

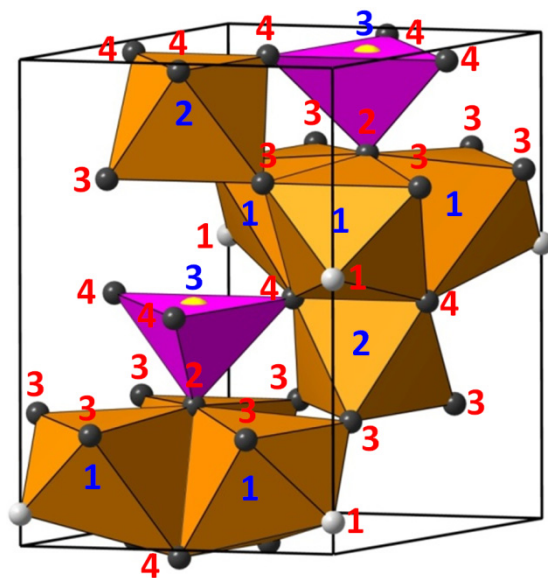
Supplement for the article: PDF analysis of ferrihydrite: Critical assessment of the underconstrained akdalaite model

Figure S1. Structure of the akdalaite model and its parametrization in PDFgui

Polyhedral representation of the akdalaite unit cell. Independent atoms in the asymmetric unit are labeled.

Screen shot of the PDFgui interface window showing the parametrization of the akdalaite model. Symmetry-related positions in the full cell were generated from the asymmetric unit and symmetry constraints of the $P6_3mc$ space group.

Screen shot of the initial and refined parameter values. The Fe1 site occupancy was fixed to 1.0 to reduce correlations (19 parameters adjusted).



Phase Constraints

a

@4

alpha

b

@4

beta

c

@5

gamma

Scale Factor

delta1

@6

sratio

delta2

spdiameter

@8

Included Pairs

all-all

	elem	x	y	z	u11	u22	u33	u12	u13	u23	occ
1	Fe 1	@11	-@11 +1	@12	@100	@100	@100				@301
2	Fe 1	@11	+2*@11	@12	@100	@100	@100				@301
3	Fe 1	-2*@11 +1	-@11 +1	@12	@100	@100	@100				@301
4	Fe 1	-@11 +1	@11	@12 -0.5	@100	@100	@100				@301
5	Fe 1	-@11 +1	-2*@11 +1	@12 -0.5	@100	@100	@100				@301
6	Fe 1	+2*@11	@11	@12 -0.5	@100	@100	@100				@301
7	Fe 2			@13	@100	@100	@100				@302
8	Fe 2			@13 +0.5	@100	@100	@100				@302
9	Fe 3			@15	@100	@100	@100				@303
10	Fe 3			@15 -0.5	@100	@100	@100				@303
11	O 1			@16	@200	@200	@200				
12	O 1			@16 +0.5	@200	@200	@200				
13	O 2			@17	@200	@200	@200				
14	O 2			@17 +0.5	@200	@200	@200				
15	O 3	@18	-@18 +1	@19	@200	@200	@200				
16	O 3	@18	+2*@18	@19	@200	@200	@200				
17	O 3	-2*@18 +1	-@18 +1	@19	@200	@200	@200				
18	O 3	-@18 +1	@18	@19 +0.5	@200	@200	@200				
19	O 3	-@18 +1	-2*@18 +1	@19 +0.5	@200	@200	@200				
20	O 3	+2*@18	@18	@19 +0.5	@200	@200	@200				
21	O 4	@20	-@20 +1	@21	@200	@200	@200				
22	O 4	@20	+2*@20 -1	@21	@200	@200	@200				
23	O 4	-2*@20 +2	-@20 +1	@21	@200	@200	@200				
24	O 4	-@20 +1	@20	@21 -0.5	@200	@200	@200				
25	O 4	-@20 +1	-2*@20 +2	@21 -0.5	@200	@200	@200				
26	O 4	+2*@20 -1	@20	@21 -0.5	@200	@200	@200				

	Initial	Fixed	Refined
@ 1	1.3	<input type="checkbox"/>	1.26078215171
@ 2	0.137	<input type="checkbox"/>	0.0735800893587
@ 4	5.928	<input type="checkbox"/>	5.94375215241
@ 5	9.126	<input type="checkbox"/>	9.16963651216
@ 6	1.8	<input type="checkbox"/>	1.88517177714
@ 8	35.0	<input checked="" type="checkbox"/>	35.0
@ 11	0.1695	<input type="checkbox"/>	0.16918043634
@ 12	0.6365	<input type="checkbox"/>	0.63630493601
@ 13	0.3379	<input type="checkbox"/>	0.331055495526
@ 15	0.9595	<input type="checkbox"/>	0.953356338802
@ 16	0.0446	<input type="checkbox"/>	0.0659270295649
@ 17	0.7634	<input type="checkbox"/>	0.769203681119
@ 18	0.1697	<input type="checkbox"/>	0.167758743399
@ 19	0.2467	<input type="checkbox"/>	0.244748555132
@ 20	0.5227	<input type="checkbox"/>	0.523994536215
@ 21	0.9796	<input type="checkbox"/>	0.980284557646
@100	0.011	<input type="checkbox"/>	0.0117534396498
@200	0.007	<input type="checkbox"/>	0.00384039869658
@301	1.0	<input checked="" type="checkbox"/>	1.0
@302	0.97	<input type="checkbox"/>	0.855348533147
@303	0.96	<input type="checkbox"/>	0.861677349147

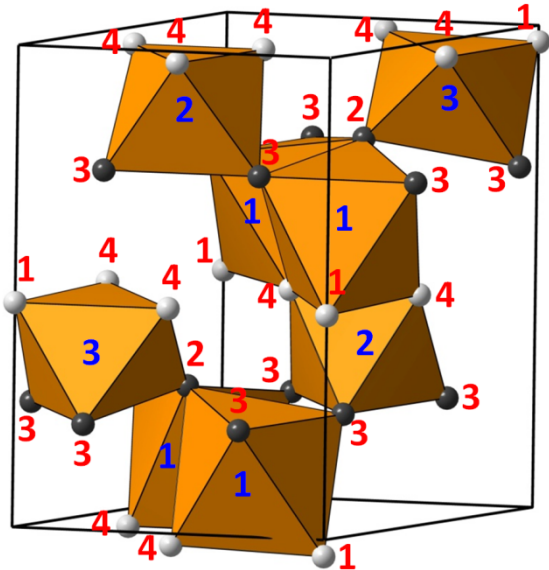
@1 is the scale factor and @2 is the resolution dampening (Q_{damp}). Q_{broad} was fixed to 0.069 \AA^{-1} . Full results are listed in Table S2.

Figure S2. Structure of the modified akdalaite model and its parametrization in PDFgui

Polyhedral representation of the modified akdalaite unit cell. Independent atoms in the asymmetric unit are labeled. The oxygen atoms and hydroxyls are positioned as in the f-phase (Fig. 1).

Screen shot of the PDFgui interface window showing the parametrization of the modified akdalaite model.

Screen shot of the initial and refined parameter values.



Phase Constraints												
a @4		b @4		c @5								
alpha		beta		gamma								
Scale Factor												
delta1		delta2		spdiameter @8								
sratio @6												
Included Pairs		all-all										
	elem	x	y	z	u11	u22	u33	u12	u13	u23	occ	
1	Fe 1	@11	+2*@11	@12	@100	@100	@100				@301	
2	Fe 1	-2*@11 +1	-@11 +1	@12	@100	@100	@100				@301	
3	Fe 1	-@11 +1	-2*@11 +1	@12 -0.5	@100	@100	@100				@301	
4	Fe 1	+2*@11	@11	@12 -0.5	@100	@100	@100				@301	
5	Fe 2			@13	@100	@100	@100				@302	
6	Fe 2			@13 +0.5	@100	@100	@100				@302	
7	Fe 3	@14	-@14 +1	@15	@100	@100	@100				@303	
8	Fe 3	-@14 +1	@14	@15 -0.5	@100	@100	@100				@303	
9	O 1			@16	@200	@200	@200					
10	O 1			@16 +0.5	@200	@200	@200					
11	O 2			@17	@200	@200	@200					
12	O 2			@17 +0.5	@200	@200	@200					
13	O 3	@18	-@18 +1	@19	@200	@200	@200					
14	O 3	@18	+2*@18	@19	@200	@200	@200					
15	O 3	-2*@18 +1	-@18 +1	@19	@200	@200	@200					
16	O 3	-@18 +1	@18	@19 +0.5	@200	@200	@200					
17	O 3	-@18 +1	-2*@18 +1	@19 +0.5	@200	@200	@200					
18	O 3	+2*@18	@18	@19 +0.5	@200	@200	@200					
19	O 4	@20	-@20 +1	@21	@200	@200	@200					
20	O 4	@20	+2*@20 -1	@21	@200	@200	@200					
21	O 4	-2*@20 +2	-@20 +1	@21	@200	@200	@200					
22	O 4	-@20 +1	@20	@21 -0.5	@200	@200	@200					
23	O 4	-@20 +1	-2*@20 +2	@21 -0.5	@200	@200	@200					
24	O 4	+2*@20 -1	@20	@21 -0.5	@200	@200	@200					

	Initial	Fixed	Refined
@ 1	1.3	<input type="checkbox"/>	1.46023322482
@ 2	0.137	<input type="checkbox"/>	0.0797513125045
@ 4	5.928	<input type="checkbox"/>	5.95041595549
@ 5	9.126	<input type="checkbox"/>	9.13279706467
@ 6	1.0	<input type="checkbox"/>	0.461806863636
@ 8	35.0	<input checked="" type="checkbox"/>	35.0
@ 11	0.1695	<input type="checkbox"/>	0.17491586752
@ 12	0.6365	<input checked="" type="checkbox"/>	0.6365
@ 13	0.3379	<input type="checkbox"/>	0.320720779344
@ 14	0.1697	<input type="checkbox"/>	0.169786935837
@ 15	0.85	<input type="checkbox"/>	0.842817540034
@ 16	-0.0446	<input type="checkbox"/>	-0.0344265657565
@ 17	0.7634	<input type="checkbox"/>	0.779493448447
@ 18	0.1697	<input type="checkbox"/>	0.167311652982
@ 19	0.2467	<input type="checkbox"/>	0.233612214827
@ 20	0.5227	<input type="checkbox"/>	0.528761606496
@ 21	0.9796	<input type="checkbox"/>	0.971194873621
@ 100	0.011	<input type="checkbox"/>	0.00697294046269
@ 200	0.007	<input type="checkbox"/>	0.00563328878938
@ 301	1.0	<input checked="" type="checkbox"/>	1.0
@ 302	0.97	<input type="checkbox"/>	1.05785376365
@ 303	0.96	<input type="checkbox"/>	0.83144015261

The z(Fe1) position was fixed during the refinement to the value of Michel et al. (2007) to limit the total number of fitted parameters to 19. Full results are listed in Table S3.

Table S1. Results from the akdalaite fit to the 6Fh PDF with 20 adjusted parameters

* Mon Mar 25 09:17:47 2013

[illegible]

DATA SET : 1 (string)

Data range in r [Å] : 1.38 -> 20 Step dr : 0.02
Calculated range : 1.38 -> 21.7952
Refinement r range : 1.38 -> 20 Data pts : 0 -> 931
Reduced chi squared : 0.222497
Rw - value : 0.297642

Experimental settings :
Radiation : X-Rays
Termination at Qmax : 21 Å⁻¹
DQ dampening Qdamp : 0.0727986 (0.007) Å⁻¹
DQ broadening Qbroad : 0.069 Å⁻¹
Scale factor : 1.37253 (0.089)

Selected phases and atoms for this data set :

Phase 1 :
Atoms (i) : FE O
Atoms (j) : FE O

Relative phase content in terms of

	atoms	unit cells	mass
Phase 1 : 1		1	1

PARAMETER INFORMATION :

Number of constraints : 157
Number of refined parameters : 20
Number of fixed parameters : 1

Refinement parameters :

1: 1.37253 (0.089)	2: 0.0727986 (0.007)	4: 5.9395 (0.0092)
5: 9.17173 (0.025)	6: 1.81458 (0.21)	8: 35
11: 0.170377 (0.001)	12: 0.638305 (2.2e+04)	13: 0.334625 (2.2e+04)
15: 0.953882 (2.2e+04)	16: 0.0612022 (2.2e+04)	17: 0.757992 (2.2e+04)
18: 0.171725 (0.0041)	19: 0.246359 (2.2e+04)	20: 0.519454 (0.0035)
21: 0.977773 (2.2e+04)	100: 0.0105771 (0.0011)	200: 0.0105045 (0.0024)
301: 0.82616 (0.076)	302: 0.736728 (0.18)	303: 0.815759 (0.14)

REFINEMENT INFORMATION:

Number of iterations : 5
Reduced chi squared : 0.204832
Rw - value : 0.285582

Correlations greater than 0.8 :

Corr(p[12], p[13]) = 1
Corr(p[12], p[15]) = 1
Corr(p[12], p[16]) = 1
Corr(p[12], p[17]) = 1
Corr(p[12], p[19]) = 1
Corr(p[12], p[21]) = 1
Corr(p[13], p[15]) = 1
Corr(p[13], p[16]) = 1
Corr(p[13], p[17]) = 1
Corr(p[13], p[19]) = 1
Corr(p[13], p[21]) = 1
Corr(p[15], p[16]) = 1
Corr(p[15], p[17]) = 1
Corr(p[15], p[19]) = 1
Corr(p[15], p[21]) = 1
Corr(p[16], p[17]) = 1
Corr(p[16], p[19]) = 1
Corr(p[16], p[21]) = 1
Corr(p[17], p[19]) = 1
Corr(p[17], p[21]) = 1
Corr(p[19], p[21]) = 1
Corr(p[302], p[303]) = -0.823727

Table S2. Results from the akdalaite fit to the 6Fh PDF with 19 adjusted parameters

* Mon Mar 25 09:19:53 2013

[illegible]

DATA SET : 1 (string)

Data range in r [Å] : 1.38 -> 20 Step dr : 0.02
Calculated range : 1.38 -> 21.7952
Refinement r range : 1.38 -> 20 Data pts : 0 -> 931
Reduced chi squared : 0.183335
Rw - value : 0.270329

Experimental settings :
Radiation : X-Rays
Termination at Qmax : 21 Å⁻¹
DQ dampening Qdamp : 0.0735801 (0.0062) Å⁻¹
DQ broadening Qbroad : 0.069 Å⁻¹
Scale factor : 1.26078 (0.048)

Selected phases and atoms for this data set :

Phase 1 :
Atoms (i) : FE O
Atoms (j) : FE O

Relative phase content in terms of
atoms unit cells mass
Phase 1 : 1 1 1

PARAMETER INFORMATION :

Number of constraints : 157
Number of refined parameters : 19
Number of fixed parameters : 2

Refinement parameters :
1: 1.26078 (0.048) 2: 0.0735801 (0.0062) 4: 5.94375 (0.0083)
5: 9.16964 (0.023) 6: 1.88517 (0.0072) 8: 35
11: 0.16918 (0.0011) 12: 0.636305 13: 0.331055
15: 0.953356 16: 0.065927 17: 0.769204
18: 0.167759 (0.0027) 19: 0.244749 20: 0.523995 (0.003)
21: 0.980285 100: 0.0117534 (0.0011) 200: 0.0038404 (0.0016)
301: 1 302: 0.855349 (0.2) 303: 0.861677 (0.15)

REFINEMENT INFORMATION:

Number of iterations : 22
Reduced chi squared : 0.182609
Rw - value : 0.269793

Correlations greater than 0.8 :

Corr(p[302], p[303]) = -0.866634

Table S3. Results from the modified akdalaite fit to the 6Fh PDF with 19 adjusted parameters

* Mon Mar 25 10:00:51 2013

[illegible]

DATA SET : 1 (string)

Data range in r [Å]	: 1.38	-> 20	Step dr	: 0.02
Calculated range	: 1.38	-> 21.7952		
Refinement r range	: 1.38	-> 20	Data pts	: 0 -> 931
Reduced chi squared	: 0.270855			
Rw - value	: 0.328578			

Experimental settings :

Radiation	: X-Rays
Termination at Qmax	: 21 Å ⁻¹
DQ dampening Qdamp	: 0.0797513 (0.0059) Å ⁻¹
DQ broadening Qbroad	: 0.069 Å ⁻¹
Scale factor	: 1.46023 (0.071)

Selected phases and atoms for this data set :

Phase 1 :

Atoms (i)	: FE O
Atoms (j)	: FE O

Relative phase content in terms of

	atoms	unit cells	mass
Phase 1	: 1	1	1

PARAMETER INFORMATION :

Number of constraints	: 147
Number of refined parameters	: 19
Number of fixed parameters	: 3

Refinement parameters :

1: 1.46023 (0.071)	2: 0.0797513 (0.0059)	4: 5.95042 (0.0071)
5: 9.1328 (0.02)	6: 0.461807 (0.1)	8: 35
11: 0.174916 (0.00091)	12: 0.6365	13: 0.320721 (0.0029)
14: 0.169787 (0.0033)	15: 0.842818 (0.0023)	16: -0.0344266 (0.0046)
17: 0.779493 (0.0041)	18: 0.167312 (0.0026)	19: 0.233612 (0.0033)
20: 0.528762 (0.0019)	21: 0.971195 (0.0019)	100: 0.00697294 (0.00075)
200: 0.00563329 (0.0014)	301: 1	302: 1.05785 (0.13)
303: 0.83144 (0.16)		

REFINEMENT INFORMATION:

Number of iterations	: 22
Reduced chi squared	: 0.268319
Rw - value	: 0.327036

Correlations greater than 0.8 :

*** none ***
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