GPa. Therefore, the  $K_0$  of the schorl reported by Li et al.  
101 (2004) seems abnormally high and unreasonable. However, further studies on the EoS  
102 are needed to resolve this discrepancy.

103 To the best of our knowledge, few experimental studies on the  
104 pressure-volume-temperature ( $P$ - $V$ - $T$ ) EoS of tourmaline under high pressure and high  
105 temperature conditions are available. To date, the only previous  $P$ - $V$ - $T$  EoS study of  
106 tourmaline was by Xu et al. (2016), who tested a natural uvite up to 18 GPa and 723  
107 K and obtained its thermal EoS parameters. However, the  $P$ - $V$ - $T$  EoS of other  
108 tourmalines has not yet been reported. Thus, additional  $P$ - $V$ - $T$  EoS studies on  
109 tourmalines with different compositions are needed to evaluate the compositional  
110 influence on the thermal EoS parameters (Fan et al. 2015b; Ye et al. 2019; Li et al.  
111 2022; Xu et al. 2020, 2022a).

112 In this study, we investigated the  $P$ - $V$ - $T$  relationships of schorl up to 15.5 GPa and  
113 673 K, using a diamond anvil cell combined with *in situ* synchrotron XRD. First, the  
114 compressibility of the schorl under room temperature and high pressure conditions

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115 was determined. In addition, we compared the compressibility of schorl and elbaite,  
116 and analyzed the possible influencing factors. Moreover, the anisotropic linear  
117 compressibilities of schorl and elbaite were also discussed. Finally, the thermal EoS  
118 properties of the schorl were obtained by fitting the  $P$ - $V$ - $T$  data to the high  
119 temperature Birch-Murnaghan EoS. Our results were also compared with those of  
120 previous studies on other tourmalines.

## 121 **SAMPLE AND EXPERIMENT**

122 The tourmaline selected in this study is a natural sample with a good columnar  
123 crystal morphology. Chemical analyses (Table 1) were carried out by various  
124 methods, including electron probe microanalysis (EPMA) and laser ablation  
125 inductively coupled plasma mass spectrometry (LA-ICP-MS).

126 The chemical composition of the tourmaline sample was determined by EMPA  
127 with a JEOL JXA-8230 instrument using a 15 kV accelerating voltage, a 20 nA beam  
128 current, and a beam diameter of 5  $\mu\text{m}$ . The element peaks and backgrounds were  
129 measured for all elements with counting times of 10 s and 5 s, respectively. The  
130 following standards were used: hornblende ( $\text{SiO}_2$ ,  $\text{TiO}_2$ ,  $\text{MgO}$ ,  $\text{CaO}$ ,  $\text{Na}_2\text{O}$ ,  $\text{K}_2\text{O}$ , and  
131  $\text{Al}_2\text{O}_3$ ), gahnite ( $\text{ZnO}$ ), olivine ( $\text{NiO}$ ), pyrope ( $\text{FeO}$ ,  $\text{MnO}$ , and  $\text{Cr}_2\text{O}_3$ ) and fluorite (F).  
132 The data were reduced online using the ZAF program. More detailed experimental  
133 conditions for the EMPA measurements are reported by Chen et al. (2022, 2023).

134 Because some significant components (e.g., Li, B and  $\text{H}_2\text{O}$ ) cannot be directly  
135 determined by EMPA, the concentrations of Li and B in the tourmaline sample were  
136 investigated by LA-ICP-MS at the State Key Laboratory of Ore Deposit  
137 Geochemistry, Institute of Geochemistry, Chinese Academy of Sciences. An Agilent  
138 7500 ICP-MS instrument was connected to a GeoLas Pro 193-nm ArF excimer laser  
139 ablation system. A beam diameter of 15  $\mu\text{m}$  with a laser repetition rate of 10 Hz was  
140 used. Helium was used as the carrier gas and was mixed with argon via a T-connector  
141 before entering the ICP-MS instrument. The glass standard NIST610 was used for  
142 external calibration. More detailed analysis conditions are reported by Tang et al.  
143 (2020).

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144 Previous studies have shown that the OH content can be relatively accurately  
145 determined by the charge balance (e.g., Henry et al. 2002). Thus, the amount of OH-  
146 at the *V*- and *W*-sites can be evaluated from bond valence sum calculations. The  
147 Windows program WinTcac developed by Yavuz et al. (2014) was used to calculate  
148 the chemical formula of the tourmaline sample from the EMPA and LA-ICP-MS data.  
149 In this study, the OH content was calculated by considering  $\text{OH} + \text{O} + \text{F} = 4$  apfu and  
150  $V = \text{OH} = 3$  apfu. The estimated chemical formula was  
151  $(\text{Na}_{0.75}\text{Ca}_{0.04}\text{K}_{0.01}\square_{0.20})(\text{Al}_{0.78}\text{Li}_{0.74}\text{Fe}_{1.32}\text{Mn}_{0.04}\text{Mg}_{0.08}\text{Zn}_{0.01}\text{Ti}_{0.03})\text{Al}_6\text{Si}_{6.09}\text{O}_{18}(\text{BO}_3)_3(\text{O}$   
152  $\text{H})_3(\text{OH}_{0.27}\text{F}_{0.03}\text{O}_{0.70})$ , where  $\square$  indicates vacancy. Finally, the species of the  
153 tourmaline sample was additionally verified by the spreadsheet of Henry et al. (2011),  
154 and the chemical composition corresponded to the schorl species (Li-rich schorl).

155 The pure schorl mineral grains were selected by hand under a microscope and then  
156 ground under ethanol in an agate mortar for 4-6 h to an average grain size of  $\sim 10$   $\mu\text{m}$ .  
157 The ground samples were heated at 100 °C in a constant temperature furnace for 2 h  
158 to eliminate the absorbed water before being used in the subsequent synchrotron XRD  
159 experiments.

160 High pressure and high temperature experiments were carried out by using a  
161 modified Merrill-Bassett diamond anvil cell with a pair of 500  $\mu\text{m}$  culet-size diamond  
162 anvils. The sample chamber was prepared from a rhenium gasket with a preindented  
163 thickness of  $\sim 60$   $\mu\text{m}$  and a 300  $\mu\text{m}$ -diameter hole in the center of the indented region.  
164 The schorl powder was mixed with 3 wt.% platinum powder as the pressure calibrant  
165 by mechanically grinding the mixture for approximately 2 h. Subsequently, the  
166 mixture was lightly pressed between two opposing diamond anvils to form an  
167 approximately 25  $\mu\text{m}$  thick disk, and a piece of the pressed sample approximately 100  
168  $\mu\text{m}$  in diameter was loaded into the sample chamber. A methanol-ethanol-water  
169 mixture (16:3:1) was used as the pressure transmitting medium. The pressure was  
170 determined using the thermal EoS of platinum (pressure marker) (Fei et al. 2007).  
171 Heating was carried out by using a resistance-heating system, and the temperature  
172 was measured by a Pt<sub>90</sub>Rh<sub>10</sub>-Pt<sub>100</sub> thermocouple attached to one of the diamond anvils

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173 approximately 500  $\mu\text{m}$  away from the diamond culet. The resistance-heating system  
174 provides a stable and uniform temperature distribution within the pressure chamber  
175 and reliable temperature control by means of a thermocouple. Moreover, the  
176 exceptional thermal conductivity of the diamond anvil has the major advantage of  
177 transferring heat to the sample inside the pressure chamber. Thus, obtaining a stable  
178 and uniform temperature distribution within the pressure chamber highly depends on  
179 the stabilization time at high temperature and the tightness of the thermocouple glued  
180 to the diamond. Thus, to ensure that the thermocouple correctly reflected the  
181 temperature of the sample chamber, we tightly glued the thermocouple to the diamond.  
182 Each *in situ* XRD pattern was collected after the experimental temperature was  
183 maintained for 600 s for temperature stability. The temperatures of the sample  
184 chamber were actively stabilized using a temperature controller with a self-tuning  
185 function, and the fluctuation temperature displayed by the temperature controller was  
186 within  $\pm 1$  K. The exposure time for collecting diffraction patterns of the sample was  
187 600 s. Details of the experimental setup and cell assembly were described in  
188 previously published articles (e.g., Fan et al. 2010).

189 *In situ* high pressure and high temperature angle-dispersive XRD experiments were  
190 conducted at the 4W2 beamline of the Beijing Synchrotron Radiation Facility (BSRF).  
191 A Pilatus detector was used to collect diffraction patterns. The wavelength of the  
192 monochromatic X-ray beam was 0.6199 (1)  $\text{\AA}$ , which was calibrated by scanning  
193 through the Mo metal *K*-absorption edge. The beam size was focused to  $20 \times 30 \mu\text{m}^2$   
194 by a pair of Kirkpatrick-Baez mirrors (Kirkpatrick and Baez 1948). The tilting and  
195 rotation of the detector relative to the incident X-ray beam were calibrated using  
196 cerium dioxide ( $\text{CeO}_2$ ) powder as the XRD standard. The sample-detector distance  
197 was calculated from the powder  $\text{CeO}_2$  diffraction pattern under ambient conditions.

198 The diffraction patterns were integrated to generate conventional one-dimensional  
199 profiles using the *Fit2D* program (Hammersley et al. 1996). The diffraction peak  
200 positions were fitted by *Origin 8.5* software. The unit-cell parameters and volumes  
201 were calculated using *UnitCell* software (Holland and Redfern 1997).

## 202 RESULTS

203 The typical XRD patterns of the schorl at various pressures and temperatures are  
204 shown in Figure 2. With increasing pressure at different temperatures (Fig. 2), all  
205 peaks shifted toward higher  $2\theta$  angles. Moreover, the number of peaks in the  
206 diffraction data of the schorl sample did not change over the experimental  
207 pressure-temperature range (Fig. 2), indicating that no structural transition occurred.  
208 The unit-cell parameters and volumes of the schorl at various pressure and  
209 temperature conditions are listed in Tables 2 and 3. Figures 3 and 4 show the  
210 volumetric and axial compression of the schorl in this study. In addition, the XRD  
211 data collected under ambient conditions yielded the unit-cell parameters and volumes  
212 of  $a_0 = 15.9532(3) \text{ \AA}$ ,  $c_0 = 7.1751(3) \text{ \AA}$ , and  $V_0 = 1581.45(5) \text{ \AA}^3$ .

213 We first fitted the  $P$ - $V$  data collected at the 300 K isotherm to the room-temperature  
214 Birch-Murnaghan EoS. Then, we employed another common method, the  
215 high-temperature Birch-Murnaghan EoS approach, to derive the thermal EoS  
216 parameters from the measured  $P$ - $V$ - $T$  data.

### 217 Room-temperature Birch-Murnaghan equation of state

218 The pressure-volume ( $P$ - $V$ ) relationships were determined by fitting the room  
219 temperature data to a third-order Birch-Murnaghan EoS, which is represented as  
220 follows (Birch 1947):

$$221 \quad P = (3/2)K_0[(V_0/V)^{7/3} - (V_0/V)^{5/3}] \times \{1 + (3/4)(K'_0 - 4)[(V_0/V)^{2/3} - 1]\} \quad (1)$$

222 where  $V_0$ ,  $K_0$ , and  $K'_0$  are the zero-pressure unit-cell volume, zero-pressure isothermal  
223 bulk modulus and its pressure derivative, respectively. Analyses of Eq. (1) by the  
224 *EoSFit* program (Angel et al. 2014; Gonzalez-Platas et al. 2016) with all parameters  
225 free yielded:  $V_0 = 1581.45 \pm 0.25 \text{ \AA}^3$ ,  $K_0 = 111.6 \pm 0.9 \text{ GPa}$ , and  $K'_0 = 4.4 \pm 0.2$  (Table  
226 4). The refined value of  $V_0$  ( $1581.45(25) \text{ \AA}^3$ ) was within approximately  $1\sigma$  compared  
227 with the  $V_0$  ( $1581.45(5) \text{ \AA}^3$ ) measured by XRD under ambient conditions; this  
228 indicated the excellent accuracy of the refined results (Angel 2000). With  $K'_0$  fixed at  
229 4, the results were  $V_0 = 1581.04 \pm 0.20 \text{ \AA}^3$ , and  $K_0 = 113.6 \pm 0.3 \text{ GPa}$ . In addition, with  
230  $V_0$  fixed at  $1581.45 \text{ \AA}^3$ , the results were  $K_0 = 111.6 \pm 0.4 \text{ GPa}$ , and  $K'_0 = 4.4 \pm 0.1$ .



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231 To evaluate the quality of our third-order Birch-Murnaghan EoS fitting, the  
232 relationship between the Eulerian definition of finite strain  $f_E$  ( $f_E = [(V_0/V)^{2/3} - 1]/2$ )  
233 and the “normalized stress”  $F_E$  ( $F_E = P/3f_E(1+2f_E)^{5/2}$ ) (Birch 1978) is plotted and  
234 shown in Figure 5a. The weighted linear fit of the data points yielded an intercept  
235 value of  $F_{EV}(0) = 111.9$  (4) GPa, which was in good agreement with the isothermal  
236 bulk modulus obtained by the third-order Birch-Murnaghan EoS ( $K_0 = 111.6$  (9)  
237 GPa). Moreover, the functions of  $F_E$  and  $f_E$  had a slightly positive slopes, indicating  
238 that  $K'_0$  was greater than 4; this results was consistent with  $K'_0 = 4.4$  (2) from the  
239 third-order Birch-Murnaghan EoS. Therefore, the obtained EoS parameters from the  
240 third-order Birch-Murnaghan EoS fitting are a reasonable description of the  $P$ - $V$  data  
241 in this study.

242 The normalized unit-cell parameters ( $a/a_0$  and  $c/c_0$ ) of schorl at room temperature  
243 are plotted as a function of pressure in Figure 4. By fitting the unit-cell parameters of  
244 the schorl at room temperature using a “linearized” third-order Birch-Murnaghan EoS  
245 with the *EosFit* program (Angel et al. 2014; Gonzalez-Platas et al. 2016), the obtained  
246  $a_0$  and  $c_0$  are 15.9532 (3) Å and 7.1751 (3) Å, respectively. The refined unit-cell  
247 parameters are consistent with the results obtained from the XRD measurements  
248 under ambient conditions in this study due to their uncertainties (Table 2). The refined  
249 linear moduli and their pressure derivatives are  $K_a = 621$  (9) GPa,  $K_c = 174$  (2) GPa  
250 and  $K'_a = 16$  (3),  $K'_c = 8.7$  (5), respectively. In addition, the weighted linear fit of the  
251  $F_E$ - $f_E$  data points yields intercepts of  $F_{Ea}(0) = 620$  (6) GPa for the  $a$ -axis and  $F_{Ec}(0) =$   
252  $174$  (1) GPa for the  $c$ -axis; these results effectively agree with the results from the  
253 “linearized” third-order Birch-Murnaghan EoS. Moreover, the slopes obtained from  
254 the linear fits of the  $F_E$ - $f_E$  plots are positive for the  $a$ -axis and negative for the  $c$ -axis  
255 (Figs. 5b and 5c). The results are in good agreement with  $K'_a > 12$  and  $K'_c < 12$  from  
256 the “linearized” third-order Birch-Murnaghan EoS fits.

257 The axial compressibility  $\beta_l$  under ambient conditions has the following form  
258 (Angel et al. 2014):

$$259 \quad \beta_l = 1/K_l \quad (2)$$

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260 In analyses using Eq. (2) with  $K_l$ , we obtained the compressibility of the  $a$ - and  
261  $c$ -axes and they were determined to be  $1.61 \times 10^{-3} \text{ GPa}^{-1}$  and  $5.75 \times 10^{-3} \text{ GPa}^{-1}$ ,  
262 respectively; these results indicated that schorl has axial compressive anisotropy. The  
263  $c$ -axis of the schorl was 3.57 times more compressible than the  $a$ -axis under ambient  
264 conditions (Fig. 4).

265 **High-temperature Birch-Murnaghan equation of state**

266 The  $P$ - $V$ - $T$  data (Table 3) were used to determine the thermal EoS parameters of  
267 schorl up to  $\sim 15.50 \text{ GPa}$  and  $673 \text{ K}$ . The third-order Birch-Murnaghan EoS was  
268 applied to our high pressure and high temperature data as follows:

$$269 \quad P = (3/2)K_{T0}[(V_{T0}/V)^{7/3} - (V_{T0}/V)^{5/3}] \times \{1 + (3/4)(K'_{T0} - 4)[(V_{T0}/V)^{2/3} - 1]\} \quad (3)$$

270 In this equation, the thermal dependences of the zero-pressure unit-cell volume  $V_{T0}$   
271 and bulk modulus  $K_{T0}$  at different isotherms are expressed using the following  
272 equations:

$$273 \quad V_{T0} = V_0 \exp \int_{300}^T \alpha_T dT \quad (4)$$

$$274 \quad K_{T0} = K_0 + (\partial K_T / \partial T)_P \times (T - 300) \quad (5)$$

275 where  $V_0$  is the volume at zero-pressure and room-temperature, and the temperature  
276 derivative of  $V_{T0}$  can be estimated by a function of the thermal expansion  $\alpha_T$  (Eq. 4).  
277 The thermal dependence of the bulk modulus  $K_{T0}$  is expressed by a linear function of  
278 temperature (Eq. 5), assuming that the temperature derivative  $(\partial K_T / \partial T)_P$  is constant in  
279 the temperature range of this study.

280 The obtained thermal EoS parameters  $\alpha_{V0}$ ,  $(\partial K_T / \partial T)_P$ ,  $K_0$  and  $K'_0$  for the schorl in  
281 this study are shown in Table 4, and are compared with those from other tourmalines  
282 in previous studies. Fitting of the  $P$ - $V$ - $T$  data to the high-temperature third-order  
283 Birch-Murnaghan EoS yields the following results for the schorl:  $V_0 = 1581.2 \pm 0.2 \text{ \AA}^3$ ,  
284  $K_0 = 110.5 \pm 0.6 \text{ GPa}$ ,  $K'_0 = 4.6 \pm 0.2$ ,  $(\partial K_T / \partial T)_P = -0.012 \pm 0.003 \text{ GPa K}^{-1}$  and  $\alpha_{V0} =$   
285  $(2.4 \pm 0.2) \times 10^{-5} \text{ K}^{-1}$ . The obtained  $V_0$ ,  $K_0$  and  $K'_0$  determined here are very consistent  
286 with those from the  $P$ - $V$  data fitting at  $300 \text{ K}$  within their uncertainties. The measured  
287 unit-cell volumes are plotted in Figure 6 as a function of pressure together with the  
288 isotherms calculated using the thermal EoS parameters derived from the current fits;

289 the results show good agreement between the fit and the measured  $P$ - $V$ - $T$  data.

## 290 **DISCUSSION**

291 The  $P$ - $V$  EoS of various tourmalines (e.g., uvite, dravite, maruyamaite, foitite,  
292 olenite, and elbaite) has been investigated in previous high-pressure XRD  
293 experiments, but  $P$ - $V$  EoS studies on schorl are limited. To date, only Li et al. (2004)  
294 reported the  $P$ - $V$  EoS of schorl, they measured the compressibility of a natural  
295 tourmaline (schorl) at high pressures up to 27.8 GPa using the synchrotron XRD  
296 method. Although they did not characterize the composition of their tourmaline  
297 sample, they reported that the natural tourmaline sample was schorl (Li et al. 2004).  
298 They used a methanol-ethanol-water (at a ratio of 16:3:1) pressure medium and  
299 obtained an unusually high  $K_0$  value of 184 (4) GPa (with fixed  $K'_0 = 4$ ). In contrast,  
300 the obtained  $K_0$  (113.6 (3) GPa) of schorl in this study (with fixed  $K'_0 = 4$ ) is ~38%  
301 lower. From Figures 3 and 4, the volumetric and axial compression of the schorl from  
302 Li et al. (2004) is not only very scattered and irregular but also significantly greater  
303 than the volumetric and axial compression of the schorl in this study and of the elbaite  
304 in the study by Chen et al. (2022). Notably, the experimental maximum pressure  
305 (~27.8 GPa) from the study by Li et al. (2004) greatly exceeded the hydrostatic  
306 pressure condition (~10.5 GPa) of their pressure medium (Angel et al. 2007; Klotz et  
307 al. 2009a). Thus the previously reported  $K_0 = 184$  (4) GPa by Li et al. (2004) should  
308 be considered unreasonable and inaccurate.

309 In this study, we also used a methanol-ethanol-water mixture with a ratio of 16:3:1  
310 for the pressure media. This pressure medium solidifies at pressures above ~10.5 ( $\pm$   
311 0.5) GPa, and therefore the hydrostatic pressure environment in the sample chamber  
312 may be significantly influenced (Angel et al., 2007; Klotz et al. 2009a). However, we  
313 did not collect data far above the hydrostatic limit of the pressure medium, as in Li et  
314 al. (2004). In addition, previous studies have demonstrated that the hydrostatic limits  
315 can be considerably increased by modest heating (Klotz et al. 2009b). Thus, the  
316 sample chamber in this study was heated to 673 K at pressures for the relaxation of  
317 deviatoric stress (Fan et al. 2017b). Furthermore, to evaluate the possible influence of

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318 nonhydrostatic conditions on the  $P$ - $V$ - $T$  EoS fitting results, we also fitted the  $P$ - $V$ - $T$   
319 EoS of schorl after removing the experimental data with pressures greater than  $\sim 12$   
320 GPa, and obtained the following results for the schorl:  $V_0 = 1581.4 \pm 0.5 \text{ \AA}^3$ ,  $K_0 =$   
321  $111.5 \pm 1.5 \text{ GPa}$ ,  $K'_0 = 4.6 \pm 0.3$ ,  $(\partial K_T / \partial T)_P = -0.009 \pm 0.003 \text{ GPa K}^{-1}$  and  $\alpha_{V0} = (2.1 \pm$   
322  $0.2) \times 10^{-5} \text{ K}^{-1}$ . These values are very consistent with all the  $P$ - $V$ - $T$  data fitting results  
323 within their uncertainties (Table 4). Based on the above analysis, we deduce that the  
324 sample chamber in this study maintains a good hydrostatic pressure environment at  
325 pressures up to 16.05 GPa.

326 Recently Chen et al. (2022) summarized the results from previous experiments and  
327 discussed in detail the potential factors behind the discrepancies in  $K_0$  and  $K'_0$  among  
328 tourmalines. They concluded that the different pressure media,  $K'_0$  values and mineral  
329 compositions could all contribute to the discrepancies in the reported bulk moduli of  
330 tourmalines. They further inferred that excluding the influence of external factors  
331 such as the pressure medium, reasonable ranges of  $K_0$  and  $K'_0$  could be 106-128 GPa  
332 and 3.5-5.0, respectively. The obtained  $K_0$  (111.6 (9) GPa) and  $K'_0$  (4.4 (2)) of the  
333 schorl in this study are both within the aforementioned range. Thus the above analysis  
334 not only indicates that our results are more reasonable but also further confirms the  
335 reliability of the  $K_0$  and  $K'_0$  ranges summarized by Chen et al. (2022). In addition,  
336 there are similarities between the composition of tourmaline in this study and that of  
337 Chen et al. (2022); specifically, both are Li- and Fe-bearing tourmaline. Thus, the  
338 obtained  $P$ - $V$  EoS parameters of the schorl in this study and those of the elbaite from  
339 Chen et al. (2022) enable the further exploration the compositional influence (e.g., Fe  
340 or Li) on the volumetric and axial compressibilities of Li-bearing tourmalines.

341 Table 4 also shows that the  $K_0$  and  $K'_0$  of the elbaite reported by Chen et al. (2022)  
342 are  $\sim 2.8\%$  and  $\sim 4.5\%$  greater than those of the schorl in this study, respectively. In  
343 static compression studies, a trade-off exists between the fitted  $K_0$  and  $K'_0$ , which are  
344 negatively correlated. Considering the correlation between  $K_0$  and  $K'_0$  in an EoS fit,  
345 we cannot only compare  $K_0$  and neglect the  $K'_0$ . Thus, to accurately evaluate the  
346 difference between the  $K_0$  values obtained in this study and those reported by Chen et  
347 al. (2022), we compared the results with a fixed  $K'_0$  value of 4.0. From Table 4, the  $K_0$

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348 values of this study and Chen et al. (2022) with a fixed  $K'_0$  of 4.0 are 113.6(3) GPa  
349 and 116.4(4) GPa, respectively. The obtained  $K_0$  in this study for schorl is ~2.4%  
350 lower than that reported by Chen et al. (2022).

351 By carefully examining the composition characteristics of elbaite  
352  $[(\text{Na}_{0.62}\text{Ca}_{0.04}\square_{0.34})(\text{Al}_{1.90}\text{Li}_{0.98}\text{Fe}_{0.09}\text{Mn}_{0.02})\text{Al}_6\text{Si}_6\text{O}_{18}(\text{BO}_3)_3(\text{OH})_3(\text{OH}_{0.20},\text{F}_{0.48},\text{O}_{0.32})]$   
353 from Chen et al. (2022) and schorl  
354  $(\text{Na}_{0.75}\text{Ca}_{0.04}\text{K}_{0.01}\square_{0.20})(\text{Al}_{0.78}\text{Li}_{0.74}\text{Fe}_{1.32}\text{Mn}_{0.04}\text{Mg}_{0.08}\text{Zn}_{0.01}\text{Ti}_{0.03})\text{Al}_6\text{Si}_{6.09}\text{O}_{18}(\text{BO}_3)_3(\text{O}$   
355  $\text{H})_3(\text{OH}_{0.27}\text{F}_{0.03}\text{O}_{0.70})$  in this study, the  $X$  sites in these samples are relatively simple.  
356 They are predominantly occupied by Na, some of them are vacant ( $\square$ ), and the other  
357 elements (e.g., Ca and K) are negligible. However, the compositional variation at the  
358  $X$  site in tourmalines merely leads to changes in the neighboring O1–H1 bond without  
359 any identifiable changes in the lattice-bonding environment (Berryman et al. 2016).  
360 Thus, the  $X$ -site-occupying ion does not have a demonstrable effect on the  
361 compression behavior of tourmaline (Berryman et al. 2019; Chen et al. 2022).

362 However, in comparison to the simple compositional variation at the  $X$  site of these  
363 two tourmalines in this study and that reported by Chen et al. (2022), the  
364 compositional characteristics at the  $Y$  site are more complex. For the elbaite sample  
365 from Chen et al. (2022), the  $Y$  site is predominantly occupied by Al and Li, with a few  
366 other elements (e.g., Fe and Mn). In contrast, except for Al and Li, the schorl sample  
367 in this study contains a significant amount of Fe at the  $Y$  site. The effective ionic radii  
368 of  $\text{Fe}^{2+}(\text{VI})$  (0.776 Å) are ~41.9% larger than those of  $\text{Al}^{3+}(\text{VI})$  (0.547 Å) (Bosi 2018).  
369 As a consequence, the mean bond length of  $\text{Fe}^{2+}\text{-O}$  (2.1536 Å) at the  $Y$  site is ~13.1%  
370 greater than the mean bond length of  $\text{Al}^{3+}\text{-O}$  (1.9043) (Bačík and Fridrichová 2021).  
371 Accordingly, the bond strength of  $\text{Fe}^{2+}\text{-O}$  in the schorl is weaker than that of  $\text{Al}^{3+}\text{-O}$ .  
372 Therefore, the schorl exhibits greater compressibility and a smaller isothermal bulk  
373 modulus.

374 Thus, based on the above discussion, the bond strengths of  $\text{Fe}^{2+}\text{-O}$  at the  $Y$  site may  
375 mainly contribute to the different compressibilities between the schorl in this study  
376 and the elbaite in Chen et al. (2022). This reasoning is consistent with the conclusion

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377 of Chen et al. (2023), who suggested that the bond strengths of the corresponding  
378 bonds at the *Y* site likely have a significant effect on the expansibility of Li-bearing  
379 tourmaline. Furthermore, to the best of our knowledge, there have been only two  
380 previous studies on the *P-V* EoS of Fe-bearing tourmalines, one study by Chen et al.  
381 (2022) investigated the *P-V* EoS of Fe-bearing elbaite, while the other one by  
382 Likhacheva et al. (2019) examined the *P-V* EoS of Fe-bearing maruyamaite  
383 (K-tourmaline) with the composition of  
384  $(\text{Na}_{0.28}\text{Ca}_{0.19}\text{K}_{0.54})(\text{Al}_{1.17}\text{Fe}_{0.39}\text{Mg}_{1.3}\text{Ti}_{0.14})(\text{Al}_5\text{Mg})[\text{Si}_{5.95}\text{Al}_{0.05}\text{O}_{18}](\text{BO}_3)_3(\text{OH}_{2.31}\text{O}_{1.69})$ .  
385 Thus, in this study, based on the obtained *P-V* EoS of the schorl and combining our  
386 results with the *P-V* EoS of previous studies (Likhacheva et al. 2019; Chen et al.  
387 2022), we constructed a relationship between the  $K_0$  values and the Fe content at the *Y*  
388 site of Fe-bearing tourmalines (Fig. 7). In addition, to accurately evaluate the  
389 influence of the Fe content on the  $K_0$  of Fe-bearing tourmalines, we compared their  $K_0$   
390 values while keeping  $K'_0$  fixed at 4.0. The  $K_0$  of the Fe-bearing tourmalines shows a  
391 linear relationship with the Fe content. Within the experimental uncertainties,  $K_0$   
392 decreases linearly with increasing Fe content (Fig. 7):

$$393 \quad K_0 = 116.59 (0.05) - 6.8 (0.1) X_{\text{Fe}} \quad (R^2 = 0.999) \quad (6)$$

394 where  $X_{\text{Fe}} = \text{Fe} / (\text{Fe} + \text{Mg} + \text{Li} + \text{Al})$  is the Fe content at the *Y* site of the tourmalines.  
395 Thus, the above equation further indicates that the bond strength of  $\text{Fe}^{2+}\text{-O}$  at the *Y*  
396 site likely has a significant effect on the compressibility of Fe-bearing tourmaline.

397 The axial compressibility of the schorl in this study indicates that the *c*-axis is  
398 softer than the *a*-axis. The calculated axial compressibilities are  $\beta_a = 1.61 \times 10^{-3} \text{ GPa}^{-1}$   
399 and  $\beta_c = 5.75 \times 10^{-3} \text{ GPa}^{-1}$ , resulting in an anisotropic ratio of  $\beta_a:\beta_c = 0.28:1.00$ . Thus,  
400 our results reinforce the highly anisotropic elasticity of tourmaline. Similar  
401 anisotropic compression behaviors have been reported for natural elbaite, dravite,  
402 uvite, maruyamaite, and synthetic Mg-Al tourmalines (Xu et al. 2016; O'Bannon III  
403 et al. 2018; Berryman et al. 2019; Likhacheva et al. 2019; Chen et al. 2022). There are  
404 two possible reasons for the anisotropic compression behaviors of tourmalines with  $\beta_c$   
405  $> \beta_a$  (Chen et al. 2022). One reason is the incorporation of relatively larger water

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406 molecules in the *c*-parallel structural channels of tourmalines (Bosi 2018). Another  
407 reason is that the [Si<sub>6</sub>O<sub>18</sub>] rings and cationic octahedral layers are arranged in the  
408 *c*-axis direction of tourmalines, which can be refilled with larger cations with large  
409 voids (Bosi and Lucchesi 2007; Bosi 2018).

410 Furthermore, the obtained linear moduli of the schorl in this study and their  
411 pressure derivatives under ambient conditions are different from those reported for the  
412 elbaite ( $K_a = 201$  (4) GPa,  $K_c = 60$  (1) GPa and  $K'_a = 6.9$  (4),  $K'_c = 2.8$  (1)) by Chen et  
413 al. (2022). Based on the relevant analysis of a recent article (Basu et al. 2023), the  
414 evident difference between our results and those of Chen et al. (2022) is the  
415 formalism used in Chen et al. (2022) where the unit-cell parameters were cubed to  
416 obtain a nonexistent volume, and a bulk finite strain formalism was used to determine  
417 axial compressibility. Thus, we refitted the linear moduli and their pressure  
418 derivatives of elbaite using the data from Chen et al. (2022) by the “linearized”  
419 third-order Birch-Murnaghan EoS. The refitted results for elbaite are as follows  
420 (Table 5):  $K_a = 610$  (8) GPa,  $K_c = 182$  (1) GPa,  $K'_a = 20$  (1), and  $K'_c = 8.2$  (1).

421 From Table 5, within their uncertainties, the axial compressibility of the *a*-axis for  
422 the schorl in this study is similar to that of the elbaite in Chen et al. (2022), but the  
423 axial compressibility of the *c*-axis for the schorl is smaller than that of the elbaite (Fig.  
424 4 and Table 5). These results indicate that the axial compressibility anisotropy of the  
425 schorl in this study is larger than that of elbaite. Considering that the *c*-axis of  
426 tourmaline is correlated with the ZO<sub>6</sub> octahedron, the substitution of Al by larger  
427 cations (e.g., Fe) at the *Y* site will reduce the strength of the ZO<sub>6</sub> octahedra along the  
428 *c*-axis and perturb the degree of puckering of the six-membered SiO<sub>4</sub> rings, resulting  
429 in greater compressibility along the *c*-axis direction. Thus, the lower axial  
430 compressibility along the *c*-axis of the schorl can be attributed to the reduced stiffness  
431 of the ZO<sub>6</sub> octahedra.

432 Table 4 also provides a comparison between the  $\alpha_{V0}$  of the schorl obtained in this  
433 study and those from previous studies. The  $\alpha_{V0}$  obtained by *P-V-T* EoS fitting in this  
434 study is ~49% greater than the  $\alpha_{V0}$  obtained for the same schorl sample through *T-V*

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435 EoS fitting by Chen et al. (2023). Because both studies used the same tourmaline  
436 sample, the difference in the  $\alpha_{V0}$  cannot be attributed to compositional variations.

437 Moreover, the obtained  $\alpha_{V0}$  ( $4.39 \times 10^{-5} \text{ K}^{-1}$ ) for a natural uvite from the  $P$ - $V$ - $T$  EoS  
438 fitted by Xu et al. (2016) is more than double or triple the  $\alpha_{V0}$  derived from other  
439 investigations ( $\alpha_{V0} = 1.34\text{-}2.05 \times 10^{-5} \text{ K}^{-1}$ ) via  $T$ - $V$  EoS fitting (Celata et al. 2021;  
440 Ballirano et al. 2022; Chen et al. 2023; Hovis et al. 2023). Excluding the  
441 compositional effects, the  $\alpha_{V0}$  obtained by  $P$ - $V$ - $T$  EoS fitting (this study and Xu et al.  
442 2016) is notably greater than that obtained by  $T$ - $V$  EoS fitting. This phenomenon  
443 occurs not only in tourmalines but also in many other silicate minerals, such as  
444 pyroxene (Hovis et al. 2021; Ye et al. 2021; Xu et al. 2022b), garnet (Gréaux et al.  
445 2011; Fan et al. 2017a), amphibole (Tribaudino et al. 2022), epidote (Li et al. 2021),  
446 clinohumite (Ye et al. 2013; Qin et al. 2017), topaz (Huang et al. 2020; Liu et al.  
447 2023; Zhao et al. 2023), beryl (Fan et al. 2015a). There are likely two main reasons  
448 for this phenomenon. First, the thermal expansion coefficient  $\alpha_T$  is dependent on the  
449 temperature range and temperature interval. Compared with  $T$ - $V$  EoS fitting, the  
450 number of  $T$ - $V$  data points at ambient pressure used for  $P$ - $V$ - $T$  EoS fitting is  
451 significantly lower. For instance, only five  $V$ - $T$  data points between 298 and 673 K  
452 were used for  $P$ - $V$ - $T$  EoS fitting in this study. However, thirteen  $T$ - $V$  data points  
453 between 298 and 663 K were used for  $T$ - $V$  EoS fitting by Chen et al. (2023). Second,  
454  $\alpha_T$  and  $(\partial K/\partial T)_P$  will affect each other in the processing of  $P$ - $V$ - $T$  EoS fitting. Thus, to  
455 obtain an accurate thermal expansion coefficient in future high pressure and high  
456 temperature XRD experiments, narrower temperature intervals and wider temperature  
457 ranges are needed (Liu et al. 2023).

458 Table 4 also shows a comparison of  $(\partial K/\partial T)_P$  for schorl in this study with that for  
459 uvite by Xu et al. (2016). The  $(\partial K/\partial T)_P$  obtained for schorl is in good agreement with  
460 that for uvite within their uncertainties (Table 4). Therefore, based on existing data,  
461 the  $(\partial K/\partial T)_P$  of tourmalines may not be significantly affected by their composition;  
462 this reasoning is similar to the findings of some previous studies (e.g., Nishihara et al.  
463 2005; Zou et al. 2012; Fan et al. 2015b) that considered that the  $(\partial K/\partial T)_P$  for other  
464 silicate minerals exhibit similar values regardless of their mineral chemistry.



## 465 **IMPLICATIONS**

466 In this study, we examined the thermal EoS and stability of schorl at high  
467 temperatures and pressures (up to 673 K and 16 GPa) using synchrotron radiation  
468 XRD. Depending on the exact chemistry of tourmaline, the expected thermodynamic  
469 stability of tourmaline ranged between 5-7 GPa at 500 °C, and between 800-1000 °C  
470 at 4 GPa (Ota et al. 2008; Dutrow and Henry 2011; van Hinsberg et al. 2011; Henry  
471 and Dutrow 2012).

472 Our results on the thermal EoS are vital thermodynamic data that can aid in the  
473 refinement of the  $P$ - $T$  stability field of tourmaline. For full thermodynamic data,  
474 enthalpy, entropy, and heat capacity results are crucial and available for limited  
475 chemistry (Garofalo et al. 2000; Ogradova et al. 2004; 2012). Tourmalines (e.g.,  
476 schorl and uvite) likely have the potential to transport light elements into the Earth's  
477 interior via subduction zones and can release the light elements once they decompose  
478 as the geotherm intersects the  $P$ - $T$  phase boundary. The released light elements  
479 accordingly affect the geochemical processes in the deep Earth (Nakano and  
480 Nakamura 2001; Bebout and Nakamura 2003; Zack et al. 2003; Bebout et al. 2007).  
481 For example, the breakdown of tourmaline can cause the release of boron, which  
482 largely influences the boron budget during the subduction of Earth's crust to mantle  
483 depths at convergent plate margins (Guo et al. 2022). Therefore, this potentially  
484 results in mantle B isotope anomalies near convergent margins (Nakano and  
485 Nakamura 2001). Moreover, in the subduction zones, as the pressure and temperature  
486 of the slab increase, the decomposition of the lithium-bearing minerals (e.g.,  
487 tourmaline, phengite, and epidote) releases the fluxing elements such as lithium and  
488 fluorine, which can induce partial melting and form lithium-rich magmatism (e.g.,  
489 Halama et al. 2009; Li et al. 2018; Liu et al. 2020). Simultaneously, weathering in arid  
490 areas in the hinterland of an orogenic belt can promote lithium enrichment in the basin,  
491 leading to the formation of lithium deposits (e.g., Sun et al. 2007; Chen et al. 2014).

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871 **Figure Captions**

872 **Figure 1.** Crystal structure of schorl, visualized using the software package  
873 CrystalMaker. (Color online)

874 **Figure 2.** Representative X-ray diffraction patterns of schorl in this study up to 15.50  
875 GPa and 673 K.

876 **Figure 3.** The volumetric compression of schorl, the solid circles represent the data  
877 points of schorl in this study, the hollow square represent the data points of schorl  
878 from Li et al. (2004), the hollow circles represent the data points of elbaite from Chen  
879 et al. (2022), and the solid line was obtained by third-order Birch-Murnaghan EoS  
880 fitting of schorl in this study.

881 **Figure 4.** The axial compression ( $a/a_0$ : black font;  $c/c_0$ : red font), the solid circles  
882 represent the data points of schorl in this study, the hollow square represent the data  
883 points of schorl from Li et al. (2004), the hollow circles represent the data points of  
884 elbaite from Chen et al. (2022), and the solid lines were obtained by third-order  
885 Birch-Murnaghan EoS fitting of schorl in this study. (Color online)

886 **Figure 5.** Volumetric (a) and axial (b and c) Eulerian strain-normalized pressure  
887 ( $F_E-f_E$ ) plot of schorl. The solid lines represent the linear fit through the data.

888 **Figure 6.** Unit-cell volume of schorl as a function of pressure and temperature. The  
889 solid lines represent isothermal compression curve from fitting High-temperature  
890 Birch-Murnaghan EoS at 300, 373, 473, 573, and 673 K with the following  
891 parameters:  $V_0 = 1581.2 \pm 0.2 \text{ \AA}^3$ ,  $K_0 = 110.5 \pm 0.6 \text{ GPa}$ ,  $K'_0 = 4.6 \pm 0.2$ ,  $(\partial K_T/\partial T)_P =$   
892  $-0.012 \pm 0.003 \text{ GPa K}^{-1}$  and  $\alpha_0 = (2.4 \pm 0.2) \times 10^{-5} \text{ K}^{-1}$ . The error bars of the data points  
893 are smaller than the symbols.

894 **Figure 7.** The variation of  $K_0$  of Fe-bearing tourmalines with Fe content at Y site ( $X_{\text{Fe}}$ ,  
895  $\text{Fe}/\text{Fe}+\text{Mg}+\text{Li}+\text{Al}$ ). The solid line represents a linear fit to the  $K_0$  values of Fe-bearing  
896 tourmalines.

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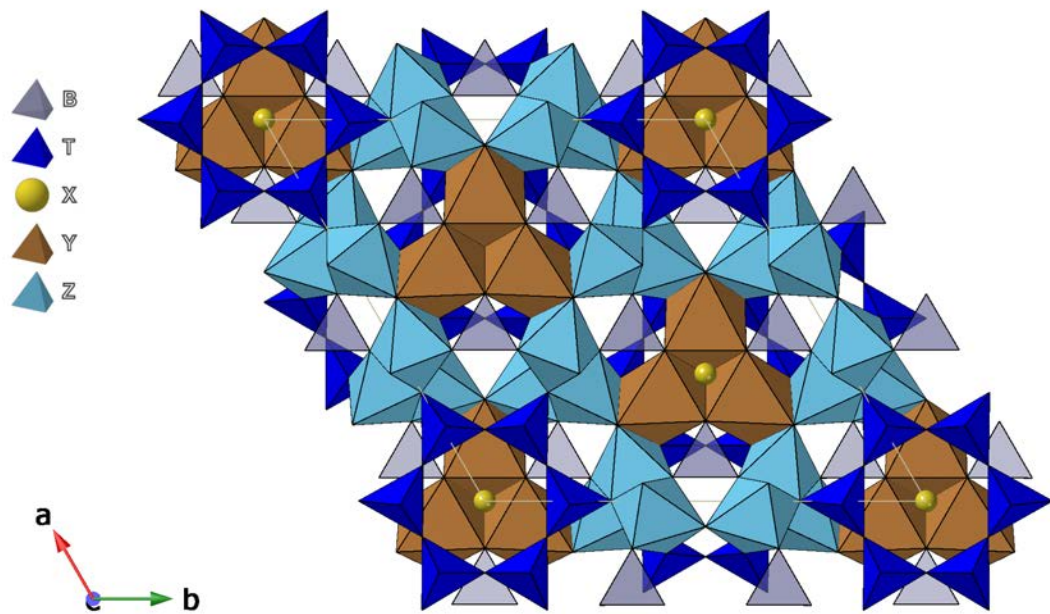
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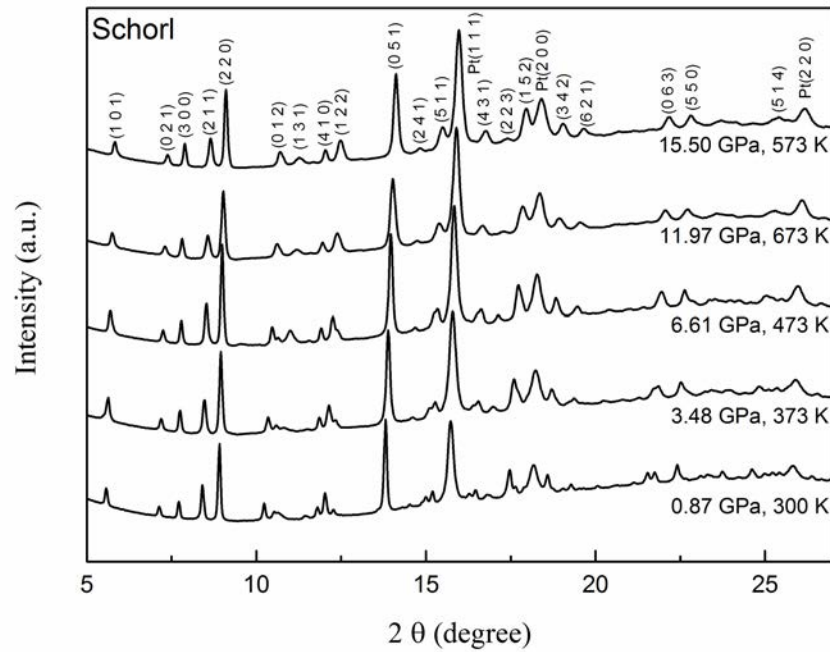
901 **Figure 1**





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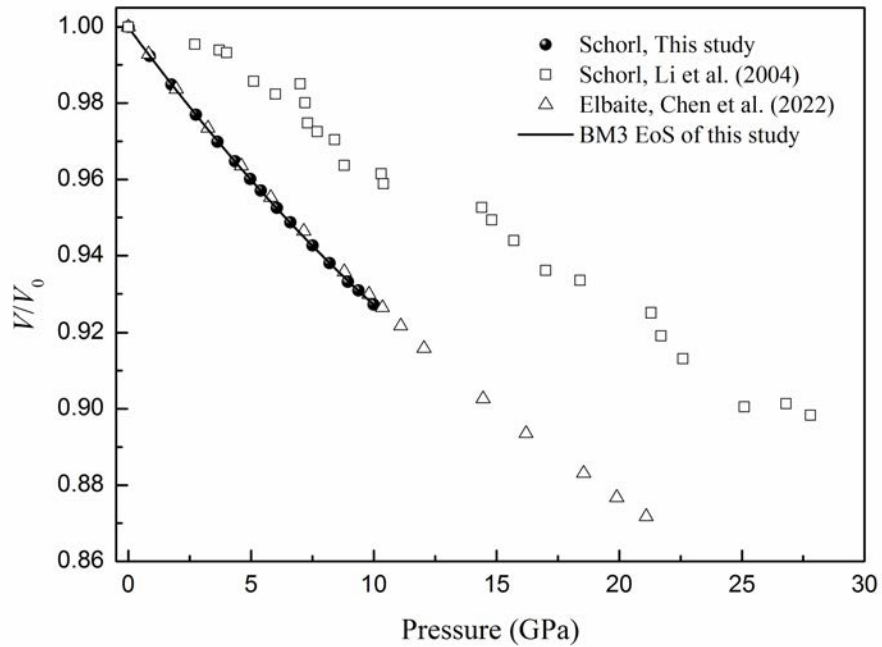
921 **Figure 2**



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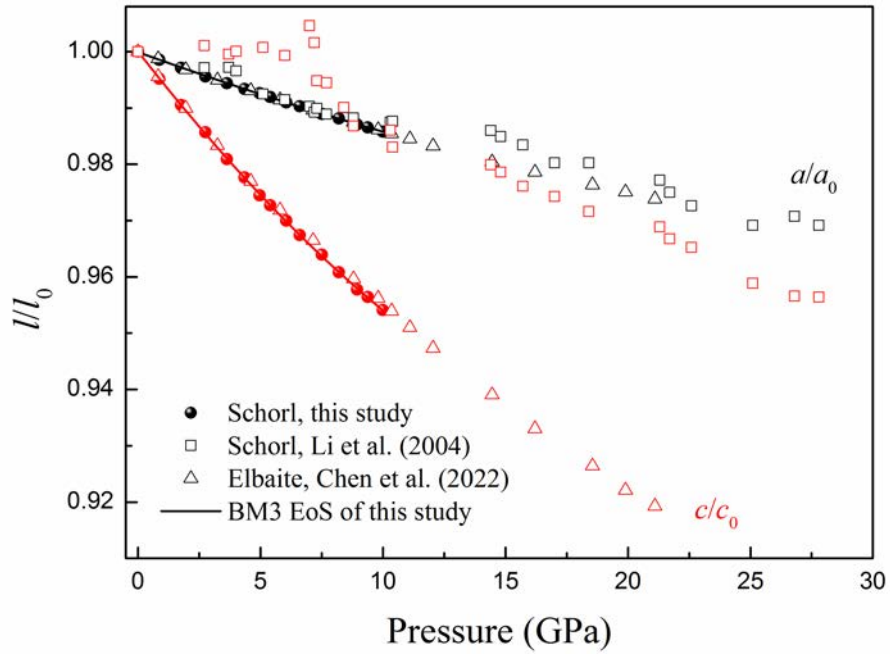
939 **Figure 3**



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957 **Figure 4**



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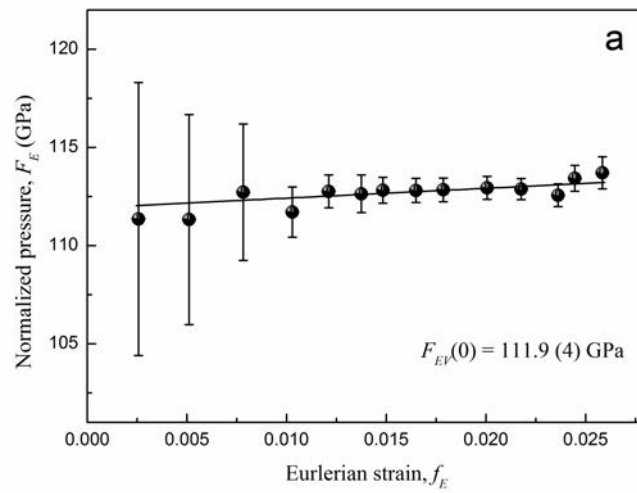
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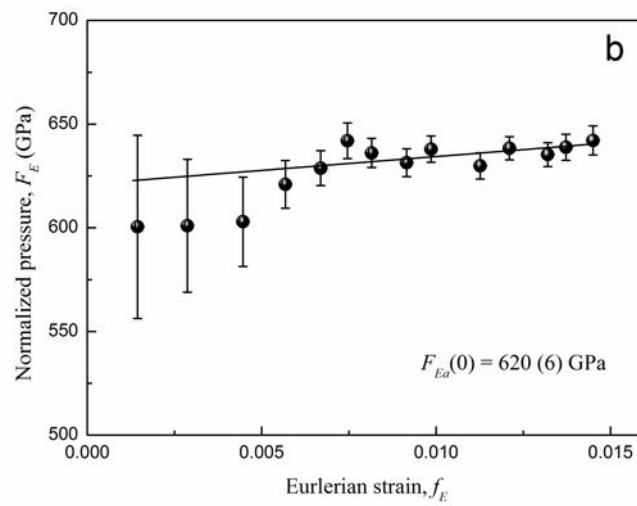
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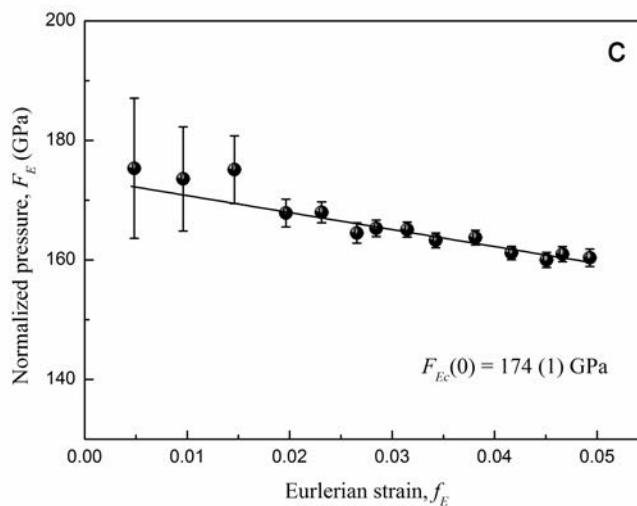
975 **Figure 5**



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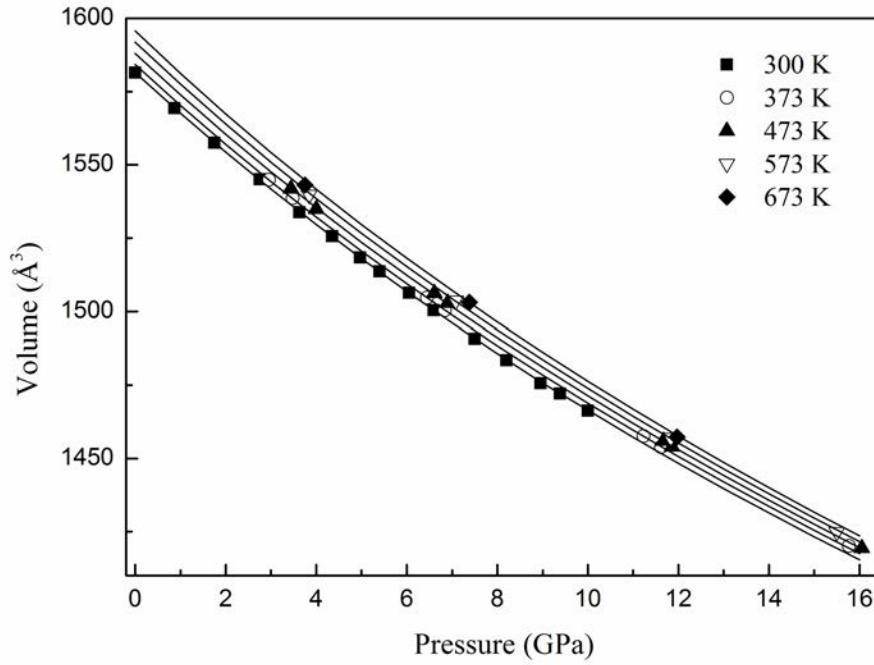
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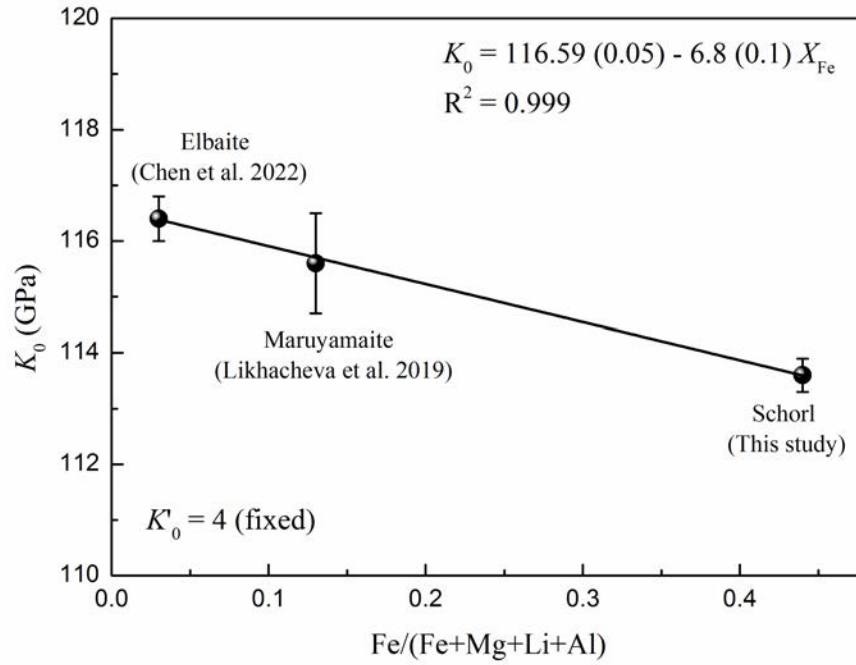
980 **Figure 6**



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998 **Figure 7**



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**Table 1** Chemical compositions of schorl in this study

Compositions (wt.%) (6) <sup>a</sup>	Schorl
SiO <sub>2</sub>	36.03(22)
TiO <sub>2</sub>	0.23(3)
Al <sub>2</sub> O <sub>3</sub>	33.58(31)
B <sub>2</sub> O <sub>3</sub> *	10.35(27)
Cr <sub>2</sub> O <sub>3</sub>	0.01(1)
MgO	0.30(7)
FeO <sup>b</sup>	9.35(5)
MnO	0.30(1)
ZnO	0.08(2)
CaO	0.21(1)
Li <sub>2</sub> O*	1.09(8)
Na <sub>2</sub> O	2.29(5)
K <sub>2</sub> O	0.05(1)
P <sub>2</sub> O <sub>5</sub>	0.01(1)
F	0.05(4)
Total	93.93

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Data in the parentheses of compositions represent standard derivations

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<sup>a</sup> Number of electron microprobe analyses in parentheses

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<sup>b</sup> Total Fe as FeO

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\* LA-ICP-MS analyses

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1043 **Table 2** Unit-cell parameters and volumes of schorl at high pressure and room temperature  
1044 conditions

<i>P</i> (GPa)	<i>a</i> (Å) ( <i>Pt</i> )	<i>a</i> (Å)	<i>c</i> (Å)	<i>V</i> (Å <sup>3</sup> )	<i>a/c</i>
0.0001	-	15.9532(3)	7.1751(3)	1581.45(5)	2.2234
0.87(5)	3.91904(9)	15.9303(10)	7.1406(11)	1569.3(3)	2.2309
1.75(8)	3.91499(9)	15.9076(12)	7.1071(13)	1557.5(4)	2.2383
2.75(8)	3.91046(9)	15.8825(14)	7.0725(13)	1545.0(5)	2.2457
3.63(3)	3.90655(8)	15.8633(14)	7.0382(13)	1533.8(5)	2.2539
4.35(1)	3.90338(8)	15.8475(13)	7.0147(14)	1525.7(5)	2.2592
4.97(3)	3.90069(9)	15.8355(13)	6.9919(13)	1518.4(5)	2.2648
5.40(1)	3.89885(9)	15.8247(13)	6.9793(13)	1513.6(5)	2.2674
6.05(1)	3.89608(8)	15.8091(14)	6.9595(13)	1506.3(6)	2.2716
6.60(1)	3.89376(9)	15.7983(14)	6.9413(14)	1500.4(6)	2.2760
7.50(1)	3.89001(8)	15.7765(16)	6.9163(15)	1490.8(6)	2.2811
8.20(1)	3.88713(9)	15.7636(15)	6.8937(15)	1483.5(7)	2.2867
8.95(1)	3.88408(8)	15.7467(17)	6.8720(18)	1475.7(7)	2.2914
9.38(3)	3.88235(9)	15.7387(18)	6.8623(17)	1472.1(8)	2.2935
10.00(5)	3.87988(9)	15.7268(20)	6.8456(19)	1466.3(9)	2.2974

1045 Numbers in parenthesis represent standard deviations.

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**Table 3** Unit-cell volumes of schorl at high pressure and high temperature conditions

<i>P</i> (GPa)	<i>a</i> (Å) ( <i>Pt</i> )	<i>T</i> (K)	<i>a</i> (Å)	<i>c</i> (Å)	<i>V</i> (Å <sup>3</sup> )
2.96(3)	3.91192(8)	373	15.8835(11)	7.0712(12)	1545.0(1)
3.48(4)	3.90959(7)	373	15.8726(12)	7.0517(13)	1538.6(4)
6.45(8)	3.89666(9)	373	15.8055(11)	6.9546(14)	1504.6(3)
6.84(7)	3.89501(8)	373	15.7977(13)	6.9420(13)	1500.4(4)
11.23(6)	3.87715(8)	373	15.7065(12)	6.8228(16)	1457.6(3)
11.62(6)	3.87562(9)	373	15.6987(13)	6.8122(13)	1453.9(5)
15.77(7)	3.85992(9)	373	15.6247(18)	6.7167(17)	1420.1(8)
3.44(5)	3.91309(9)	473	15.8782(15)	7.0618(15)	1541.9(5)
4.00(6)	3.91057(8)	473	15.8654(12)	7.0414(16)	1535.0(4)
6.61(5)	3.89914(8)	473	15.8075(15)	6.9604(13)	1506.2(6)
6.90(7)	3.89790(9)	473	15.8013(13)	6.9508(14)	1503.0(6)
11.67(6)	3.87836(8)	473	15.7045(18)	6.8171(16)	1456.1(8)
11.86(7)	3.87761(8)	473	15.7006(17)	6.8113(15)	1454.1(8)
16.05(5)	3.86165(8)	473	15.6229(14)	6.7150(16)	1419.4(7)
3.84(8)	3.91464(9)	573	15.8741(16)	7.0558(18)	1539.8(8)
7.08(9)	3.90033(8)	573	15.8022(18)	6.9535(17)	1503.7(8)
11.83(6)	3.88070(8)	573	15.7071(13)	6.8194(13)	1457.0(4)
15.50(4)	3.86651(9)	573	15.6373(12)	6.7285(12)	1424.9(3)
3.75(5)	3.91847(9)	673	15.8804(13)	7.0656(15)	1543.1(5)
7.38(7)	3.90225(8)	673	15.8018(17)	6.9507(15)	1503.1(7)
11.97(5)	3.88315(9)	673	15.7082(14)	6.8199(14)	1457.3(5)

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Numbers in parenthesis represent standard deviations.

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1079 **Table 4** The thermal equation of state parameters of tourmalines

Sample	$K_0$ (GPa)	$K'_0$	$V_0$ (Å <sup>3</sup> )	$\alpha_{V0}$ ( $\times 10^{-5} \text{K}^{-1}$ )	$(\partial K/\partial T)_P$ (GPaK <sup>-1</sup> )	References
Schorl	111.6(9)	4.4(2)	1581.45(25)	—	—	This study
	111.6(4)	4.4(1)	1581.45(fixed)	—	—	This study
	113.6(3)	4.0(fixed)	1581.04(20)	—	—	This study
	110.5(6)	4.6(2)	1581.2(2)	2.4(2)	-0.012(3)	This study
	—	—	1581.41(4)	1.61(3)	—	Chen et al. (2023)
Schorl	184(4)	4.0(fixed)	1595.52(198)	—	—	Li et al. (2004)
Elbaite	114.7(7)	4.2(1)	1540.7(6)	—	—	Chen et al. (2022)
	116.4(4)	4.0(fixed)	1540.1(4)	—	—	Chen et al. (2022)
Maruyamaite	112(3)	4.5(4)	1588(1)	—	—	Likhacheva et al. (2022)
	115.6(9)	4.0(fixed)	1587.2(7)	—	—	Likhacheva et al. (2022)
Uvite	96.6(9)	12.5(4)	1537.1(11)	4.39(27)	-0.009(6)	Xu et al. (2016)

1080 Numbers in parenthesis represent standard deviations.

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**Table 5** The axial compressibility of tourmaline

Sample	$K_a$ (GPa)	$K'_a$	$a_0$ (Å)	$K_c$ (GPa)	$K'_c$	$c_0$ (Å)	References
Schorl	621(9)	16(3)	15.9532(3)	174(2)	8.7(5)	7.1751(3)	This study
Elbaite <sup>a</sup>	610(8)	20(1)	15.8305(9)	182(1)	8.2(1)	7.0991(9)	Chen et al. (2022)

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<sup>a</sup> Refitting using the data presented in Chen et al. (2022). Numbers in parenthesis represent standard deviations.