

## SUPPLEMENTS

**Supplement Table S1:** Variables and measured quantities in the manuscript text and supplement table 2. Those in the manuscript figures and tables are explained in their captions.

Symbol	Unit	Definition	Principal occurrence
$\phi$	(degrees)	angle between the track axis and the apatite <i>c</i> -axis (track angle)	figure 2
$\phi_{30}$	(degrees)	measured track angle $\phi$ after 30 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	supplement 2
$\phi_{45}$	(degrees)	measured track angle $\phi$ after 45 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	supplement 2
$\phi_M$	(degrees)	average of measured track angles ( $\phi_{30}$ and $\phi_{45}$ )	supplement 2
$\phi'_M$	(degrees)	orientation perpendicular to the track ( $90 - \phi_M$ )	supplement 2
$\theta$	(degrees)	angle between facing edges of the etched track channel	figure 2; equation 3
$\theta_{30}$	(degrees)	measured cone angle $\theta$ after 30 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	supplement 2
$\theta_{45}$	(degrees)	measured cone angle $\theta$ after 45 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	supplement 2
$\theta_M$	(degrees)	average of measured cone angles ( $\theta_{30}$ and $\theta_{45}$ )	supplement 2
$\eta_E$	-	traditional track etching efficiency	equation 1
$l_{30}$	μm	track length measured after 30 s immersion in 5.5 M HNO <sub>3</sub> at 21°C	figure 2; supplement 2
$l_{45}$	μm	track length measured after 45 s immersion in 5.5 M HNO <sub>3</sub> at 21°C	figure 2; supplement 2
$\Delta l$	μm	track length increase from 30 s to 45 s ( $\Delta l = l_{45} - l_{30}$ )	figure 2; equation 4; supplement 2
$w_{30}$	μm	track width measured after 30 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	figure 2; supplement 2
$w_{45}$	μm	track width measured after 45 s immersion in 5.5 M HNO <sub>3</sub> at 21 °C	figure 2; supplement 2
$\Delta w$	μm	track width increase from 30 s to 45 s ( $\Delta w = w_{45} - w_{30}$ )	figure 2; equation 2; supplement 2
$t_{E30}$	s	effective track etch time after 30 s immersion in 5.5 M HNO <sub>3</sub> at 21°C	equation 5; supplement 2
$t_{E45}$	s	effective track etch time after 45 s immersion in 5.5 M HNO <sub>3</sub> at 21°C	equation 6; supplement 2
$\Delta t_E$	s	etch time increment ( $\Delta t_E = t_{E45} - t_{E30} = 15$ s)	equations 2 and 4; supplement 2
$v_B$	μm/min	traditional bulk etch rate of "undamaged" apatite (i.e. outside the track core)	equation 1; supplement 2
$v_T$	μm/min	etch rate of the disordered track core along the track axis (track etch rate)	figure 2c; equation 3; supplement 2
$v_R$	μm/min	etch rate of the plane perpendicular to the etch rate vector (apatite etch rate)	figure 2c; equation 2; supplement 2
$v_L$	μm/min	measured rate of track length increase resulting from intermittent damage	figure 2c; equation 4; supplement 2
$v_S$	μm/min	apatite etch rate perpendicular to the polished surface (surface etch rate)	figure 9
$\rho_L$	cm <sup>-2</sup>	number of unetched (latent) tracks intersecting 1 cm <sup>2</sup> of the mineral surface	manuscript text
$\rho_E$	cm <sup>-2</sup>	counted number of track etch channels intersecting 1 cm <sup>2</sup> of mineral surface	manuscript text

**Supplement Table S2:** AM 7614 supplement table 2.xls